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The nature of interactions between *N*-butylpyridinium tetrafluoroborate and thiophenic compounds: A theoretical investigation

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ABSTRACT

In an effort to understand the nature of the interactions between pyridinium-based ionic liquids and thiophenic compounds, the electronic and topological properties of the interactions between *N*-butylpyridinium tetrafluoroborate ([BPY]⁺[BF₄]⁻) and thiophene (TS), benzothiophene (BT), dibenzothiophene (DBT) have been investigated by density functional theory. The most stable structure of the [BPY]⁺[BF₄]⁻ ion-pair indicated that hydrogen bonding interactions between fluorine atoms on [BF₄]⁻ anions and C2–H2 on the pyridinium ring play an important role in the formation of the ion-pair. The NBO and AIM analyses indicate the occurrence of π - π stacking interactions. The electron density at bond critical points and Wiberg bond indices are correlated with the interacting distances of H...F interactions, so electron density and Wiberg bond index can demonstrate the interacting strength of H...F hydrogen bonds. The interaction energies suggest that DBT adsorbs prior to the other compounds on *N*-butylpyridinium tetrafluoroborate ionic liquid. © 2013 Académie des sciences. Published by Elsevier Masson SAS. All rights reserved.

1. Introduction

Fuel desulfurization has received worldwide attention because environmental regulation of the sulfur limit for fuels is becoming increasingly stringent. The EU legislation set the upper limit of the sulfur content in diesel fuels to 10 ppm in 2009 and the US Environmental Protection Agency (EPA) reduced the limit for the sulfur content in diesel fuels to 15 ppm in 2006–2010 [1,2]. Conventional hydrodesulfurization (HDS) is more effective for the removal of aliphatic sulfur compounds than for the removal of sulfur-containing aromatic compounds, such as thiophene, benzothiophene, and dibenzothiophene series. HDS requires high temperatures and high hydrogen pressures in order to eliminate the alicyclic sulfur compounds [3]. Alternative sulfur removal techniques should be explored. In the past years, ionic liquids have gained increasing interest due to their unique properties both as extractant and catalyst [4]. The first attempt of deep desulfurization using ionic liquids was made by Bosmann et al. in 2001 [5]. Lo et al. firstly investigated the removal of sulfur-containing compounds from light oils by a combination of both chemical oxidation and solvent extraction using imidazolium-based ionic liquids [6]. Following their reports, sulfur and nitrogen removals by extraction or oxidative desulfurization using ionic liquids have been extensively investigated.

Recently, pyridinium-based ionic liquids were employed to remove sulfur compounds from fuel [7–16]. The mechanism for the extraction of sulfur compounds with pyridinium-based ionic liquids was proposed as a possible π - π interaction between aromatic sulfur compounds and the pyridinium rings of ionic liquids.

In 2008, Gao et al. investigated the use of *N*-butylpyridinium tetrafluoroborate ($[BPY]^+[BF_4]^-$) as a solvent for deep desulfurization of fuels [7]. The high extraction of sulfur compounds with pyridinium-based ionic liquids was

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ascribed to a possible $\pi - \pi$ interaction between ionic liquids and aromatics. However, the detailed structures and nature of the interactions between [BPY]⁺[BF₄]⁻ and thiophene (TS), benzothiophene (BT), dibenzothiophene (DBT) are still unknown. Therefore, this work reports an analysis of structures of [BPY]⁺[BF₄]⁻, [BPY]⁺[BF₄]⁻ - TS, [BPY]⁺[BF₄]⁻ - BT, and [BPY]⁺[BF₄]⁻ - DBT complexes using quantum chemical calculations. The theoretical results here will confirm the formation of hydrogen bonding and $\pi \cdots \pi$ interactions between [BPY]⁺[BF₄]⁻ and TS, BT, DBT at the molecular level firstly.

2. Specification of initial structures

The structures of the *N*-butylpyridinium cation ([BPY]⁺), $[BF_4]^-$, thiophene (TS), benzothiophene (BT), and dibenzothiophene (DBT) are shown in Fig. 1. The $[BF_4]^-$ anion or/ and TS, BT, DBT have been gradually placed in different regions around the $[BPY]^+$ cation to form $[BPY]^+[BF_4]^-$, $[BPY]^+[BF_4]^- - TS$, $[BPY]^+[BF_4]^- - BT$, and $[BPY]^+[BF_4]^- - DBT$ for optimization. The most stable structures were further employed for NBO and AIM analyses.

3. Computational details

All geometric optimizations reported here were performed at the level of ω -B97XD/aug-cc-pVTZ with spherical-harmonic-type basis functions 5d and 7f. ω -B97XD was produced by Head-Gordon and Chai, whose work contains empirical dispersion and long-range corrections [17,18]. All the stationary structures have been fully optimized without geometrical constraints. A frequency analysis was performed on all structures to insure the absence of imaginary frequencies. To examine the nature of interactions, the electronic properties of stationary points are illustrated based on natural bond orbital (NBO) analysis [19]. These non-local donor–acceptor-orbital interactions are associated with the delocalization of electron density between states *i* and *j* in the NBO basis, as given by:



Fig. 1. Structures of (a) *N*-butylpyridinium($[BPY]^+$) (b) $[BF_4]^-$ (c) thiophene (TS) (d) benzothiophene (BT) and (e) dibenzothiophene (DBT).

where n_i is the donor orbital occupancy, ε_i and ε_j are the diagonal elements, and F_{ij} is the off-diagonal NBO Fork matrix element. Intermolecular interactions such as lone pair \rightarrow anti-bonding orbital mixtures are representative of donor–acceptor bonding, whereas non-Lewis-type (highly delocalized) interactions such as anti-bond \rightarrow anti-bond orbital mixtures represent effects like resonance stabilization. The AIM analysis was used to analyze the nature of interactions at the same level by AIM2000 package [20,21] with the wave function-generated results.

The interaction energies between $[BPY]^{+}[BF_{4}]^{-}$ and TS, BT, DBT were calculated using the following expression:

$$\Delta E = -\{E([BPY]^+[BF_4]^- - TS/BT/DBT) - [E([BPY]^+[BF_4]^-) + E(TS/BT/DBT)]\}$$

where $E([BPY]^+[BF_4]^- - TS/BT/DBT)$ represents the energies of $[BPY]^+[BF_4]^- - TS$, $[BPY]^+[BF_4]^- - BT$, and $[BPY]^+[BF_4]^- - DBT$, $E([BPY]^+[BF_4]^-)$, and $E([BPY]^+[BF_4]^-)$, E(TS/BT/DBT) the individual energies of $[BPY]^+[BF_4]^-$, TS, BT, DBT; ΔE is the interaction energies between $[BPY]^+[BF_4]^-$ and TS, BT, DBT. The basis set superposition error (BSSE) was also considered by the counterpoise method.

4. Results and discussion

4.1. Geometries of $[BPY]^{+}[BF_{4}]^{-}$, $[BPY]^{+}[BF_{4}]^{-} - TS$, $[BPY]^{+}[BF_{4}]^{-} - BT$ and $[BPY]^{+}[BF_{4}]^{-} - DBT$

In this section, we discussed the most stable geometries of $[BPY]^{+}[BF_{4}]^{-}$, $[BPY]^{+}[BF_{4}]^{-} - TS$, $[BPY]^{+}[BF_{4}]^{-} - BT$ and $[BPY]^+[BF_4]^- - DBT$. In order to give a visual understanding of [BPY]⁺[BF₄]⁻ pair interactions before the design of initial geometries for the ion-pair, the electrostatic potential for the most stable geometries of the isolated [BPY]⁺ cation and $[BF_4]^-$ anion were calculated to gain the possible interaction modes between cation and anion shown in Fig. 2, respectively. The highly negative regions of the $[BF_4]^-$ anion are on the electronegative F atoms, while the highly positive regions in the [BPY]⁺ cation are around the pyridinium ring hydrogen atoms and the butyl hydrogen atoms. The possible interacting sites on the more positively charged regions of the [BPY]⁺ cation and the more negatively charged regions of the $[BF_4]^-$ anion have been taken into consideration for the initial geometry design. The most stable structure of [BPY]⁺[BF₄]⁻ is shown in Fig. 3a. It can be found that $[BPY]^+[BF_4]^-$ has five F...H interactions. The interacting distances are 1.861 Å (F4...H2), 2.337 Å (F1...H2), 2.246 Å (F2...H71), 2.246 Å (F1...H71) and 2.506 Å (F4...H81), while the sum of Bondi's van der Waals radii of fluorine atom and hydrogen atom (1.47 Å and 1.20 Å) is 2.67 Å [22]. The short distances of H2 and H71-involved interactions may be ascribed to the highly positive H2 and H71 due to the withdrawing electron of the nitrogen atom. A single hydrogen atom may participate in two hydrogen bonds instead of one. This type of bonding is called bifurcated hydrogen bonding (threecenter hydrogen bonding) [23]. The results show that H71 and H2 in $[BPY]^+[BF_4]^-$ are involved in the formation of bifurcated hydrogen bonding. The F.-.H contacts within the bifurcated hydrogen bonds are found to be unequivalent in



Fig. 2. Electrostatic potentials (ESP) of (a) the [BF₄]⁻ anion and (b) the [BPY]⁺ cation.





