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## Bistable electron magnetic resonance in solids

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#### Abstract

This paper describes the phenomenon of Bistable Electron Magnetic Resonance, which manifests itself by a resonance line with a distorted shark fin-like shape. This effect requires only a fluctuating hyperfine interaction between electron spins and nuclear spins. It is demonstrated for shallow donors in semiconductors and conduction electrons in light metals. Bistability is an intrinsic property of electron magnetic resonance when the shift of the resonance by the nuclear polarization is larger than the EPR linewidth. *To cite this article: D. Gourier et al., C. R. Chimie 7 (2004).* © 2004 Académie des sciences. Published by Elsevier SAS. All rights reserved.

#### Résumé

Cet article décrit le phénomène de résonance magnétique électronique bistable, qui se traduit par une raie de résonance distordue en forme d'aileron de requin. L'obtention de cet effet nécessite seulement une interaction hyperfine en régime de fluctuation rapide. Un tel effet est démontré pour des donneurs diffus dans les semiconducteurs et pour les électrons de conduction dans les métaux légers. La bistabilité est une propriété intrinsèque de la résonance électronique quand le déplacement de la raie de résonance par la polarisation nucléaire est plus grand que la largeur de raie. *Pour citer cet article : D. Gourier et al., C. R. Chimie 7 (2004).* 

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#### 1. Introduction

Important devices in computing, signal processing and communication technologies are based on bistable systems used as switches, memory elements and logic gates. Generally speaking, a system is bistable if it

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exhibits two stable output responses R for a single perturbation or input signal P, and shows a hysteresis loop in the curve R = f(P). Thus a bistable system reveals a different response for upward and downward sweeps of the input signal.

Two ingredients are required to generate a bistable phenomenon: (*i*) a *feedback loop* and (*ii*) a *non-linear effect*. In the particular case of optical bistability, – i.e.

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the bistability of the interaction of light with matter – the first experimental example of bistable set-up is a non-linear medium placed in a Fabry–Perot cavity [1]. It is important to note that the bistability is macroscopic in this kind of system, whereby the nonlinearity is brought by the optical material and the feedback is produced by the cavity mirrors.

In the forthcoming decades, advances in nanosciences and nanotechnology promise to have major implications in materials devices and systems. For this reason, macroscopic properties such as optical bistability have to be scaled down to the nanometre level, in the domain of individual atoms, molecules or clusters. Recently, intrinsic (or mirrorless) optical bistability (IOB) of the emission from Yb<sup>3+</sup> ion pairs have been observed in an ytterbium doped solid matrix [2]. However, the origin of this bistability remains puzzling, and different mechanisms are still debated.

For this reason, it is tempting to investigate the equivalent of IOB in magnetic resonance, reminding that concepts invented for nuclear magnetic resonance have often been a source of inspiration in optics community [3]. In the last decade, we showed that Electron Magnetic Resonance in solids is an intrinsically bistable phenomenon when several conditions are satisfied [4]. This effect is hereafter referred to as Bistable Electron Magnetic Resonance (BEMR). In this case, the non-linear effect is the saturation of the resonance, and the intrinsic feedback loop is provided by the nuclear spins via the Overhauser effect [5]. The detailed understanding of the mechanism of bistability allowed us to predict and observe BEMR in several systems, such as InP [6], metallic lithium colloids [7,8], gallium oxide [4], and to explain the origin of hysteresis observed in the EPR of GaAs-GaAlAs heterostructures [9]. It is important to realize that this elementary two-component elementary bistable system, composed of saturable absorbers (the electron spins) and intrinsic feedback elements (the nuclear polarization via the Overhauser effect) can in principle be extrapolated to UV-visible IOB with other types of two-component systems, such as atom pairs for example. In this case, the saturable absorber is the atom probed by the electromagnetic field, and the feedback system is the polarization induced on the second atom by the saturated absorption [10]. In this paper, we restrict IOB to BEMR, its magnetic equivalent.



Fig. 1. (a) Graphical representation of the response R of the system described by Eqs. (1) and (2). Case (*i*) corresponds to a monostable situation, while case (*ii*) corresponds to a bistable situation. (b) Shape of a transition induced in a two-state quantum system in monostable (case (*i*)) and bistable (case (*ii*)) situations. In the latter case, the transition exhibits a 'shark-fin' shape.

