A tunable multivariable nonlinear robust observer for biological systems

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Received 7 March 2004; accepted after revision 9 November 2004
Available online 16 February 2005
Presented by Pierre Auger

Abstract

This paper presents a robust nonlinear asymptotic observer with adjustable convergence rate with a great potential of applicability for biological systems in which the main state variables are difficult and expensive to measure or such measurements do not exist. This observer scheme is based on the classical asymptotic observer, which is modified to allow the tuning of the convergence rate. It is shown that the proposed observer provides fast and satisfactory estimates when facing load disturbances, system failures and parameter uncertainty while maintaining the excellent robustness and stability properties of the classical asymptotic observer. The implementation of the tunable observer is carried out by numerical simulations of a mathematical model of an anaerobic digestion process used for wastewater treatment. The key results are examined and further developed. To cite this article: V. Alcaraz-González et al., C. R. Biologies 328 (2005).

Résumé

Un observateur multi-variable, robuste et non-linéaire, à vitesse de convergence réglable pour des systèmes biologiques. Cet article présente un observateur non-linéaire à vitesse de convergence réglable pour les systèmes biologiques, dont les principales variables d’état sont difficilement mesurables. Cet observateur est basé sur le principe de l’observateur asymptotique, dont l’intérêt a déjà été largement démontré dans la littérature, mais il est modifié pour permettre à l’utilisateur d’en régler la vitesse de convergence. Il est en particulier démontré au sein de cet article que l’observateur proposé fourni des estimations rapides et satisfaisantes vis-à-vis de perturbations affectant le procédé, de défaillances du système et d’incertitudes paramétriques liées au modèle utilisé, alors que les bonnes propriétés de stabilité et de robustesse de l’observateur asymptotique...
1. Introduction

In recent years, there has been an increasing interest to develop new state and parameter estimation schemes to reduce the deficiencies of classical schemes such as the Kalman Filter (KF) and the Luenberger Observer (LO) which have been frequently used to reconstruct variables that are not measured and to reduce the effect of noise on the available measurements. However, due to the fact that the stability and convergence properties of these estimators are essentially locally valid, their application has been restrictive in many practical situations. Other estimation approaches (the high gain [1], adaptive [2], and sliding mode [3]) have been also devised to solve the state reconstruction problem since the stability of the system is guaranteed but their designs involve conditions that must be assumed a priori or that are usually hard to verify [4]. These may account for the failure of these estimators to find widespread application in biological processes [2].

In this paper we present an innovative state estimation schemes to overcome the difficulties associated with the reconstruction of important nonmeasured variables in biological processes. It is based on the well-known Asymptotic Observer (AO) [2], which has proved to be suitable for certain biological processes by yielding satisfactory estimates in the face of uncertain kinetic parameters and load disturbances despite the dependence of the AO performance and convergence on the system operating conditions (particularly on the dilution rate which may be relatively low in most industrial scale biological processes) that have prevented the implementation of efficient monitoring and control strategies.

The objective of this study is then to propose an alternative to tune the convergence rate of a typical AO to compensate the effect of this plant features dependence of asymptotic observers by reducing the close interaction of the plant parameters in the estimator equations. This is accomplished by adopting a methodology similar to that used in [5] for a single-dimension bounded error observer, which is further developed to more complex n-dimensional cases. The main result is the inclusion of an adjustable convergence rate in the design of asymptotic observers while maintaining the stability and robustness convergence properties in the presence of nonlinear terms (i.e., process kinetics) and under the influence of load disturbances. The performance improvement of the classical asymptotic observer is finally demonstrated by applying in simulations the proposed tunable observer in an anaerobic digestion wastewater treatment process.

2. The considered general model

Let us consider the general class of biological systems that fits within the following model [2]:

\[
\begin{align*}
\dot{x}(t) &= Cf(x(t),t) + A(t)x(t) + b(t) \\
x(0) &= x_0
\end{align*}
\]  