Fig. 3. Optimized structures and some interacting distances $(\hat{A}) of(a) [BPY]^* [BF_4]^-, (b) [BPY]^* [BF_4]^- - TS, (c) [BPY]^* [BF_4]^- - BT, and (d) [BPY]^* [BF_4]^- - DBT.$ Color available on the web.

terms of the different $F \cdots H$ distances. These deviations from linearity of the C-H \cdots F angles are common for bifurcated hydrogen bonds.

The most stable structures of $[BPY]^+[BF_4]^- - TS$. $[BPY]^+[BF_4]^- - BT$ and $[BPY]^+[BF_4]^- - DBT$ are shown in Fig. 3b-3d. Similar results for the strongest hydrogen bonds between one fluorine atom on the $[BF_4]^-$ anion and C2–H2 on the pyridinium ring were obtained for the above three structures. In the most stable $[BPY]^+[BF_4]^- - TS$, $[BPY]^{+}[BF_{4}]^{-} - BT$ and $[BPY]^{+}[BF_{4}]^{-} - DBT$ structures, the ring planes of TS, BT, DBT and of the pyridinium ring are parallel to each other, implying that $\pi - \pi$ interactions may occur. $\pi - \pi$ Interaction (also called $\pi - \pi$ stacking) refers to attractive non-covalent interactions between aromatic rings. Despite their frequent occurrence, there is no unifying picture of the factors that contribute to the interaction, which include electrostatic (quadrapolequadrapole, quadrapole-dipole, and dipole-dipole), hydrophobic, and van der Waals interactions. This is complicated by the fact that aromatic rings interact in several different conformations, each of which is favored by a different combination of forces. The face-face stacked. edge-face stacked, and offset stacked geometries are three representative configurations of π - π interactions [24,25]. As shown in Fig. 3b-3d, the offset parallel stacking interactions between the pyridinium ring and TS, BT, DBT rings occur. The offset stacked interactions are dependent on the orientation of the rings; it seems that the interactions of S1...H91 (3.044 Å), F4...H2' (2.441 Å), F1…H2′ (2.403 Å) in [BPY]⁺[BF₄]⁻ – TS, F1…H7′ (2.575 Å), F4...H7'(2.408 Å), S'...H91 (2.889 Å) in $[BPY]^+[BF_4]^- - BT$, F3…H9' (2.369 Å), F2…H1' (2.642 Å), F3…H1' (2.365 Å) in $[BPY]^+[BF_4]^- - DBT$ may pronouncedly influence the formation of π - π interactions [26]. The interactions of $C5' \cdots C4$ (3.523 Å), $C2' \cdots C3$ (3.224 Å) in $[BPY]^+[BF_4]^- - TS$, C7a…C4 (3.214 Å) in [BPY]⁺[BF₄]⁻ – BT, C11'…C4 (3.205 Å) in $[BPY]^+[BF_4]^-$ – DBT demonstrate the occurrence of π – π interactions.

4.2. Interaction energies

The interaction energies between $[BPY]^+[BF_4]^-$ and TS, BT, DBT are important factors in reasonable explanations for the extraction of TS, BT and DBT by $[BPY]^+[BF_4]^-$ ionic liquids. So, we investigated the interaction energies between $[BPY]^+[BF_4]^-$ and TS, BT, DBT. Interaction energy (ΔE) is defined as the difference between the energy of the appointed complexes and the sum of the energies of its free fragments. The interaction energies between $[BPY]^+[BF_4]^-$ and TS, BT, DBT are 10.29 kcal/mol, 14.59 kcal/mol, and 18.30 kcal/mol, demonstrating that the magnitude of the interacting energies follows the trend $[BPY]^+[BF_4]^- - TS < [BPY]^+[BF_4]^- - BT < [B-[BPY]^+[BF_4]^- - DBT.$

4.3. NBO analysis

NBO analyses for TS, BT, DBT, $[BPY]^+[BF_4]^-$, $[BPY]^+[BF_4]^-$, $[BPY]^+[BF_4]^-$ – TS, $[BPY]^+[BF_4]^-$ – BT, and $[BPY]^+[BF_4]^-$ – DBT were carried out to obtain the charge distribution and intrinsic properties of the interactions between

[BPY]⁺[BF₄]⁻ and TS, BT, DBT. From NBO atomic charges, most of the positive charge is focused on the peripheral hydrogen atoms of the pyridinium ring and the butyl hydrogen atoms in the $[BPY]^+$ cation, while the $[BF_4]^$ anion preferentially approaches the positively charged groups, indicating that the electrostatic interaction between the $[BPY]^+$ cation and the $[BF_4]^-$ anion is dominative for the formation of the ion-pair. The sums of the charges of $[BF_4]^-$ in $[BPY]^+[BF_4]^-$, $[BPY]^+[BF_4]^- - TS$, $[BPY]^{+}[BF_{4}]^{-} - BT$, and $[BPY]^{+}[BF_{4}]^{-} - DBT$ are -0.94337, -0.95082, -0.95787, -0.95663, suggesting that the negative charges migrate from $[BF_4]^-$ to other parts. It is clear that TS, BT, DBT adsorptions on [BPY]⁺[BF₄]⁻ influence the charge distribution in [BPY]⁺[BF₄]⁻ and TS, BT, DBT. Compared with the NBO charges, the positive charge of H and the negative charge of F increase when they are involved in H…F interactions. The shorter the H…F contact, the larger the increase in the positive charges of hydrogen atoms and in the negative charges of fluorine atoms. The interactions between the F of $[BF_4]^-$ and TS, BT, DBT increase the negative charges of F, resulting in the less negative charge migration of $[BF_4]^-$ in $[BPY]^+[BF_4]^-$ -TS (-0.95082), $[BPY]^+[BF_4]^- - BT$ (-0.95787), and $[BPY]^+[BF_4]^- - DBT (-0.95663)$ in contrast with that of $[BPY]^+[BF_4]^-$ (-0.94337).

It seems quite well accepted that hydrogen bonding influences the structures of ionic liquids. The NBO method can provide information about the interactions in both filled and virtual orbital spaces that facilitates analysis of the intermolecular interactions. A second-order perturbation theory analysis of the Fock matrix was carried out to evaluate donor-acceptor interactions in the NBO basis. In this analysis, a stabilization energy E(2) related to the delocalization trend of the electrons from donor to acceptor orbitals was calculated via perturbation theory. If the stabilization energy E(2) between a donor bonding orbital and an acceptor-orbital is large, then there is a strong interaction between them. Table 1 lists the selected donor-acceptor interactions in [BPY]⁺[BF₄]⁻, $[BPY]^{+}[BF_{4}]^{-} - TS, [BPY]^{+}[BF_{4}]^{-} - BT, [BPY]^{+}[BF_{4}]^{-} - DBT$ and their second-order perturbation stabilization energies. As indicated in Table 1, the C2-H2 involved hydrogen bonds are the strongest, in terms of the large E(2) of 16.67 kcal/mol (LP(F4) $\rightarrow \sigma^{*}(C2-H2)$) in [BPY]⁺[BF₄]⁻, 9.13 kcal/mol (LP(F3) $\rightarrow \sigma^{*}(C2-H2)$) in [BPY]⁺[BF₄]⁻ – TS, 7.01 kcal/mol (LP(F3) $\rightarrow \sigma^{*}(C2-H2)$) in [BPY]⁺[BF₄]⁻ – BT, 5.38 kcal/mol (LP(F4) $\rightarrow \sigma^{*}(C2-H2)$) in [BPY]⁺[BF₄]⁻ – DBT, in agreement with their short F...H contacts.