#### 2. The 'shark-fin' effect

The transition between two quantum states induced by an electromagnetic field, the basic event in spectroscopy, exhibits a symmetrical lineshape. Experimentally, the spectrum remains always unchanged upon upward and downward sweeps of the angular frequency  $\omega$  of the electromagnetic field (or the magnetic field amplitude  $B_0$  at fixed frequency  $\omega$  in the case of EPR). This usual situation is illustrated by the dotted line in Fig. 1b. However, it can be easily imagined that if the theoretical lineshape is bent in such a way that it describes a 'shark-fin' shape, the experimental spectrum becomes dependent on the field sweep direction, with a hysteresis width delimited by abrupt transitions at critical frequencies  $\omega^{\uparrow}$  and  $\omega^{\downarrow}$  (or magnetic field values  $B\uparrow$  and  $B\downarrow$  in EPR). This bistability window is characterized by a well-defined field range where the quantum system does not absorb the radiation for the increasing field sweep mode (the  $\alpha$ -branch), while it strongly absorbs this radiation for the reverse field sweep mode (the  $\gamma$ -branch). In this case, a portion of the spectrum (the  $\beta$ -branch) cannot be recorded, and is

lost experimentally (full line in Fig. 1b). It should be emphasized that this bistability in a two-state quantum system implies a memory of the field during the transition, since the response for given values of the control parameter (the frequency, or the magnetic field, etc.) depends on previous values of these parameters.

We have recently shown [10] that this 'shark fin' effect in a spectroscopic transition occurs if the quantum system is composed of two subsystems L and K, linked by a weak interaction V which fluctuates with a correlation time  $\tau_c \ll \hbar/V$ , the well-known 'narrowing condition' in magnetic resonance. The two subsystems retain the memory of their mutual interaction during  $\tau_{c}$ . The consequence is that correlations between L and K vanish after a time  $t \ge \tau_c$ , which means that we may clearly distinguish the subsystem L probed by the electromagnetic field and the subsystem K responsible for the feedback loop. When the narrowing condition  $\tau_{c} \ll \hbar/V$  is fulfilled, the steady-state response *R* (for example the absorption) of the LK system versus the angular frequency  $\omega$  can be written with two coupled equations of the type [10]:

$$R = \frac{a}{1 + b \left(c - \omega\right)^2 + a} \tag{1}$$

$$R = (d - \omega) \frac{1}{e}$$
<sup>(2)</sup>

where coefficients *a* to *e* are functions of the control parameters, such as the temperature, the power of the incident radiation, and of material-dependent parameters such as the relaxation times of the L and K subsystems, and the frequency of the probed subsystem L. All these parameters are discussed in part 3 of this paper, where Eqs. (1) and (2) are represented by Eqs. (4) and (7), respectively. Equations (1) and (2) correspond to the *non-linear process* and the *feedback loop*, respectively. Combining (1) and (2) shows that *R* is a function of itself, -i.e. R = f(R) -, and bistability occurs if *R* exhibits three values (two stable and one unstable) for one set of control parameters.

A renormalization of the resonance frequency is necessary to get a bistable 'shark-fin' shape. By renormalization, it is meant that the resonance frequency has to change continuously during the interaction with the electromagnetic field. This renormalization is included in Eq. (2), which directly comes from the condition  $\tau_c \ll \hbar/V$  [10]. Fig. 1a shows a graphical representation of the coupled Equations (1) and (2). The system is monostable (no memory) when the straight line (Eq. (2)) and the bell-shaped curve (Eq. (1)) have only one crossing point (case (i)). In this case, the resulting monostable lineshape, corresponding to the ensemble of crossing points versus  $\omega$ , is represented by the dotted curve in Fig. 1b. The system is bistable when Eqs. (1) and (2) exhibit three crossing points  $\alpha$ ,  $\beta$  and  $\gamma$ (case (ii) in Fig. 1a). In this case, the response of the system, represented by the set of crossing points versus  $\omega$ , exhibits the expected 'shark-fin' shape for bistability (full lines in Fig. 1b). Whether the response R is bistable or not depends only on the set of parameters *a*–*e* in Eqs. (1) and (2).