(1)

where \( x(t) \in \mathbb{R}^n \) is the state vector, \( C \in \mathbb{R}^{n \times r} \) represents a matrix of constant coefficients. The mapping \( f(x(t),t) \in \mathbb{R}^r \) denotes the nonlinearities and \( b(t) \in \mathbb{R}^n \) gathers the inputs of the process. The time-varying matrix \( A(t) \in \mathbb{R}^{n \times n} \) is the state matrix. The number of measured states that are available on-line is \( n_2 \). Thus, the problem reduces to estimate \( n_1 = n - n_2 \) variables. For this purpose, the state vector is split in such a way that (1) can be rewritten such as

\[
\begin{align*}
\dot{x}_1(t) &= C_1 f(x(t),t) + A_{11}(t)x_1(t) \\
&\quad + A_{12}(t)x_2(t) + b_1(t), \quad x_1(0) = x_{1,0} \\
\dot{x}_2(t) &= C_2 f(x(t),t) + A_{21}(t)x_1(t) \\
&\quad + A_{22}(t)x_2(t) + b_2(t), \quad x_2(0) = x_{2,0}
\end{align*}
\]  

(2)
where the $n_2$ measured states $y(t)$ have been grouped in the $x_2(t)$ vector (i.e., $y(t) = x_2(t)$) while the variables that have to be estimated are represented by $x_1(t)$. $A_{ij}(t) \in \mathbb{R}^{n \times n}$, $C_i \in \mathbb{R}^{n \times n}$, $b_i(t) \in \mathbb{R}^n$, for $i = 1, 2$ and $j = 1, 2$ are the corresponding partitions of $x(t)$, $A(t)$, $C$ and $b(t)$, respectively. The following hypotheses about the model are introduced:

1. **(H1)** The matrix $A(t)$ is known and bounded for all $t \geq 0$, i.e., there exist constant matrices $A_{\min}$ and $A_{\max}$ such that $A_{\min} \leq A(t) \leq A_{\max}$ for all $t \geq 0$.

2. **(H2)** The matrix $C$ is constant and known with the property $\text{rank}(C) = n$.

3. **(H3)** The vector $b(t)$ is known for all $t \geq 0$.

**Note.** The operator $\leq$ is applied between vectors and between matrices should be understood as a collection of inequalities between elements.

### 3. A robust asymptotic observer

Under hypotheses (H1) to (H3), the following system designed by the linear transformation $w(t) = N(t)x(t)$:

$$
\begin{align*}
\dot{w}(t) &= W(t)\dot{v}(t) + Y(t)y(t) + Nb(t) \\
\dot{v}(0) &= N\tilde{x}_0 \\
\tilde{x}_1(t) &= N_1^{-1}(\tilde{v}(t) - N_2y(t))
\end{align*}
$$

with

$$
W(t) = (N_1A_{11}(t) + N_2A_{21}(t))N_2^{-1}$$

$$
Y(t) = N_1A_{12}(t) + N_2A_{22}(t) - W(t)N_2
$$

is an asymptotic nonlinear observer of (1) [6]. Here, $N = [N_1 \quad N_2]$ where $N_1 \in \mathbb{R}^{n \times n_1}$ is an arbitrary invertible matrix, $N_2 = -N_1C_1C_2^{-1}$ ($N_2 \in \mathbb{R}^{n \times p}$) and $C_2$ is the generalized pseudo-inverse of $C_2$. Notice that observer (3) is fully independent of the nonlinear terms and thus, it is robust with respect to these terms. Let us now denote $e_{\text{cao}}(t) = \tilde{x}_1(t) - x_1(t)$ if $\dot{x}_1(0) - x_1(0) \geq 0$ or $e_{\text{cao}}(t) = x_1(t) - \tilde{x}_1(t)$ if $\dot{x}_1(0) - x_1(0) \leq 0$. $e_{\text{cao}}$ is the observation error associated to (3) (the subscripts “cao” denotes “classical asymptotic observer”). It is easy to verify that $e_{\text{cao}}$ follows the dynamics: $\dot{e}_{\text{cao}}(t) = W_e(t)e_{\text{cao}}(t)$ with $W_e(t) = N_2^{-1}W(t)N_1$. Notice also that under hypothesis (H1), it is possible to find two constant matrices $W_e^-$ and $W_e^+$ such that $W_e^- \leq W_e(t) \leq W_e^+ \forall t \geq 0$. Thus, in order to guarantee the stability of (3), the following hypotheses are introduced:

1. **(H4)** $W_{e,i,j}^+ \geq 0$, $\forall i \neq j$.

2. **(H5)** $W_e^-$ and $W_e^+$ are Hurwitz stable.