The π - π interactions were studied based on the calculations of the natural bond orbital (NBO) method, which is now widely used for analyzing chemical bonds in non-covalent compounds. Table 1 shows that hydrogen bonding (LP(F)- σ *(C-H)), and LP(F)- π occur between [BPY]*[BF₄]⁻ and TS, BT, DBT. The $\pi(\pi^*) \rightarrow \pi^*$ interactions between [BPY]*[BF₄]⁻ and TS, BT, DBT indicate the occurrence of π - π interactions. It is noted that the charges of sulfur of TS, BT, and DBT are +0.45934, +0.42368 and +0.41332, while the sulfur-involved interactions are LP(S1)- σ *(C9-H91) (0.64 kcal/mol), LP(S1)- π *(C2-N1) (0.27 kcal/mol) in [BPY]*[BF₄]⁻ – TS, LP(S1')- σ *(C9-H91) (2.18 kcal/mol) in [BPY]*[BF₄]⁻ – BT, indicating that the

Table 1

Some donor-acceptor interactions in $[BPY]^{+}[BF_{4}]^{-}$, $[BPY]^{+}[BF_{4}]^{-} - TS$, $[BPY]^{+}[BF_{4}]^{-} - BT$, $[BPY]^{+}[BF_{4}]^{-} - DBT$ and their second-order perturbation stabilization energies, E(2) (kcal/mol).

Donor	Acceptor	<i>E</i> (2) (kcal/mol)	Donor	Acceptor	E(2) (kcal/mol)
[RDV]+[RF.]-	X			*	
[DF 1] [DF4] [D(F1)]	$\pi^{*}(N1-C2)$	1.47	IP(F1)	$\sigma^{*}(C7-H71)$	1.46
LP(F1)	$\sigma^{*}(C2-H2)$	0.31	LP(F1)	$\sigma^{*}(N1-C2)$	0.06
LP(F1)	$\sigma^{*}(N1-C7)$	0.06	LP(F1)	$\sigma^{*}(C2-C3)$	0.08
LP(F3)	$\sigma^*(C2-H2)$	0.12	LP(F3)	$\sigma^{*}(C7-H71)$	0.18
LP(F4)	$\sigma^*(C2-H2)$	16.67	LP(F4)	$\sigma^{*}(C8-H81)$	1.27
LP(F2)	σ*(C7-H71)	2.43	LP(F2)	$\sigma^*(C8-C9)$	0.18
LP(F2)	σ*(N1-C7)	0.10			
[BPY] [BF4] - 15 [D(E1)]	(C) U)	1 10	ID/E1)	(C2 N1)	0.42
LI (III)	$\sigma^{*}(C4, C3)$	0.11	LI (II)	$\pi^{*}(C2' - C3')$	0.45
IP(F1)	$\pi^{*}(C2-N1)$	0.19	IP(F1)	$\sigma^{*}(C2'H2')$	1.48
LP(F3)	$\sigma^{*}(C9-C8)$	0.08	LP(F3)	$\sigma^{*}(C7-H71)$	0.64
LP(F3)	$\sigma^{*}(C8-H81)$	0.15	LP(F3)	$\sigma^{*}(C2-H2)$	9.13
LP(F3)	$\sigma^{*}(C7-H72)$	0.06	LP(F3)	$\sigma^{*}(C2-C3)$	0.11
LP(F3)	$\sigma^{*}(C2'-H2')$	0.07	LP(F4)	$\sigma^{*}(C8-H81)$	5.47
LP(F4)	$\pi^{*}(C2-N1)$	0.12	LP(F4)	$\sigma^*(C2'-H2')$	0.66
LP(F4)	$\sigma^*(C2'-C3')$	0.24	LP(F4)	σ*(S1-C5')	0.55
LP(F2)	σ*(C2-H2)	0.24	$\pi(C4-C3)$	$\pi^{*}(C2'-C3')$	0.06
LP(F2)	$\pi^{*}(C2-N1)$	0.07	$\pi(C5-C6)$	$\pi^{*}(C4'-C5')$	0.11
σ(C9–H91)	σ*(S1-C2')	0.07	$\pi^{*}(C4-C3)$	$\pi^{*}(C2'-C3')$	1.51
$\pi^{*}(C2-N1)$	$\pi^{*}(C2'-C3')$	0.12	$\pi^{*}(C5-C6)$	$\pi^{*}(C4'-C5')$	0.46
$\pi(C4'-C5')$	$\pi^{*}(C4-C3)$	0.86	$\pi(C2'-C3')$	$\pi^{*}(C4-C3)$	0.54
$\pi(C2'-C3')$	$\pi^{*}(C5-C6)$	0.05	$\pi(C4'-C5')$	$\pi^{*}(C5-C6)$	0.14
LP(S1)	π*(C2–N1)	0.27	LP(S1)	σ*(C9–H91)	0.64
[BPV] ⁺ [BF.] ⁻ _ BT					
LP(F1)	$\sigma^{*}(C4-C3)$	0.27	LP(F1)	$\sigma^{*}(C3-H3)$	0.48
LP(F1)	$\pi^{*}(C4-C3)$	0.22	LP(F1)	$\sigma^*(C2-N1)$	0.22
LP(F1)	$\pi^{*}(C2-N1)$	0.08	LP(F1)	$\sigma^*(C2-H2)$	0.08
LP(F1)	σ*(C8-H81)	0.10	LP(F1)	σ*(C7'-H7')	0.39
LP(F3)	σ*(C2-H2)	7.01	LP(F3)	σ*(C2-C3)	0.06
LP(F3)	$\pi^{*}(C2-N1)$	0.20	LP(F3)	σ*(C8-H81)	1.75
LP(F4)	$\pi^{*}(C2-N1)$	1.15	LP(F3)	σ*(C7′-H7′)	0.15
LP(F4)	σ*(C7'-H7')	1.03	LP(F4)	σ*(C8-H81)	2.05
LP(F4)	σ*(C8–H82)	0.08	LP(F4)	σ*(C2'-S1')	0.17
LP(F4)	$\pi^{*}(C6'-C7')$	0.06	LP(F4)	σ*(C6′-C7′)	0.05
LP(F2)	σ*(C8–H81)	0.06	LP(F2)	$\pi^{*}(C2-N1)$	0.13
LP(F2)	σ*(C2-H2)	0.09	$\pi(C6'-C7')$	$\pi^{*}(C2-N1)$	0.05
π (C4–C3)	π*(C7a-C3a)	0.13	π (C4–C3)	$\pi^{*}(C6'-C7')$	0.27
$\pi(C6'-C7')$	σ*(C3-H3)	0.05	$\pi^{*}(C4-C3)$	$\pi^{*}(C6'-C7')$	0.16
$\pi(C5'-C4')$	$\sigma^*(C4-H4)$	0.84	$\pi(C6'-C7')$	$\pi^{*}(C4-C3)$	0.08
$\pi(C3'-C2')$	$\pi^{*}(C5-C6)$	0.14	$\pi(C/a-C3a)$	$\pi^{*}(C4-C3)$	1.21
$\pi(C/a-C3a)$	$\pi^{*}(C5-C6)$	0.09	$\pi(C3^{-}C2^{+})$	σ*(C5-H5)	0.06
EF(31)	0 (09-091)	2.10			
$[BPY]^+[BF_4]^ DBT$					
LP(F1)	$\pi^{*}(C2-N1)$	0.12	LP(F1)	σ*(C2–H2)	0.10
LP(F1)	σ*(C8–H81)	0.06	σ (C10–H101)	σ*(C8′-H8′)	0.11
LP(F3)	$\sigma^*(C9'-H9')$	1.67	LP(F3)	$\sigma^*(C1'-H1')$	1.63
LP(F3)	$\pi^{*}(C2-N1)$	1.40	LP(F3)	$\sigma^{*}(C8-H81)$	0.73
LP(F3)	$\sigma^{*}(C10-H101)$	0.13	LP(F3)	σ*(C8-H82)	0.09
LP(F4)	$\sigma^*(CI'-HI')$	0.15	LP(F4)	$\sigma^{*}(C2-H2)$	5.38
LP(F4)	$\sigma^{*}(C2 - H81)$	4.08	LP(F4)	$\pi^{*}(C2-N1)$	0.15
LP(F2)	$\sigma^{*}(C11/C1/)$	0.05	LP(F2)	$\sigma^{*}(C4, C2)$	0.15
IP(F2)	$\pi^{*}(C3-H3)$	0.44	IP(F2)	$\pi^{*}(C4-C3)$	0.24
IP(F2)	$\sigma^{*}(C2-N1)$	0.18	IP(F2)	$\sigma^{*}(C8-H81)$	0.09
IP(F2)	$\pi^{*}(C2-N1)$	0.06	IP(F2)	$\sigma^{*}(C11'-C1')$	0.05
LP(F2)	$\sigma^{*}(C1'-H1')$	0.08	$\sigma(C4-H4)$	$\pi^*(C12'-C4')$	0.09
$\pi^*(C12'-C4')$	$\sigma^*(C4-H4)$	0.13	$\pi^{*}(C4-C3)$	$\sigma^{*}(C4'-H4')$	0.15
$\pi(C13'-C10')$	$\pi^{*}(C4-C3)$	0.47	$\pi(C13'-C10')$	$\pi^*(C5-C6)$	0.51
$\pi(C6'-C7')$	σ*(C5-H5)	0.08	$\pi(C11'-C1')$	$\pi^{*}(C5-C6)$	0.06
$\pi(C8'-C9')$	σ*(C9-H91)	1.19	$\pi(C12'-C4')$	σ*(C4–H4)	0.39
π (C4–C3)	π*(C13'-C10')	0.17	σ(C4-H4)	π*(C11'-C1')	0.10
σ(C3-H3)	π*(C11′-C1′)	0.06	σ(C8'-H8')	σ*(C9–H91)	0.07
$\pi^{*}(C4-C3)$	$\pi^{*}(C11'-C1')$	2.83	$\pi^{*}(C5-C6)$	π*(C8′-C9′)	0.06
σ(C8'-H8')	σ*(C9–H91)	0.08	$\pi(C11'-C1')$	π*(C2–N1)	0.06
σ(C12'-C4')	σ*(C5-H5)	0.07	$\pi(C12'-C4')$	σ*(C6–N1)	0.07
$\pi(C2'-C3')$	σ*(C3-H3)	0.06	σ(C3'-C4')	σ*(C5–H5)	0.06
σ(C4-H4)	σ*(C5–H5)	0.32	σ (C4–H4)	σ*(C6–N1)	0.17