# **3.** The mechanism of bistability in Electron Magnetic Resonance

We pointed out that a bistable shark-fin-like resonance might exist if two conditions are fulfilled: a non-linearity in the radiation-matter interaction, and a feedback mechanism. A collection of electrons in a magnetic field  $B_0$ , characterized by a spin S = 1/2 interacting with neighbouring nuclear spins I via an hyperfine interaction A is the most elementary pair system that can exhibit a bistable interaction with a microwave electromagnetic field [4]. In this case, the non-linearity is the saturation of the resonance. It is well known that an electron spin resonance transition at energy  $\hbar \omega = g \beta B_0$  is saturable at moderate value of the microwave field  $B_1$  if spin-orbit coupling effects are small, -i.e. if the g-factor is close to the free spin value  $g_{\rm e} = 2.0023$ . We thus consider the saturation factor s, defined as follows [11]:

$$s = \frac{\left\langle S_z^0 \right\rangle - \left\langle S_z \right\rangle}{\left\langle S_z^0 \right\rangle} \tag{3}$$

where  $\langle S_z^0 \rangle = -g \beta B_0/4 k T$  and  $\langle S_z \rangle$  are the electron spin polarizations at thermal equilibrium (in the high temperature limit) and under microwave irradiation, respectively. Thus Eq. (3) gives s = 0 at thermal equilibrium and s = 1 for complete saturation. The equivalent of Eq. (1) in magnetic resonance is written



Fig. 2. Decomposition of the mechanism of BEMR into four elementary steps, for a system composed of electron spins interacting with nuclear spins via a hyperfine interaction *A*.

as follows for an electron spin system [4] (step 1 in Fig. 2):

$$s = \frac{\gamma^2 T_1 T_2 B_1^2}{1 + \gamma^2 T_1 T_2 B_1^2 + \gamma^2 T_2^2 (B_{\text{eff}} - \hbar\omega/g \beta)^2}$$
(4)

where  $T_1$  and  $T_2$  are the usual longitudinal and transverse relaxation times for electron spins,  $B_{\text{eff}}$  is the effective magnetic field seen by the electrons, and  $\gamma = g \beta/\hbar$  is the electron gyromagnetic ratio. The main effect of saturation is the transfer of electron polarization to nuclear spins via the hyperfine interaction, with the consequence that the nuclear polarization deviates from the thermal equilibrium polarization  $\langle I_z^0 \rangle$  (step 2 in Fig. 2):

$$\left\langle I_{z}\right\rangle = -\frac{4}{3}I\left(I+1\right)\left\langle S_{z}^{0}\right\rangle$$
 fs (5)

where the leakage factor  $0 \le f \le 1$  is defined below.

The *feedback* loop of BEMR is due to this polarization transfer, and must operate in such a way that it produces a renormalization of the resonance [10], – i.e. a shift of the resonance field (or frequency) during the interaction with the microwave radiation. This renormalization is possible only if the correlation time  $\tau_c$  of the unpaired electron at the nuclear position is much shorter than  $\hbar/A$  [10]. For most paramagnetic defects in solids (impurities, point defects...),  $\tau_c$  is generally characterized by  $\tau_c > \hbar/A$ , so that the hyperfine interaction is resolved in the EPR spectrum, or contributes to the inhomogeneous broadening of the resonance line. Renormalization is thus not possible for localized electrons and large hyperfine coupling, and we do not expect bistability to occur in this case.

If the electron spin density is distributed over many nuclei, which occurs for shallow donors in semiconductors or for electrons delocalised in conduction band of solids, the hyperfine interaction A with each nuclear spin becomes small and  $\hbar/A$  is large. If, on the other hand, the spin density diffuses either by electron motion or by exchange interaction between electron spins, the correlation time  $\tau_c$  of the unpaired electron at a nuclear site is considerably shortened ( $\tau_c < 10^{-13}$ s for exchange interaction in the meV range) and the condition  $\tau_c \ll \hbar/A$  prevails even for large hyperfine coupling A. The EPR line is exchanged (or motionally) narrowed with no remaining traces of the hyperfine splitting. It is important to note that in this case the electron resonance position is shifted by an effective nuclear field  $B_n = NA\langle I_z^0 \rangle / g \beta$ , where N is the number of nuclei interacting with the electron spin, and the thermal equilibrium nuclear polarization is given by:

$$\left\langle I_{z}^{0} \right\rangle = \frac{g_{n} \beta_{n} I (I+1) B_{0}}{3 k T}$$
 (6)

This nuclear field shifts the EPR resonance line to low field, and thus play the role of the feedback system as it modifies the saturation factor (4) via the effective field  $B_{\text{eff}} = B_0 + B_n$  seen by electron spins.