The hypothesis (H4) simply states that the matrix $W_e^-$ and thus, the matrices $W_e(t)$ and $W_e^+$ are cooperative [7], while the hypothesis (H5) states the stability of these two constant matrices.

**Lemma 1.** Under hypotheses (H1)–(H5) the asymptotic observer (3) is stable and $\tilde{x}_1(t)$ converges asymptotically towards $x_1(t)$ for any set of initial conditions.

The proof of this lemma is given in [8].

### 4. A robust tunable asymptotic observer

This section presents the main results of this study. The most important limitation of observer (3) is indeed that, in most of the cases, its convergence rate is fixed by the operating conditions of the biological system (namely the dilution rate). To face this limitation, a change in the observer design is introduced in the following in order to obtain adjustable convergence rates.

**Proposition.** Let us consider the following modified transformation $z(t) = \tilde{N}(t)x(t)$ with $\tilde{N}(t) = [N_1 \quad \Theta(t)N_2]$ and where $\Theta(t) \in \mathbb{R}^{n \times n_1}$, the gain matrix, is a continuously derivable function matrix with the property:

$$
\lim_{t \to \infty} \Theta(t) = I
$$

Then, under hypotheses (H1) to (H5), the following dynamical system

$$
\begin{align*}
\dot{\tilde{z}}(t) &= (N_1C_1 + \Theta(t)N_2C_2)\tilde{f}(\tilde{x}(t), t) \\
&+ \tilde{W}(t)\tilde{z}(t) + \tilde{Y}(t)y(t) + \tilde{N}(t)b(t) \\
\dot{x}_1(t) &= N_1^{-1}(\tilde{z}(t) - \Theta(t)N_2y(t))
\end{align*}
$$

where

$$
\tilde{W}(t) = (N_1A_{11}(t) + \Theta(t)N_2A_{21}(t))N_1^{-1}
$$

is a robust tunable asymptotic observer.
\[ \ddot{Y}(t) = N_1 A_{12}(t) + \Theta(t) N_2 A_{22}(t) + (\hat{\Theta}(t) + W(t) \Theta(t)) N_2 \]

\[ \ddot{f}(\hat{x}(t), t) \in W' \] is the best possible approximation of the badly known \( f \) mapping is a stable tuning asymptotic observer for model (1).

**Proof** (Convergence and stability). Let \( e(t) = \hat{x}_1(t) - x_1(t) \) be the observation error associated to (6). Under hypotheses (H1) to (H3), it is straightforward to verify that the error dynamics is given by

\[ \dot{e}(t) = E_e(t) e(t) + K(t) \phi(\hat{x}(t), x(t), t) \]

with

\[ E_e(t) = N^{-1}_1 \tilde{W}(t) N_1 = A_{11}(t) - N^{-1}_1 \Theta(t) N_2 A_{21}(t) \]

\[ K(t) = C_1 + N^{-1}_1 \Theta(t) N_2 C_2 \]

\[ \phi(\hat{x}(t), x(t), t) = \dot{f}(\hat{x}(t), t) - f(x(t), t) \]

Now, since \( \lim_{t \to \infty} \theta(t) = I \), it is clear that:

(i) \( \lim_{t \to \infty} E_e(t) = W_e(t) \),
(ii) \( \lim_{t \to \infty} K(t) = C_1 + N^{-1}_1 N_2 C_2 = 0 \), and thus,
(iii) \( \lim_{t \to \infty} \dot{e}(t) = \dot{e}_{cao}(t) \).

Therefore, given the stability properties of \( W_e(t) \) provided by hypotheses (H4) and (H5), it can be concluded that \( \lim_{t \to \infty} e(t) = \lim_{t \to \infty} e_{cao}(t) = 0 \). \( \Box \)