Fig. 4. Wiberg bond indices of (a) pyridinium ring bonds of $[BPY]^*[BF_4]^-$, $[BPY]^*[BF_4]^- - TS$, $[BPY]^*[BF_4]^- - BT$, and $[BPY]^*[BF_4]^- - VDBT$, (b) thiophenic ring bonds of TS and $[BPY]^*[BF_4]^- - TS$, (c) benzothiophenic ring bonds of BT and $[BPY]^*[BF_4]^- - BT$, and (d) dibenzothiophenic ring bonds of DBT and $[BPY]^*[BF_4]^- - DBT$. Color available on the web.

trend of sulfur-involved interactions is BT > TS > DBT, which may be ascribed to steric hindrance.

In addition, the Wiberg bond index (WBI) [27] has been used to evaluate the number of covalent bonds, or evaluate the strength of covalent bonds. The Wiberg bond index is calculated as the sum of the quadratic non-diagonal elements of the density matrix between two atoms. In π - π stacking systems if the distance of a pair of atoms is within 3.7 Å, there may be a special π - π stacking bond for this pair of atoms and ring bond strength should be evaluated by the Wiberg bond index. So, we try to evaluate the ring bond strengths of the present π - π stacking system with the Wiberg bond index. Fig. 4 displays the Wiberg bond indices (WBI) of ring bonds. The significant changes of WBI of ring bonds may be ascribed to the π - π interactions. There exist bond critical points of C5'...C4, C2'...C3 in $[BPY]^{+}[BF_{4}]^{-}$, C3'...C5, C7a...C4 in $[BPY]^{+}[BF_{4}]^{-}$ – BT, and C4...C11' in $[BPY]^+[BF_4]^- - DBT$, their corresponding WBI are 0.0035, 0.0054, 0.0006, 0.0032 and 0.0028, indicating the occurrence of π - π interactions.

The WBI of the H···F interactions of $[BPY]^+[BF_4]^-$, $[BPY]^+[BF_4]^- - TS$, $[BPY]^+[BF_4]^- - BT$, $[BPY]^+[BF_4]^- - DBT$ and their corresponding interacting distances are shown in Fig. 5. It can be seen that the WBI are correlated with their interacting distances. The higher the WBI, the longer the interacting distances.

4.4. Topological properties analyses

The bond properties between each pair of atoms were systematically analyzed using quantum theory of atoms in molecules (AIM) [28], which is based on the topological analysis of electron density (ρ) and of its Laplacian ($\bigtriangledown^2 \rho$) at



Fig. 5. Relationship between F...H distances (Å) and their Wiberg bond indices. Color available on the web.

Table 2

The topological properties of electron density (ρ), Laplacian of density ($\nabla^2 \rho$), Wiberg bond indices (WBI) of TS, BT, DBT, [BPY]⁺[BF₄]⁻, [BPY]⁺[BF₄]⁻ – TS, [BPY]⁺[BF₄]⁻ – DBT (atomic units).