We have now to determine the equivalent of Eq. (2) for the feedback,  $s = f(B_{eff})$  and obtain the equation s = f(s) of bistability by combining this equation with Eq. (4). In the case of exchange or motional narrowing regime, the dynamic nuclear polarization occurs via the Overhauser effect. The decrease of the electron spin polarization  $\langle S_z \rangle$  induced by saturation is transferred to  $\langle I_z \rangle$  via the 'flip-flop' relaxation mechanism  $\Delta(m_s + m_I) = 0$  with a characteristic time  $T_x$ . This enhancement of the nuclear field  $B_n$  upon saturation is at the origin of the following feedback equation of bistability [4] (step 3 in Fig. 2):

$$s = \frac{B_{\rm eff} - B_0}{\left(\Delta B_{\rm ov}\right)_{\rm max}} \tag{7}$$

with

$$\left(\Delta B_{\rm ov}\right)_{\rm max} = \frac{I(l+1) NA f B_0}{3 k T} \tag{8}$$

being the largest possible value of the nuclear field enhancement, which is obtained for complete saturation. The parameter f is the leakage factor, which reflects the efficiency of the flip-flop relaxation mechanism upon competition with other relaxation mechanisms. The leakage factor is given by [12]:

$$f = \frac{1/T_x}{1/T_x + 1/T_x}$$
(9)

where  $T_n$  represents all the other nuclear relaxation times. The optimal situation corresponds to  $f \approx 1$ , which is favoured when the hyperfine interaction A is of purely Fermi-type:

$$A = (8 \pi/3) h^{-1} g \beta g_n \beta_n |\Psi_0|^2$$
(10)

where  $|\Psi_0|^2$  is the electron spin density at each of the *N* nuclear spins.

As pointed out in the preceding part, bistability is expected when the line described by Eq. (7) has three crossing points with the curve of Eq. (4). This is equivalent to say that that the following equation s = f(s), obtained by combining Eqs. (4) and (7), representing step 4 in Fig. 2:

$$s = \frac{\gamma^2 T_1 T_2 B_1^2}{1 + \gamma^2 T_1 T_2 B_1^2 + \gamma^2 T_2^2 [B_0 + s(\Delta B_{ov})_{max} - \hbar \omega / g \beta]^2}$$
(11)

exhibits three different values of the saturation factor *s* for fixed values of the external field  $B_0$  and other parameters. Under these conditions, the EPR line exhibits the 'shark-fin' shape of Fig. 1b, where  $\omega$  must be replaced by the external magnetic field  $B_0$  (experimental situation for CW EPR). The EPR signal being detected by modulation of the magnetic field  $B_0$ , the intensity  $I_{\text{EPR}}$  of the BEMR signal is proportional to the first derivative of the absorption, which gives [4]:

$$I_{EPR} = -I_0 \frac{B_1(B_0 + B_n - \hbar\omega/g\beta)}{\left[1 + \gamma^2 T_2^2 (B_0 + B_n - \hbar\omega/g\beta)^2 + \gamma^2 T_1 T_2 B_1^2\right]^2}$$
(12)

where the constant  $I_0$  depends on temperature, instrumental parameters,  $T_2$ , g-factor and unpaired spin concentration. Fig. 3 shows an example of BEMR in the case of  $\beta$ -Ga<sub>2</sub>O<sub>3</sub>. Part **a** of this figure shows the Overhauser shift of the resonance field upon saturation of the EPR line, the spectra being recorded upon decreasing the magnetic field  $B_0$ . Part **b** of Fig. 3 shows the theoretical BEMR absorption for an incident microwave power P = 63 mW, simulated with