Clearly, the advantage of the tunable observer (6) over the classical AO is that, by choosing a suitable gain matrix \( \Theta(t) \), the classical AO is provided with an adjustable convergence rate, which can be tuned by the user. Notice that \( \Theta(t) \) influences both the stability and the convergence properties (see Eq. (8)) of the tuning observer and it can be properly chosen to accelerate the convergence rate which allows to reach the zero steady state, \( e = 0 \), even if the uncertainty of the nonlinear terms \( f(x(t), t) \) is reasonable high. It is also worth mentioning that, with the exception of the property (5), no other restrictions are imposed on the gain matrix \( \Theta(t) \). Thus, the choice of \( \Theta(t) \), may be, at first glance, a relatively easy task. In other words, \( \Theta(t) \) must be chosen to give the fastest convergence to the true state. Moreover, one can see that, as \( \Theta(t) \to I \), the knowledge of the nonlinearities is no longer required and therefore, the tuning observer design converges to the classical AO with the same robustness, stability and convergence properties of the AO. Furthermore, if \( \Theta(t) \) is chosen as \( \Theta(t) = \text{diag}(\theta(t)) \), with \( \theta(t) \in \mathbb{R}^{n_1} \), a fully decoupled tuning observer is obtained, where the parameters needed to tune each estimated state variable, \( x_{1,i}(t) \) (\( i = 1 \ldots n_1 \)), are exclusively those involved in the function \( \theta_i(t) \). In the following section the proposed tuning observer will be applied to an actual highly nonlinear biological wastewater treatment process.

5. Application to wastewater treatment processes

Anaerobic Digestion (AD) is a series of multi-substrate multi-organism biological processes that take place in the absence of oxygen and by which organic matter (expressed as COD, the Chemical Oxygen Demand) is decomposed and converted into biogas, a mixture of mainly carbon dioxide and methane, microbial biomass and residual organic matter [9]. Several advantages are recognised to AD processes when used in wastewater treatment processes: high capacity to treat slowly degradable substrates at high concentrations, very low sludge production, potentiality for production of valuable intermediate metabolites, low energy requirements and possibility for energy recovery through methane combustion. AD is indeed one of the most promising options for delivery of alternative renewable energy carriers, such as hydrogen, through conversion of methane, direct production of hydrogen, or conversion of by-product streams. However, despite these large interests and few thousands commercial installations refereed worldwide [10], many industries are still reluctant to use AD processes, probably because of the counterpart of their efficiency: they can become unstable under some circumstances. Hence, actual research aims not only to extend the potentialities of anaerobic digestion [11], but also to optimise AD processes and increase their robustness towards disturbances [12]. The design of efficient state estimators clearly goes in these two last directions since instrumentation is usually scarce at industrial scale.

5.1. An anaerobic digestion model

Let us consider the following dynamical model (known as AM1) for continuous anaerobic digestion
process [13]. This model is given in the following matrix form (see Fig. 1) or simply $\xi = Cj(x(t), t) + A(t)\xi(t) + b(t)$ which matches exactly model (1) with $x(t) = \xi(t)$. In (9), the dotted lines indicate the partitions of Eq. (2). In this model, $\xi_1 = X_1$, $\xi_2 = X_2$, $\xi_5 = S_1$, $\xi_6 = S_2$ and $\xi_3 = Z$, $\xi_4 = C_{TI}$ are the concentrations of acidogenic bacteria, methanogenic bacteria, COD, Volatile Fatty Acids (VFA), strong ions and total inorganic carbon, respectively. The superscript “in” indicates the influent concentrations. The variable $P_{CO_2}$ is the CO$_2$ partial pressure whereas $\alpha$ ($0 \leq \alpha \leq 1$) denotes the biomass fraction that is retained by the reactor bed, i.e., $\alpha = 0$ for an ideal fixed-bed reactor and $\alpha = 1$ for an ideal continuous stirred tank reactor (CSTR) whereas $D(t)$ is the dilution rate and it is supposed to be a persisting input, i.e., $\int_{\tau}^{\infty} D(\tau) d\tau > 0$. Moreover, $D(t)$ is a bounded variable since it is conditioned by the minimum flux to the persisting input and the washout condition for the upper bound, i.e., $D_{\text{min}} \leq D(t) \leq D_{\text{max}}$. Last but not least, $\mu_1$ and $\mu_2$ are complex nonlinear mathematical expressions that describe the kinetics of the biochemical reactor. These expressions are given by Eq. (10):

$$\mu_1 = \frac{\mu_{1, \text{max}} S_1}{k_{s, 1} + S_1}$$

$$\mu_2 = \frac{\mu_{2, \text{max}} S_2}{k_{s, 2} + S_2 + (S_2/k_{1, 2})^2}$$

The AM1 model was developed and experimentally validated in a continuous 1 m$^3$ up-flow fixed bed anaerobic digester used for the treatment of industrial wine vinasses [13]. More details about the process design and instrumentation can be found in [14].