TS TS ring (3, +1) 0.03905 0.27129 BT TS ring (3, +1) 0.03701 0.25568 DBT Sring (3, +1) 0.03517 0.4005 DBT Sring (3, +1) 0.03517 0.42005 DBT B7 ring2 (3, +1) 0.02072 0.16270 [BPV]'[BF_4]^- F1-H2 (3, -1) 2.337 0.01320 0.05663 0.00207 [BPV]'[BF_4]^- F1-H2 (3, -1) 2.466 0.01357 0.05811 0.00297 P1-H2 (3, -1) 2.246 0.01355 0.00237 0.03499 0.017 P1-H2 (3, -1) 2.246 0.01355 0.0127 0.05634 0.00497 P1-H2 (3, -1) 2.2177 0.01303 0.05634 0.00497 P1-H2 (3, -1) 2.441 0.00951 0.03493 0.0025 P1-H2 (3, -	Species	X…Y	cp type	D/Å	ρ	$\bigtriangledown^2 ho$	WBI
BT Sring BZ ring S. + ing S. ring BZ ring S. + ing S. ring S. ring S. + ing S. ring BPY S. + ing S. ring S. + ing S. + ing S. + ing S. + ing S. + ing<	TS	TS ring	(3, +1)		0.03905	0.27129	
BZ mg (3, +1) 0.02053 0.16178 DBT TS ng (3, +1) 0.03517 0.24065 [BFY]"[BF4]- TS ng (3, +1) 0.02072 0.16270 [BFY]"[BF4]- (3, -1) 2.37 0.01387 0.05191 0.0026 [F1-H71 (3, -1) 2.246 0.01387 0.05191 0.00867 [F4-H81 (3, -1) 2.246 0.01387 0.0020 0.00867 [F4-H81 (3, -1) 2.246 0.01387 0.00393 0.0017 [F4-H81 (3, -1) 2.246 0.01355 0.05211 0.00867 [F4-H81 (3, -1) 2.277 0.01303 0.01343 0.00144 [F4-H81 (3, -1) 2.471 0.01393 0.01343 0.0024 [F4-H81 (3, -1) 2.434 0.00651 0.00353 0.0024 [F4-H81 (3, -1) 2.434 0.00651 0.00353 0.0024 0.00470	ВТ	TS ring	(3, +1)		0.03701	0.25568	
DBT 15 ring B2 ring2 (3, +1) (3, +1) 0.03317 0.02072 0.16270 0.16270 [BFV]"[BF4] FIH71 (3, -1) 2.337 0.01320 0.05963 0.0025 [BFV]"[BF4] FIH71 (3, -1) 2.337 0.01327 0.035963 0.0025 [BFV]"[BF4] FIH71 (3, -1) 2.566 0.00297 0.03499 0.0017 [F2H71] (3, -1) 2.518 0.00797 0.03499 0.0017 [F2-H71] (3, -1) 2.772 0.01303 0.05614 0.00498 [F4-H81] (3, -1) 2.772 0.01303 0.05614 0.00491 [F4-H81] (3, -1) 2.472 0.01323 0.07393 0.0224 [F4-H81] (3, -1) 2.172 0.01325 0.0125 0.0125 [F4-H81] (3, -1) 2.172 0.01323 0.00481 0.0052 [F4-H7] (3, -1) 2.0445 0.00521 0.0117 0.0035 [F4-H7] (3, -1)		BZ ring	(3, +1)		0.02053	0.16178	
Dot BZ mgg (3, +1) 002072 0.16270 BPY]"[BF_a]" Fi-H12 (3, +1) 002072 0.16270 [BPY]"[BF_a]" Fi-H171 (3, -1) 2.337 0.01320 0.05963 0.0020 Fi-H71 (3, -1) 2.246 0.01355 0.05191 0.0036 Fi-H71 (3, -1) 2.246 0.01355 0.05211 0.0089 Fi-H71 (3, -1) 2.518 0.00797 0.03499 0.0017 Fi-H2 (3, -1) 2.518 0.00797 0.03499 0.0017 Fi-H2 (3, -1) 2.518 0.00797 0.03499 0.0017 Fi-H2 (3, -1) 2.518 0.00752 0.036634 0.0041 Fi-H2 (3, -1) 2.414 0.00512 0.0012 0.00151 0.0014 Fi-H3 (3, -1) 2.441 0.00521 0.00051 0.00380 0.0022 Fi-H47 (3, -1) 2.403 0.00521	חפת	TS ring	(3 +1)		0.03517	0.24005	
BZ mg2 (3, +1) 0.02072 0.12270 [BPY]"[BF4] ⁻ FI-M71 (3, -1) 2.337 0.01327 0.05963 0.0025 [4-H2 (3, -1) 2.367 0.01327 0.03991 0.0035 [4-H2 (3, -1) 1.861 0.02927 0.08921 0.0391 [2-H71] (3, -1) 2.246 0.01355 0.05211 0.0099 [BPY]"[BF4] ⁻ - TS [3-H71] (3, -1) 2.518 0.00797 0.03499 0.0017 [BP4]"[BF4] ⁻ - TS [3-H71] (3, -1) 2.518 0.00797 0.03499 0.0017 [BP4]"[BF4] ⁻ - TS [3-H71] (3, -1) 2.441 0.00822 0.04051 0.0047 [BP4]"[BF4] ⁻ - TS [3-H1] 2.403 0.00077 0.00396 0.0229 [F1-H2] (3, -1) 3.624 0.00079 0.0214 0.0025 [F1-H2] (3, -1) 2.403 0.00073 0.0025 0.00370 0.0025 [F1-H2] (3, -1)<	DBI	R7 ring1	$(3, \pm 1)$ (3 +1)		0.03017	0.24003	
[BPY]'[BF4]" F1-H2 31 2.337 0.01320 0.05963 0.0005 F1-H71 31 2.246 0.01337 0.05191 0.0085 F4-H81 31 2.246 0.01355 0.05211 0.0039 F4-H81 31 2.2566 0.00804 0.0312 0.0039 PY ing (3.+1) 0.02211 0.1729 [BPY]'[BF4]" - TS F3-H71 (31) 2.518 0.00797 0.03499 0.0214 F1-H22 (31) 2.172 0.01525 0.0215 0.0214 F1-H21 (31) 2.172 0.01529 0.0214 0.0049 F1-H22 (31) 2.441 0.0051 0.03508 0.0022 F1-H22 (31) 3.243 0.0051 0.03508 0.0022 F1-H21 (31) 2.403 0.0011 0.03803 0.0025 F1-H21 (31) 2.403 0.00214 0.00470 0.0025 F1-H21 </td <td></td> <td>BZ ring2</td> <td>(3, +1)</td> <td></td> <td>0.02072</td> <td>0.16270</td> <td></td>		BZ ring2	(3, +1)		0.02072	0.16270	
[BPT] [BF4] Filler 1 3, -1) 2.537 0.01387 0.05191 0.0020 H4 H12 3, -1) 1.861 0.02227 0.0891 0.00367 H4 H12 3, -1) 1.861 0.02221 0.03312 0.00367 P2 H71 3, -1) 2.246 0.01357 0.05211 0.00800 P2 H71 3, -1) 2.246 0.01353 0.05211 0.00801 P3 H2 3, -1) 2.518 0.00797 0.03499 0.0017 F3 H2 3, -1) 2.172 0.01303 0.05634 0.0448 H4 H81 3, -1) 2.172 0.01303 0.00215 0.0127 F4 H81 (3, -1) 3.184 0.00521 0.0125 0.0127 F4 H2 (3, -1) 3.224 0.00533 0.00470 0.0025 F5<-C4		E1 U2	(2 1)	2 2 2 7	0.01220	0.05062	0.0020
[BPY]'[BF4]^ BT F3 - H2 (3, -1) 2.640 0.0135 0.0391 0.0039 [BPY]'[BF4]^ TS P' ring (3, +1) 2.266 0.00804 0.03312 0.0039 [BPY]'[BF4]^ TS P' ring (3, +1) 0.02253 0.07393 0.02134 [BPY]'[BF4]^ TS P' ring (3, -1) 2.177 0.01529 0.05125 0.00234 [B+H2] (3, -1) 2.177 0.01529 0.05125 0.00234 [B+H2] (3, -1) 2.177 0.01529 0.00135 0.00235 [B+H2]' (3, -1) 2.441 0.00251 0.00205 0.0021 [G'-C4 (3, -1) 3.243 0.00513 0.00430 0.0025 [G'-C4 (3, -1) 3.224 0.00523 0.01397 0.0035 [BPY]'[BF4]^ BT F3H2 (3, -1) 2.377 0.01021 [BPY]'[BF4]^ BT F3H2 (3, -1) 2.377 0.01023 0.0035 [G'-C4 (3, -1)		Г1…ПZ F1_H71	(3, -1)	2.557	0.01320	0.05905	0.0020
IBPY]"[BF4]" - BT IS-1 2.506 0.00001 0.00351 0.0003 [BFY]"[BF4]" - TS IS-4171 (3, -1) 2.246 0.01355 0.05211 0.0003 [BFY]"[BF4]" - TS IS-4171 (3, -1) 2.518 0.00797 0.03499 0.00174 IFA-H2 (3, -1) 2.518 0.00797 0.03499 0.00174 IFA-H2 (3, -1) 2.777 0.01303 0.05634 0.0049 IFA-H2 (3, -1) 2.441 0.00952 0.004651 0.0049 IFA-H2 (3, -1) 3.184 0.00513 0.00253 0.00479 IFA-H2 (3, -1) 3.243 0.00523 0.00479 0.00303 IFA-H2 (3, -1) 3.244 0.00759 0.02143 0.0052 IFA-H31 (3, -1) 2.405 0.00682 0.0179 0.0035 IFA-H81 (3, -1) 2.405 0.00682 0.01742 IBPY]"[BF4]" - BT F3-H2 (3, -1) 2.405 0.00682		F4H2	(3, -1)	1 861	0.01987	0.03131	0.0085