Fig. 3. (a) EPR spectra of a  $\beta$ -Ga<sub>2</sub>O<sub>3</sub> single crystal at 150 K, showing the renormalization of the resonance by the Overhauser effect, resulting from the narrowing condition  $\tau_c \ll \hbar/A$ . The spectra are recorded upon decreasing the magnetic field  $B_0$ . (b) Selected BEMR spectrum at P = 63 mW. The simulation of the absorption and the first derivative of the absorption have been obtained with  $T_1 = T_2 = 1.4 \times 10^{-7}$  s,  $(\Delta B_{ov})_{max} = 0.47$  mT and  $\hbar \omega/g \beta = 343.51$  mT.

 $T_1 = T_2 = 1.4 \times 10^{-7}$  s, and the first derivative of the BEMR absorption (Eq. (12)). The microwave power is related to the microwave field  $B_1$  of Eq. (12) by  $P = K B_1^2$ , with  $K = 6.1 \times 10^4$  mW mT<sup>-2</sup> for our EPR cavity. Comparison with the experimental BEMR spectrum recorded upon sweeping up and down the field  $B_0$  shows a very good agreement with theory. The bistable memory effect appears clearly in this figure, as the electron spins do not absorb the microwave radiation upon sweeping up  $B_0$  in the range 343.25–343.4 mT, while they absorb the radiation upon sweeping down  $B_0$  in the same range.

#### 4. Conditions for bistability

It should be emphasized that, in most cases, the EPR of shallow donors or conduction electrons in solids does not exhibit a bistable behaviour, although they correspond to the optimal condition of BEMR, as discussed in part 3. The reason is due to the fact that in most cases, Eqs. (4) and (7) have only one crossing point in all the magnetic field range. This implies that the values of the parameters  $B_1, T_1, T_2$  and  $(\Delta B_{ov})_{max}$  in Eqs. (11) and (12) are such that the nuclear field  $B_n$  has only one value for each value of the external field  $B_0$ . However, the analysis of BEMR in terms of nonlinearity (saturable absorption, Eq. (4)) and feedback effect (Eq. (7)) allows us to predict the characteristics of compounds (chemical composition, electronic structure...) and the experimental conditions (temperature, magnetic field, microwave intensity) to obtain the 'shark fin' shape of BEMR. Equations (4) and (7) exhibit three crossing points in a given range of  $B_0$ , the condition for bistability, when the slope of Eq. (7) is smaller than the tangent at the inflection point of the curve of Eq. (4). This condition gives [13]:

$$\frac{I(I+1) NAf}{3 k T} B_0 > \frac{8}{3\sqrt{3}} \frac{(1+\gamma^2 T_1 T_2 B_1^2)^{3/2}}{\gamma^3 T_1 T_2^2 B_1^2}$$
(13)

This inequality is controlled by two kinds of parameters: (*i*) external parameters represented by the temperature *T* and the microwave field  $B_1$ , and (*ii*) material parameters represented by the electron relaxation times  $T_1/T_2$ , the nuclear spin *I*, the number *N* of nuclear spins interacting with each electron (the extension of the electronic wave function), the scalar hyperfine interaction *A* with each nucleus and the leakage factor *f*. In the case of a pure scalar (Fermi-type) hyperfine interaction, an estimation of *NA* in (13) is given by  $A_0$ , the hyperfine interaction for a single ion or atom in a <sup>2</sup>S spectroscopic state, – i.e. a single electron in a s-atomic orbital. We thus expect  $NA f \le A_0$ . As  $B_1$  is a control parameter, the right-hand member of Eq. (13) can be minimized with respect to  $B_1$ , which gives:

$$\gamma T_2 \frac{I(I+1) NAfB_0}{3 kT} > 4$$
 (14)

This critical inequality expresses the condition for the existence of at least one value of the microwave field  $B_1$  for which BEMR can be observed. By using Eq. (8) and the expression  $\Delta B_{pp} = 2/(\sqrt{3} \gamma T_2)$  of the peak-to-peak linewidth of the unsaturated line, this inequality can be simplified into a more general form for the existence of bistability:

$$\left(\Delta B_{\rm ov}\right)_{\rm max} > 2\sqrt{3}\,\Delta B_{\rm pp} \tag{15}$$

which means that bistability will occur if the maximum Overhauser shift  $(\Delta B_{ov})_{max}$  of the resonance line is larger than 3.5 times the linewidth.