5.2. Observer design

The goal in this application example is the estimation of $X_1$, $X_2$, $Z$ and $C_{TI}$ by using readily available $S_1$ and $S_2$ measurements. In order to match the split model (2), the matrix partitions $x_i(t)$, $A_{ij}(t)$, $C_i$ and $b_i(t)$, for $i = 1, 2$ and $j = 1, 2$ have been clearly indicated in (9) by the dotted lines. Without loss of generality, one can choose $N_1 = I$, such that

$$N_2 = (k_1 k_3)^{-1} \begin{bmatrix} k_1 & k_2 & 0 & k_3 k_4 + k_2 k_5 \\ 0 & k_1 & 0 & k_1 k_5 \end{bmatrix}^T$$

Matrices $W$, $\tilde{W}$, $Y$ and $\tilde{Y}$ are calculated by using Eqs. (4) and (7) and the gain matrix $\Theta(t)$, can be computed by solving the following ODE system:

$$\dot{\Theta} = -G\Theta + g$$

with $G = \text{diag}(g)$, $g \in \mathbb{R}^{n_1}$. Notice that the necessary property (5) is not restrictive at all and thus, one can choose many forms on $G$ that can fulfill it. In the present study, it is obvious that (11) not only fulfills this property but also it is very simple and allows the decoupling of the observer design. In fact, the selection of the constants, $g_i$, $\forall i = 1, 2, \ldots, n_1$, allows us to tune the convergence rate for each estimated state individually. In addition, in this way, it is possible to influence the fast convergence of $\Theta(t)$ to the identity matrix. Notice however that, as long as $\Theta(t)$ does not reach the identity matrix, the proposed tunable observer exhibits a highly nonlinear behavior and thus, a stability analysis similar to the one used in classical approaches, e.g., the extended LO and the extended KF, should be implemented. It is worth mentioning
that the observer gains used here in the implementation of the tunable observer were chosen after a trial and error process. In fact, a number of different gain matrices \( \Theta(t) \) were tested and they all yielded similar results. These results are not shown in this paper due to space limitation. For the results shown here, we used the following parameters in the solution of Eq. (11):

\[
\Theta(0) = [-2.5 \ 0 \ -14 \ 2 \ -10]^T, \quad g = [1 \ 2 \ 1 \ 0.35]^T.
\]

A methodology to decide upon the optimal choice of the observer gains is now in progress.

5.3. Hypotheses verification

(H1) The matrix \( A(t) \) is bounded and known \( \forall t \geq 0 \) since it depends on \( D(t) \) which is measured and it is also bounded. Moreover, \( \alpha \) and \( k_7 \) are bounded and known.

(H2) By inspection, \( \text{rank} \ C = \text{rank} \ C_2 \).

(H3) All inputs to the system are known.

(H4) Since \( A_{21} = 0 \) and provided \( N_1 = I \), we have

\[
W_e^\pm = \begin{bmatrix}
-\alpha D^\pm & 0 & 0 & 0 \\
0 & -\alpha D^\pm & 0 & 0 \\
0 & 0 & -D^\pm & 0 \\
0 & 0 & k_7 & -(D^\pm + k_7)
\end{bmatrix}
\]

(12)

that fulfills the positivity condition on the off-diagonal elements of \( W_e \).

(H5) From (12) it is clear that \( \text{eig}(W_e^\pm) \) are negative for any \( 0 < D^- \leq D(t) \leq D^+ \) (clearly, \( W_e^- \) and \( W_e^+ \) are Hurwitz).

5.4. Simulation results

Model parameters used in the proposed adjustable rate observer implementation are listed in Table 1.

Simulations shown hereafter were performed for a 50 days period by using operating conditions as close as possible to actual wastewater treatments plants. The dilution rate exhibited large fluctuations as well as drastic step perturbations (see Fig. 2). The behavior of the inlet concentration patterns for \( S_{11} \), \( S_{12} \), \( Z_{1} \), and \( C_{12} \) is shown in Figs. 3–6 while the \( P_{\text{CO}_2} \) is depicted in Fig. 9. As in many continuous bioreactors, \( X_{11} \) and \( X_{22} \) were considered as negligible. The on-line measurements of \( S_1 \) and \( S_2 \) used in the state estimation process