i2-477 (3, -1) 2.246 0.01355 0.05211 0.0080 [BFY]"[BF4]" - TS P' ring (3, -1) 2.518 0.00797 0.03499 0.0017 F3-H71 (3, -1) 1.975 0.02333 0.07393 0.0234 F1-H2 (3, -1) 1.975 0.02333 0.07393 0.0234 F4-H81 (3, -1) 2.177 0.01529 0.05125 0.0177 F4-H81 (3, -1) 2.441 0.00591 0.0048 0.0029 F1-H2 (3, -1) 3.184 0.00511 0.0363 0.0029 F1-H2 (3, -1) 3.044 0.00573 0.00470 0.00253 C2'C3 (3, -1) 3.224 0.00763 0.0177 0.00362 C2'C4 (3, -1) 2.045 0.02688 0.06820 0.0179 T5 ring (3, -1) 2.045 0.02684 0.04017 0.0015 F1-H3 (3, -1) 2.045 0.02684 0.04017 0.015 F1-H41 <td></td> <td>F4H81</td> <td>(3, -1)</td> <td>2 506</td> <td>0.00804</td> <td>0.03312</td> <td>0.0039</td>		F4H81	(3, -1)	2 506	0.00804	0.03312	0.0039
PY ring (3, +1) 0.02211 0.17729 [BPY]"[BF4]" - TS F3-H71 (3, -1) 2.518 0.00737 0.03499 0.00174 F3-H42 (3, -1) 1.975 0.00233 0.0534 0.00184 F1-H42 (3, -1) 2.277 0.01303 0.05634 0.0049 F4-H21 (3, -1) 2.441 0.00922 0.04051 0.0049 F4-H21 (3, -1) 3.184 0.00651 0.03038 0.0022 S1-H91 (3, -1) 3.244 0.00573 0.00470 0.0025 C5'C4 (3, -1) 3.224 0.00769 0.02143 0.0054 PY ring (3, +1) 0.03901 0.27120 T5 ring (3, +1) 0.03901 0.27120 [BPY]"[BF4]" - BT F1-H81 (3, -1) 2.377 0.01027 0.04058 0.0052 F1-H87 (3, -1) 2.575 0.00664 0.027120 -		F2H71	(3, -1)	2.246	0.01355	0.05211	0.0080
[BPY]'[BF4]^ TS F3-H71 (3, -1) 2.518 0.00797 0.03499 0.0017 F3-H2 (3, -1) 1.975 0.02333 0.07393 0.0234 F4-H81 (3, -1) 2.277 0.01303 0.05634 0.0048 F4-H81 (3, -1) 2.172 0.01529 0.00151 0.0049 F4-H21 (3, -1) 2.441 0.00252 0.00491 0.0049 F4-H21 (3, -1) 3.144 0.00511 0.03088 0.0025 S1-H91 (3, -1) 3.243 0.00769 0.02143 0.0051 C2'-C3 (3, -1) 3.224 0.00769 0.02143 0.0052 C2'-C3 (3, -1) 2.237 0.0380 0.0052 0.0298 0.00753 T5 ring (3, -1) 2.437 0.00268 0.0052 0.02143 0.0052 F1-H3 (3, -1) 2.307 0.00386 0.0015 0.0052 F1-H3 (3, -1) 2.375 0.00662 0.02990 0.0015		PY ring	(3, +1)		0.02211	0.17729	
[h11] [b14] = 15 [b-h12] (b, -1) 2.10 0.0749 0.0749 0.0749 Fi-H22 (3, -1) 2.277 0.01303 0.06634 0.0048 Fi-H22 (3, -1) 2.172 0.01529 0.05125 0.0177 Fi-H22 (3, -1) 2.441 0.00922 0.04051 0.0049 Fi-H22 (3, -1) 2.441 0.00523 0.00470 0.0025 S1-H91 (3, -1) 3.204 0.00573 0.00470 0.0025 S1-H91 (3, -1) 3.224 0.00769 0.02143 0.0051 C2'-c4 (3, -1) 3.224 0.00769 0.02143 0.0052 C2'-c4 (3, -1) 2.045 0.02068 0.06820 0.0179 F3-H81 (3, -1) 2.377 0.01027 0.04058 0.0052 F1-H7 (3, -1) 2.305 0.00844 0.00417 0.0012 F4-H81 (3, -1) 2.408 0.00572 0.03330 0.0037 F4-H81	[BDV] ⁺ [BF.] ⁻ TS	F3 H71	(3 1)	2 5 1 8	0.00797	0.03499	0.0017
BPY]*[BF4]* - BT B*-H2 (3, -1) 2277 0.01303 0.06634 0.0048 H=-H81 (3, -1) 2172 0.01329 0.00125 0.0124 H=-H81 (3, -1) 2.112 0.01529 0.00451 0.0049 H=-S1 (3, -1) 3.184 0.00511 0.03058 0.0025 SI-H91 (3, -1) 3.243 0.00573 0.00470 0.0025 G'-C3 (3, -1) 3.224 0.00769 0.02143 0.0054 PY ring (3, -1) 2.245 0.02068 0.06820 0.0179 FB-H81 (3, -1) 2.377 0.01027 0.04688 0.0052 FI-H7 (3, -1) 2.377 0.01062 0.02990 0.0017 FI-H81 (3, -1) 2.375 0.00662 0.02990 0.0017 FI-H7 (3, -1) 2.308 0.01194 0.04573 0.0059 F4-S1' (3, -1) 2.316 0.00571 0.03330 0.0037 F1-H7	[D[1][D[4]] = 15	F3H2	(3, -1)	1 975	0.02353	0.03433	0.0017
iF4-H81 (3, -1) 2.172 0.01525 0.05125 0.0127 iF4-H81 (3, -1) 2.441 0.00621 0.00949 iF4-H2' (3, -1) 2.441 0.00621 0.03058 0.0025 iF1-H2' (3, -1) 2.403 0.00911 0.03803 0.0025 iS1-H91 (3, -1) 3.523 0.00523 0.01397 0.0035 C2'C3 (3, -1) 3.523 0.00769 0.02143 0.0054 PY ring (3, +1) 0.02209 0.17742 TS ring (3, +1) 0.02209 0.17742 [BPY]'[BF4]^ BT F3H81 (3, -1) 2.500 0.0084 0.04017 0.0015 F1H3 (3, -1) 2.500 0.0052 0.02284 0.0017 0.00057 F4H81 (3, -1) 2.308 0.01194 0.04573 0.00027 F4H7' (3, -1) 2.308 0.01194 0.04058 0.0057 F4H44 </td <td></td> <td>F1H2</td> <td>(3, -1)</td> <td>2 277</td> <td>0.01303</td> <td>0.05634</td> <td>0.0234</td>		F1H2	(3, -1)	2 277	0.01303	0.05634	0.0234
F4-H27 (3, -1) 2.441 0.00922 0.04051 0.0099 F4-S1 (3, -1) 3.184 0.00651 0.03058 0.0029 S1-H91 (3, -1) 2.403 0.00911 0.03803 0.0025 S1-H91 (3, -1) 3.523 0.01397 0.00470 0.0025 C5'C4 (3, -1) 3.523 0.01397 0.0054 0.0079 0.02143 0.0054 PY ring (3, +1) 0.02209 0.17742 TS ring (3, +1) 0.02058 0.06820 0.0179 F3H81 (3, -1) 2.507 0.000884 0.04051 0.00151 F1-H7 (3, -1) 2.508 0.01140 0.04573 0.0027 F4-H81 (3, -1) 2.408 0.00957 0.03930 0.0037 F4-H7 (3, -1) 2.408 0.00154 0.04573 0.0062 C3'-C5 (3, -1) 2.889 0.00771 0.02044 0.0062		F4H81	(3, -1)	2.172	0.01529	0.05125	0.0127
F4-S1 (3, -1) 3.184 0.0051 0.03858 0.0029 F1H2' (3, -1) 2.403 0.00911 0.03803 0.0025 S1H91 (3, -1) 3.523 0.00573 0.00470 0.0025 C2'-C3 (3, -1) 3.523 0.00769 0.02143 0.0054 PY ring (3, +1) 0.03901 0.27742 TS ring (3, +1) 0.03901 0.0758 0.0052 [BPY]"[BF4] ⁻ - BT F3H2 (3, -1) 2.377 0.01027 0.04058 0.0052 F1H7 (3, -1) 2.500 0.00884 0.0019 0.0051 F4H81 (3, -1) 2.308 0.01194 0.04573 0.0059 F4H7' (3, -1) 2.308 0.00194 0.0051 0.0052 F4H7' (3, -1) 2.899 0.00771 0.00444 0.0052 C3'-C5 (3, -1) 2.897 0.00646 0.02133 0.00162 C4'-H4		F4…H2′	(3, -1)	2.441	0.00922	0.04051	0.0049
FIH2' (3, -1) 2.403 0.00911 0.03803 0.0025 S1H91 (3, -1) 3.044 0.00573 0.00470 0.0025 C2'-C3 (3, -1) 3.224 0.00769 0.02143 0.0054 PY ring (3, +1) 0.03901 0.27120 [BPY]'[BF4]^ BT F3H2 (3, -1) 2.377 0.01027 0.04058 0.0052 F1H3 (3, -1) 2.377 0.01027 0.04058 0.0052 F1-H3 (3, -1) 2.575 0.00684 0.04017 0.0015 F4H81 (3, -1) 2.408 0.00957 0.03930 0.0037 F4H7' (3, -1) 3.315 0.00562 0.02284 0.0019 H91S1' (3, -1) 3.315 0.00564 0.00165 0.00052 G3'-C5 (3, -1) 3.759 0.00347 0.0016 0.00226 0.0032 PY ring (3, +1) 0.02276 0.00321 0.0016 0.00		F4S1	(3, -1)	3.184	0.00651	0.03058	0.0029