The bistability condition (14) contains all the structural information concerning potential candidates for BEMR. The most favourable compounds should be characterized by long  $T_2$ , high nuclear spin, strong hyperfine interaction and a leakage factor close to one. Transverse relaxation time  $T_2$  is related to both the electronic structure of the conduction band edge and structural defects (impurities, intrinsic defects...). In the situation of extreme narrowing regime, imposed by the condition  $\tau_c \ll \hbar/A$ , the electron relaxation times of electrons in (or close to) the conduction band edge are given by [14]:

$$T_1 = T_2 \approx a \left(\frac{t_{\mathscr{I}}}{t_{\perp}}\right)^2 \frac{\tau}{\left(\Delta g\right)^2}$$
(16)

where a is a constant of the order of unity. Parameters  $t_{ll}$  and  $t_{\perp}$  are the transfer integrals parallel and perpendicular, respectively, to the preferred direction of the electronic structure. Thus, for conductors with very anisotropic band structure, with  $t_{ll}/t_1 \ge 1$ , the relaxation times are generally enhanced as compared to isotropic conductors  $(t_{//}/t_{\perp}=1)$ . The effect of Time  $T_2$ on the BEMR spectrum is shown in Fig. 4, which demonstrates that a moderate decrease of  $T_2$  is able to suppress bistability by transforming the 'shark-fin' shape into a distorted Lorentzian shape. The other parameters in Eq. (16) are the g-shift  $\Delta g$  and the characteristic time  $\tau$  of conductivity. Long  $T_2$  is favoured for small g-shift, which occurs if the conduction band edge is made of s atomic orbitals, preferably of light elements.

The other important factor for bistability in condition (14) is the term I(I + 1) NA f, which determines the intensity of the nuclear polarization at a given temperature and external magnetic field. For a solid containing one type of nuclear spins, this term is written as [15]:

$$I(I+1) NA f \approx I(I+1) A_0 |C_s|^2 f$$
 (17)

where  $C_{\rm s}$  is the coefficient of s-orbitals in crystal orbitals of the conduction band edge. The hyperfine



Fig. 4. Influence of the electron relaxation time  $T_2$  on the BEMR shape. Parameters of the calculation: I (I + 1) N A f = 13650 MHz (corresponding to gallium nuclei), T = 150 K,  $B_1 = 6 \times 10^{-2}$  mT, and  $T_1 = T_2$ .

interactions for <sup>2</sup>S atoms or ions are known from literature data. It thus appears that the most favourable situation for BEMR is an anisotropic conductor (long  $T_2$ ) with a conduction band edge made of s-orbitals (long  $T_2, f \approx 1, C_s \approx 1$ ) of elements characterized by large hyperfine coupling  $A_0$ . For example, we expect  $I(I+1) A_0$  values larger than 10<sup>5</sup> MHz for conduction band edge made of s-orbitals of indium and thalium, and between 10<sup>4</sup> and 10<sup>5</sup> MHz for gallium and caesium [15]. Lithium should only give a value of about  $10^3$ MHz, which is compensated by a long  $T_2$  because of the very small spin orbit coupling [7]. Therefore BEMR results from a compromise between favourable material characteristics (long  $T_2$ , high nuclear spin I, high  $A_0$ ...) and external conditions (*T*,  $B_0$ ). For very favourable material conditions, we expect bistability in soft experimental conditions - i.e. close to room temperature and low magnetic field. However, condition (14) shows that in principle all materials should exhibit bistability, if the temperature is sufficiently low and the magnetic field  $B_0$  sufficiently high to satisfy the bistability condition. This critical inequality indicates that bistability is a general property of the EPR of conducting materials possessing non-zero nuclear spins.