Table 1

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \mu_{\text{max},1} )</td>
<td>1.25 day(^{-1} )</td>
</tr>
<tr>
<td>( \mu_{\text{max},2} )</td>
<td>0.69 day(^{-1} )</td>
</tr>
<tr>
<td>( k_{s,1} )</td>
<td>4.95 Kg COD/m(^3 )</td>
</tr>
<tr>
<td>( k_{s,2} )</td>
<td>9.28 mol VFA/m(^3 )</td>
</tr>
<tr>
<td>( k_{f,2} )</td>
<td>20 (mol VFA/m(^3 ) ( )^{1/2} )</td>
</tr>
<tr>
<td>( \alpha )</td>
<td>0.5 (dimensionless)</td>
</tr>
<tr>
<td>( k_1 )</td>
<td>6.6 Kg COD/Kg x_1</td>
</tr>
<tr>
<td>( k_2 )</td>
<td>7.8 mol VFA/Kg x_1</td>
</tr>
<tr>
<td>( k_3 )</td>
<td>611.2 mol VFA/Kg x_2</td>
</tr>
<tr>
<td>( k_4 )</td>
<td>7.8 mol CO_2/Kg x_1</td>
</tr>
<tr>
<td>( k_5 )</td>
<td>977.6 mol CO_2/Kg x_2</td>
</tr>
<tr>
<td>( k_6 )</td>
<td>1139.2 mol CH_4/Kg x_2</td>
</tr>
<tr>
<td>( k_7 )</td>
<td>50 day(^{-1} )</td>
</tr>
<tr>
<td>( K_8 )</td>
<td>0.1579 mol/m(^3 ) KPa</td>
</tr>
</tbody>
</table>

Fig. 2. Dilution rate.

Fig. 3. Influent COD concentration.
Fig. 4. Influent VFA concentration.

Fig. 5. Influent strong ions concentration.

Fig. 6. Influent total inorganic carbon concentration.

Fig. 7. COD concentration.

Fig. 8. VFA concentration.

Fig. 9. CO₂ partial pressure profile.
were obtained from model simulations as the observer inputs to estimate $X_1, X_2, C_{TI}$ and $Z$ (see Figs. 7 and 8). The performance of the proposed adjustable nonlinear observer under these operating conditions is depicted in Figs. 10–13. For the sake of completeness, the response of a classical asymptotic observer has been added to demonstrate the convergence features of the proposed observer design. Initial conditions for both, classical asymptotic observer and the tunable observer were exactly the same. In Figs. 10–13, the continuous line (−) represents the model predictions, the dotted line (···) represents the CAO estimations whereas the dashed line (---) represents the tuning observer estimations. By inspecting these figures, it is clear that the response of the tunable observer is satisfactory for all estimated state variables since it was able to cope with all the difficulties associated to load disturbances. As expected, the tunable observer converge rate is faster than the classical one, showing excellent stability properties even in the presence of load disturbances and uncertainty on the process kinetics. Notice, however, that in the case of the $Z$ variable, both observers showed essentially the same convergence rate (see Fig. 11) since $Z$ does not depend on the nonlinearities nor on any model parameter (see $\xi_3$ in Eq. (9)) and as a consequence, the convergence rate of both observers schemes rely exclusively on the fixed gain value predetermined by the dilution rate. The tunable observer response described, nevertheless, the trend of the actual $Z$ readings. Finally, the
excellent performance of the proposed observer in the estimation of $C_{TI}$ is exhibited in Fig. 13. One can see that the tunable observer response is able to reach the true state value faster than the classical AO.

6. Conclusions and perspectives

In this work, a robust asymptotic adjustable rate nonlinear observer for multidimensional biological systems has been proposed. It has been tested in numerical simulations on an anaerobic digestion process used in a wastewater treatment context. By using observer gains that were suitably chosen, this observer exhibited faster convergence rates than a classical asymptotic observer design. New studies are currently being conducted for optimizing the observer gains calculations. Because of the clear utility of this tuning observer in highly uncertain biological systems at the experimental scale, their use in robust nonlinear control schemes with application to continuous bioreactors is now under study.

Acknowledgements

The authors gratefully acknowledge to the ECOS-ANUIES Program (project: M97-B01), the CONACYT, the PROMEP Program and the European project TELEMAC (IST-2000-28156) for the support that made this study possible.

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