S1H91 (3, -1) 3.044 0.00573 0.00470 0.0025 C5'-C4 (3, -1) 3.523 0.00523 0.01397 0.0035 C2'-C3 (3, -1) 3.224 0.00769 0.02143 0.0054 PY ring (3, +1) 0.02209 0.17742 [BPY]'[BF4]'- BT F3-H2 (3, -1) 2.045 0.02068 0.06820 0.0179 F3-H81 (3, -1) 2.377 0.01027 0.04058 0.0052 F1H3 (3, -1) 2.575 0.00662 0.0290 0.0021 F4-H7 (3, -1) 2.308 0.01194 0.04573 0.0062 C3'-C5 (3, -1) 3.315 0.00502 0.02284 0.0015 F4-H7 (3, -1) 3.315 0.0057 0.00333 0.00162 C4'-H4 (3, -1) 2.837 0.00646 0.0213 0.00162 C3'-C5 (3, -1) 3.718 0.00574 0.0032 PY ring <		F1H2'	(3, -1)	2.403	0.00911	0.03803	0.0025
		S1H91	(3, -1)	3.044	0.00573	0.00470	0.0025
[BPY]"[BF4]" - DBT F3H2 (3, -1) 3.224 0.00769 0.02143 0.0054 PY ring (3, +1) 0.03901 0.271742 [BPY]"[BF4]" - BT F3H2 (3, -1) 2.045 0.02068 0.06820 0.0179 F3H81 (3, -1) 2.377 0.01027 0.04058 0.0052 F1H3 (3, -1) 2.500 0.00662 0.02900 0.0021 F4H81 (3, -1) 2.308 0.01194 0.04573 0.0059 F4H7' (3, -1) 2.308 0.00771 0.02444 0.0061 C3'C5 (3, -1) 3.315 0.00502 0.02284 0.0019 H91S1' (3, -1) 2.889 0.00771 0.00662 0.00321 C4'-H4 (3, -1) 2.837 0.00646 0.02133 0.0016 C7a-C5 (3, -1) 3.214 0.00764 0.02276 0.00321 PY ring (3, +1) 0.02116 0.1779 </td <td></td> <td>C5′…C4</td> <td>(3, -1)</td> <td>3.523</td> <td>0.00523</td> <td>0.01397</td> <td>0.0035</td>		C5′…C4	(3, -1)	3.523	0.00523	0.01397	0.0035
$\left[BPY \right]^* \left[BF_4 \right]^ BT \qquad \begin{array}{ccccccccccccccccccccccccccccccccccc$		C2′…C3	(3, -1)	3.224	0.00769	0.02143	0.0054
TS ring (3, +1) 0.03901 0.27120 [BPY]'[BF ₄] ⁻ - BT F3H2 (3, -1) 2.045 0.02068 0.06820 0.0179 F3H81 (3, -1) 2.377 0.01027 0.04058 0.0052 F1H3 (3, -1) 2.575 0.00662 0.02990 0.0011 F4H81 (3, -1) 2.308 0.01194 0.04573 0.0059 F4H7' (3, -1) 2.408 0.00957 0.03300 0.0037 F4S1' (3, -1) 2.889 0.00711 0.02404 0.0062 C3'C5 (3, -1) 3.215 0.00276 0.0032 C4'.+H4 (3, -1) 2.879 0.00646 0.02133 0.0016 C7a-C4 (3, -1) 2.817 0.00646 0.02276 0.0032 PY ring (3, +1) 0.02271 0.16179 [BPY]'[BF_4]^ DBT F4H2 (3, -1) 2.116 0.01774 0.06064 0.0145		PY ring	(3, +1)		0.02209	0.17742	
[BPY]*[BF4] ⁻ - BT F3H2 (3, -1) 2.045 0.02068 0.06820 0.0179 F3H81 (3, -1) 2.377 0.01027 0.04058 0.0052 F1H3 (3, -1) 2.500 0.00682 0.0290 0.0015 F1H7' (3, -1) 2.500 0.00662 0.0290 0.0021 F4H81 (3, -1) 2.308 0.01194 0.04573 0.0050 F4H7' (3, -1) 2.308 0.00771 0.02284 0.0019 H91S1' (3, -1) 2.837 0.00646 0.02133 0.0016 C3'C5 (3, -1) 2.837 0.00646 0.02276 0.0032 PY ring (3, +1) 0.02276 0.0032 T5 ring (3, +1) 0.02764 0.02276 0.0032 PY ring (3, +1) 0.0271 0.16179 [BPY]*[BF4] ⁻ - DBT F4H2 (3, -1) 2.216 0.00857 0.0302 0.0009 </td <td></td> <td>TS ring</td> <td>(3, +1)</td> <td></td> <td>0.03901</td> <td>0.27120</td> <td></td>		TS ring	(3, +1)		0.03901	0.27120	
[F3H81 (3, -1) 2.377 0.01027 0.04058 0.0052 F1H3 (3, -1) 2.500 0.00884 0.04017 0.0015 F1H7' (3, -1) 2.575 0.00662 0.0290 0.0037 F4H81 (3, -1) 2.308 0.01194 0.04573 0.0059 F4H7' (3, -1) 2.308 0.0071 0.02244 0.0016 C3C5 (3, -1) 2.889 0.00771 0.02404 0.0062 C3C5 (3, -1) 2.889 0.0071 0.0226 0.0032 C4H4 (3, -1) 2.837 0.00646 0.0213 0.0016 C7aC4 (3, -1) 3.214 0.00764 0.02276 0.0032 PY ring (3, +1) 0.02719 0.16179 T5 ring (3, +1) 0.0279 0.16179 [BPY]*[BF4] ⁻ - DBT F4H2 (3, -1) 2.216 0.00465 0.0302 0.0009 F2H	$[BPY]^+[BF_4]^ BT$	F3…H2	(3, -1)	2.045	0.02068	0.06820	0.0179
$[BPY]^{\dagger}[BF_4]^ DBT = \begin{bmatrix} F1H3 \\ F1H7' \\ (3, -1) \\ F4H81 \\ (3, -1) \\ (3, $		F3…H81	(3, -1)	2.377	0.01027	0.04058	0.0052
$[BPY]^{T}[BF_4]^{-} - DBT = \begin{bmatrix} F_4 - H81 & (3, -1) & 2.375 & 0.00662 & 0.0290 & 0.0021 \\ F_4 - H81 & (3, -1) & 2.308 & 0.01194 & 0.04573 & 0.0059 \\ F_4 - H7' & (3, -1) & 2.408 & 0.00957 & 0.03930 & 0.0037 \\ F_4 - S1' & (3, -1) & 2.889 & 0.00771 & 0.02404 & 0.0062 \\ G^3 - C5 & (3, -1) & 3.759 & 0.00347 & 0.01057 & 0.0006 \\ C4' - H4 & (3, -1) & 2.837 & 0.00646 & 0.02133 & 0.0016 \\ C7_a - C4 & (3, -1) & 2.214 & 0.00764 & 0.02276 & 0.0032 \\ PY ring & (3, +1) & \cdots & 0.02211 & 0.17759 & \cdots \\ TS ring & (3, +1) & \cdots & 0.02211 & 0.17759 & \cdots \\ BZ ring & (3, +1) & \cdots & 0.02079 & 0.16179 & \cdots \\ F4 - H81 & (3, -1) & 2.216 & 0.0174 & 0.06064 & 0.0145 \\ F4 - H81 & (3, -1) & 2.526 & 0.00827 & 0.03784 & 0.0101 \\ F2 - H3 & (3, -1) & 2.526 & 0.00827 & 0.03784 & 0.014 \\ F2 - H1' & (3, -1) & 2.526 & 0.00827 & 0.03784 & 0.014 \\ F2 - H1' & (3, -1) & 2.365 & 0.01029 & 0.03995 & 0.0052 \\ F3 - C2 & (3, -1) & 2.870 & 0.0100 & 0.03990 & 0.072 \\ F3 - H1' & (3, -1) & 2.365 & 0.01029 & 0.03987 & 0.0052 \\ F3 - H1' & (3, -1) & 2.365 & 0.01029 & 0.03987 & 0.0052 \\ F3 - H1' & (3, -1) & 2.365 & 0.01029 & 0.03987 & 0.0052 \\ F3 - H1' & (3, -1) & 2.365 & 0.01029 & 0.03987 & 0.0052 \\ F3 - H1' & (3, -1) & 2.369 & 0.00364 & 0.01700 & 0.0072 \\ F3 - H9' & (3, -1) & 2.369 & 0.00364 & 0.01700 & 0.0005 \\ F3 - H9' & (3, -1) & 2.369 & 0.00364 & 0.01700 & 0.0005 \\ F3 - H9' & (3, -1) & 2.305 & 0.0774 & 0.02512 & 0.0021 \\ C4 - C11' & (3, -1) & 2.305 & 0.00754 & 0.02489 & 0.0028 \\ PY ring & (3, +1) & \cdots & 0.02210 & 0.17737 & \cdots \\ TS ring & (3, +1) & \cdots & 0.02210 & 0.17737 & \cdots \\ TS ring & (3, +1) & \cdots & 0.02210 & 0.17737 & \cdots \\ TS ring & (3, +1) & \cdots & 0.02210 & 0.17373 & \cdots \\ TS ring & (3, +1) & \cdots & 0.02210 & 0.17373 & \cdots \\ TS ring & (3, +1) & \cdots & 0.02290 & 0.23886 & \cdots \\ BZ ring1 & (3, +1) & \cdots & 0.02097 & 0.16353 & \cdots \\ BZ ring2 & (3, +1) & \cdots & 0.02097 & 0.16353 & \cdots \\ BZ ring2 & (3, +1) & \cdots & 0.02097 & 0.16353 & \cdots \\ BZ ring2 & (3, +1) & \cdots & 0.02097 & 0.16353 & \cdots \\ BZ ring2 & (3, +1) & \cdots & 0.02097 & 0.16353 & \cdots \\ BZ ring2 & (3, +1) & \cdots & 0.02097 & 0.16353 & \cdots \\ BZ ring2 & (3, $		F1H3	(3, -1)	2.500	0.00884	0.04017	0.0015