The particularly favourable characteristics of  $\beta$ -Ga<sub>2</sub>O<sub>3</sub>, namely shallow donors in exchange interaction, gallium nuclei with *I* = 3/2, strongly anisotropic band structure, conduction band edge made of 4s gal-



Fig. 5. Theoretical EPR spectrum for submicronic metallic lithium particles. Parameters of the calculation: T = 4 K;  $T_1 = T_2 = 0.5 \times 10^{-6}$  s; I (I + 1) N A f = 200 MHz.

lium orbitals, explain why this compound exhibits BEMR up to room temperature [15]. However, from known values of  $T_2$  and hyperfine coupling for the semiconductor InP and for metallic lithium particles embedded in insulating matrices, we expect BEMR at liquid helium temperature and X-band frequency with these compounds. For example, Fig. 5 shows the calculated EPR spectrum of submicronic metallic particles at different microwave power values. Fig. 6 shows the experimental spectrum of lithium particles produced by UV irradiation of LiH powder [8]. The spectrum is simulated by summing the contributions of two types of lithium, one with a long  $T_2$  (population A,  $T_2 = 4.8 \times 10^{-6}$  s) and the other with a shorter  $T_2$ (population B,  $T_2 = 9 \times 10^{-7}$  s). The BEMR spectrum of shallow donors in InP single crystal at 3 K is shown in Fig. 7, where it is compared with the spectrum predicted by considering only parameters known in the literature [6].

# 5. Analogy with other types of bistability: the dynamic potential

Bistable systems in physics, chemistry and biology are often described by a potential U = f(Q) where Q is a



Fig. 6. Experimental and calculated BEMR spectra for submicronic lithium particles at 4 K produced by UV irradiation of LiH powder. Parameters of the calculation : P = 25 mW. Two populations of particles are considered. Population A:  $T_1 = T_2 = 5 \times 10^{-6}$  s; I(I + 1) NAf = 110 MHz. Population B:  $T_1 = T_2 = 9 \times 10^{-7}$  s; I(I + 1) NAf = 140 MHz.



Fig. 7. Experimental and calculated BEMR spectra for InP at 3 K. Parameters of the calculation: P = 5 mW ( $B_1 = 10^{-2}$  mT),  $T_1 = T_2 = 4 \times 10^{-8}$  s, I(I + 1) NAf = 168 430 MHz. The unsaturated spectrum (P=0.1 mW,  $B_1 = 1.6 \times 10^{-3}$  mT) is shown on the top of the figure.

configuration (or reaction) coordinate, as shown in Fig. 8 [16]. The minima  $U_{\alpha}$  and  $U_{\gamma}$  represent the stable steady states, while the local maximum  $U_{\beta}$  is the unstable steady state. The shape of the potential is determined by the control parameters, so that the hysteresis cycle across a bistable resonance (Fig. 1b) can be



Fig. 8. Representation of the dynamic potential U versus configuration coordinate Q, for four selected situations of the bistable transition of Fig. 1b (case *ii*).

described as follows in the potential representation, in terms of the overdamped motion of a fictitious particle in the Q space. Starting from the low frequency  $\omega$  (or low-field  $B_0$ ) and sweeping up to  $\omega \le \omega \downarrow$ , the potential is monostable (Fig. 8a). For  $\omega \downarrow < \omega < \omega \uparrow$ , the branch  $\alpha$ of the spectrum of Fig. 1b is recorded, which corresponds to the bistable potential of Fig. 8b, with the system trapped in the  $\alpha$ -state. For  $\omega = \omega \uparrow$ , the spectrum exhibits an abrupt increase of intensity (Fig. 1b), which corresponds to a vanishing potential barrier in Fig. 8c, with the system making a transition to the  $\gamma$ -state. The system becomes monostable for  $\omega > \omega^{\uparrow}$ ( $\gamma$ -state only). For a decreasing variation of  $\omega$ , and starting from  $\omega > \omega^{\uparrow}$ , the spectrum of Fig. 1b follows the  $\gamma$ -branch up to  $\omega > \omega \downarrow$ , which again corresponds to the potential of Fig. 8b, but the system is now trapped in the  $\gamma$ -state. The abrupt variation of intensity at  $\omega = \omega \downarrow$  in Fig. 1b corresponds to the potential of Fig. 8d, with a vanishing potential barrier and a transition to the stable  $\alpha$ -state.

In order to get a more familiar picture of BEMR in terms of overdamped motion in the potential U = f(Q), let us consider the rate equation for the dynamic nuclear polarization [17]:

$$\frac{\partial B_n}{\partial t} = \frac{1}{T_x} \left[ -B_n + (\Delta B_{\rm ov})_{\rm max} \frac{\gamma^2 T_1 T_2 B_1^2}{1 + \gamma^2 T_1 T_2 B_1^2 + \gamma^2 T_2^2 (B_0 + B_n - \hbar \omega/g \beta)^2} \right]$$

This equation describes the time evolution of the nuclear field  $B_n$ . The steady-state nuclear field, corresponding to  $\partial B_n/\partial t = 0$  in Eq. (18), is reached after a period in the order of magnitude of the electronnuclear (flip-flop) relaxation time  $T_x$ , which amounts to 0.1 to 0.5 s in  $\beta$ -Ga<sub>2</sub>O<sub>3</sub> at 150 K [17] and 140 s in InP at 3 K [6]. Equation (18) being autonomous and a continuous function of a single variable  $(B_n)$ , it is similar to the equation of overdamped motion of a fictitious particle in the magnetic field space, for which we may associate the potential *U*, defined as follows:

$$\frac{\partial B_n}{\partial t} = -\frac{\partial U}{\partial B_n} \tag{19}$$

where  $-\partial U/\partial B_n$  represents the damping force acting on the fictitious particle, and the nuclear field  $B_n$  plays the role of the configuration coordinate Q in Fig. 8. The steady states  $\alpha$ ,  $\beta$ ,  $\gamma$  correspond to  $\partial U/\partial B_n = 0$ . Integration of Eq. (19) gives the following expression for the potential U [17]:

$$U(B_n) = \frac{B_n^2}{2 T_x}$$

$$-\frac{(\Delta B_{\rm ov})_{\rm max} \gamma T_1 B_1^2}{T_x (1 + \gamma^2 T_1 T_2 B_1^2)^{1/2}} \arctan\left[\frac{\gamma T_2 (B_0 + B_n - \hbar \omega/g \beta)}{(1 + \gamma^2 T_1 T_2 B_1^2)^{1/2}}\right]$$
(20)

This potential exhibits two minima (bistability) if condition (13) is satisfied. Comparison of Eqs. (20) and (12) shows that the steady state BEMR intensity is proportional to the second derivative of the potential at the minima  $\alpha$  and  $\gamma$ ,  $[U''(B_n)]_{\alpha,\gamma} = (\partial^2 U/\partial B_n^2)_{\alpha,\gamma}$ :

$$I_{\rm EPR} = I_0 - I_0 T_x \left[ U''(B_n) \right]_{a,\gamma}$$
<sup>(21)</sup>

Fig. 9 shows a 3D plot of the dynamic potential calculated from Eq. (20) for InP, corresponding to the spectrum of Fig. 7. Under slow sweeping of the magnetic field  $B_0$ , the shape of the potential is continuously modified, and exhibits either one or two minima. The 'trajectory' of the polarized electron-nuclear spin system (the fictitious particle) in the potential is marked by the full line in Fig. 9. It can be seen that the system switches from one potential minimum to the other



Fig. 9. (a) 3D plot of the dynamic potential calculated from Eq. (20) for InP at 3 K, corresponding to the spectrum of Fig. 7. (b) Variation of the BEMR intensity (Eq. (21)) deduced from the trajectory of the fictitious particle (the resonating electron–nuclear-spin system) in the potential.

when the potential barrier vanishes. Fig. 9 also shows that the shape of the first derivative of the EPR absorption is proportional to the second derivative of the dynamic potential.

#### 6. Conclusion

Magnetic resonance in an electron spin system under extreme narrowing condition is an intrinsically bistable resonance when the solid contains nuclear spins. BEMR implies a memory effect at the level of elementary quantum systems interacting with an electromagnetic field. Despite its originality with respect to other bistable systems described at the molecular level, such as bistable spin transitions for example [18], the similarity of these types of bistability appears more clearly when BEMR is described in terms of dynamic potential in the nuclear field space. BEMR also provides the simplest case of 'optical' bistability in a pair system AB, where the saturable absorber A is the electron-spin system and the feedback system B is the ensemble of nuclear spins polarized by A. The mechanism of BEMR can be extrapolated to IOB in pair systems AB, including atomic pairs [10].

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