$ \begin{bmatrix} F4H81 & (3, -1) & 2.308 & 0.01194 & 0.04573 & 0.0059 \\ F4H7' & (3, -1) & 2.408 & 0.00957 & 0.03930 & 0.0037 \\ F451' & (3, -1) & 3.315 & 0.00502 & 0.02284 & 0.0119 \\ H9151' & (3, -1) & 2.889 & 0.00771 & 0.02404 & 0.0062 \\ C3'C5 & (3, -1) & 3.759 & 0.00347 & 0.01057 & 0.0006 \\ C4'H4 & (3, -1) & 2.837 & 0.00646 & 0.02133 & 0.0016 \\ C7aC4 & (3, -1) & 3.214 & 0.00764 & 0.02276 & 0.0032 \\ PY ring & (3, +1) & & 0.02211 & 0.17759 & \\ B7 ring & (3, +1) & & 0.02079 & 0.16179 & \\ BPY]'[BF_4]^ DBT & F4H2 & (3, -1) & 2.116 & 0.01774 & 0.06064 & 0.0145 \\ F4H81 & (3, -1) & 2.212 & 0.01445 & 0.05040 & 0.0100 \\ F2H3 & (3, -1) & 2.526 & 0.00827 & 0.03784 & 0.0104 \\ F2H1' & (3, -1) & 2.526 & 0.00657 & 0.03002 & 0.0009 \\ F3H1' & (3, -1) & 2.365 & 0.01029 & 0.03987 & 0.0052 \\ F3H21 & (3, -1) & 2.365 & 0.01029 & 0.03987 & 0.0052 \\ F3H21 & (3, -1) & 2.369 & 0.00364 & 0.01700 & 0.0005 \\ F3H9' & (3, -1) & 2.369 & 0.00354 & 0.0395 & 0.0027 \\ F3H9' & (3, -1) & 2.369 & 0.00354 & 0.0395 & 0.0027 \\ F3H9' & (3, -1) & 2.369 & 0.00354 & 0.0395 & 0.0027 \\ F3H9' & (3, -1) & 2.369 & 0.00354 & 0.01700 & 0.0005 \\ F3H9' & (3, -1) & 2.369 & 0.00354 & 0.01700 & 0.0005 \\ F3H9' & (3, -1) & 2.369 & 0.00354 & 0.01700 & 0.0005 \\ F3H9' & (3, -1) & 2.369 & 0.00354 & 0.03818 & 0.0004 \\ C8'H91 & (3, -1) & 2.729 & 0.07741 & 0.02512 & 0.0021 \\ C4C11' & (3, -1) & 2.729 & 0.07741 & 0.02512 & 0.0021 \\ C4C11' & (3, -1) & 2.729 & 0.07741 & 0.02512 & 0.0021 \\ C4C11' & (3, -1) & 2.729 & 0.07741 & 0.02512 & 0.0021 \\ C4C11' & (3, -1) & 2.729 & 0.07741 & 0.02512 & 0.0021 \\ C4C11' & (3, -1) & 2.305 & 0.00754 & 0.02489 & 0.0028 \\ PY ring & (3, +1) & & 0.02210 & 0.17737 & \\ TS ring & (3, +1) & & 0.02210 & 0.17737 & \\ TS ring & (3, +1) & & 0.02210 & 0.17737 & \\ TS ring & (3, +1) & & 0.02210 & 0.17737 & \\ TS ring & (3, +1) & & 0.02210 & 0.16353 & \\ TS ring & (3, +1) & & 0.02097 & 0.16353 & \\ TS ring & (3, +1) & & 0.02097 & 0$		F1…H7′	(3, -1)	2.575	0.00662	0.02990	0.0021
F4H/' (3, -1) 2.408 0.0095/ 0.03930 0.0037 F4S1' (3, -1) 3.315 0.00502 0.02284 0.0019 H91S1' (3, -1) 2.889 0.00771 0.02404 0.0062 C3'C5 (3, -1) 3.759 0.00347 0.01057 0.0006 C4'H4 (3, -1) 2.837 0.00646 0.02133 0.0016 C7aC4 (3, -1) 2.837 0.00241 0.02276 0.0032 PY ring (3, +1) 0.0211 0.17759 TS ring (3, +1) 0.02079 0.16179 BZ ring (3, +1) 0.02079 0.16179 [BPY]*[BF4] ⁻ - DBT F4H2 (3, -1) 2.212 0.01445 0.05040 0.0104 F2H3 (3, -1) 2.526 0.00827 0.03002 0.0099 F3H1' (3, -1) 2.642 0.0657 0.03002 0.0095 F3H1' (3, -1) 2.870 0.01000 0.039990 0.0072 <t< td=""><td></td><td>F4…H81</td><td>(3, -1)</td><td>2.308</td><td>0.01194</td><td>0.04573</td><td>0.0059</td></t<>		F4…H81	(3, -1)	2.308	0.01194	0.04573	0.0059
$[BPY]^{*}[BF_4]^{-} - DBT = \begin{bmatrix} F451' & (3, -1) & 2.889 & 0.00771 & 0.02284 & 0.0019 \\ H9151' & (3, -1) & 2.889 & 0.00771 & 0.02404 & 0.0062 \\ C3'C5 & (3, -1) & 3.759 & 0.00347 & 0.01057 & 0.0006 \\ C4'H4 & (3, -1) & 2.837 & 0.00646 & 0.02133 & 0.0116 \\ C7aC4 & (3, -1) & 3.214 & 0.00764 & 0.02276 & 0.0032 \\ PY ring & (3, +1) & & 0.02211 & 0.17759 & \\ TS ring & (3, +1) & & 0.02279 & 0.16179 & \\ BZ ring & (3, +1) & & 0.02079 & 0.16179 & \\ BZ ring & (3, -1) & 2.116 & 0.01774 & 0.06064 & 0.0145 \\ F4H81 & (3, -1) & 2.212 & 0.01445 & 0.05040 & 0.0100 \\ F2H3 & (3, -1) & 2.526 & 0.00827 & 0.03784 & 0.0104 \\ F2H1' & (3, -1) & 2.526 & 0.00827 & 0.03784 & 0.0104 \\ F2H1' & (3, -1) & 2.365 & 0.01029 & 0.03987 & 0.0522 \\ F3C2 & (3, -1) & 2.870 & 0.01000 & 0.03990 & 0.0072 \\ F3H1' & (3, -1) & 2.880 & 0.00364 & 0.01700 & 0.0005 \\ F3H9' & (3, -1) & 2.369 & 0.00334 & 0.0395 & 0.0027 \\ F3H9' & (3, -1) & 2.369 & 0.00364 & 0.01700 & 0.0005 \\ F3H9' & (3, -1) & 2.729 & 0.00741 & 0.02512 & 0.0021 \\ C4'C11' & (3, -1) & 3.205 & 0.00754 & 0.02489 & 0.0021 \\ C4'C11' & (3, -1) & 3.205 & 0.00754 & 0.02489 & 0.0021 \\ C4'C11' & (3, -1) & 3.205 & 0.00754 & 0.02489 & 0.0021 \\ C4'C11' & (3, -1) & 3.205 & 0.00754 & 0.02489 & 0.0021 \\ C4'C11' & (3, -1) & 3.205 & 0.00754 & 0.02489 & 0.0021 \\ C4'C11' & (3, -1) & & 0.02210 & 0.17737 & \\ TS ring & (3, +1) & & 0.02209 & 0.3386 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 & (3, +1) & & 0.02097 & 0.16353 & \\ BZ ring2 &$		F4H7/	(3, -1)	2.408	0.00957	0.03930	0.0037
[BPY]*[BF4]" - DBT F4H2 (3, -1) 2.889 0.007/1 0.02404 0.0002 C3'C5 (3, -1) 3.759 0.00347 0.01057 0.0006 C4'H4 (3, -1) 2.837 0.00646 0.02133 0.0016 C7aC4 (3, -1) 3.214 0.00764 0.02276 0.0032 PY ring (3, +1) 0.02111 0.17759 BZ ring (3, +1) 0.02079 0.16179 [BPY]*[BF4]" - DBT F4H2 (3, -1) 2.212 0.01445 0.05040 0.0100 F2H3 (3, -1) 2.526 0.00827 0.03784 0.0014 F2H1' (3, -1) 2.642 0.00657 0.03002 0.0099 F3H1' (3, -1) 2.870 0.01000 0.03990 0.0072 F3H2 (3, -1) 2.880 0.00364 0.01700 0.0005 F3H2 (3, -1) 2.369 0.00935 0.03818 0.0040 <td></td> <td>F451</td> <td>(3, -1)</td> <td>3,315</td> <td>0.00502</td> <td>0.02284</td> <td>0.0019</td>		F451	(3, -1)	3,315	0.00502	0.02284	0.0019
G4*-H4 (3, -1) 2.837 0.0047 0.0157 0.0007 G4*-H4 (3, -1) 2.837 0.0046 0.02133 0.0016 C7a-C4 (3, -1) 3.214 0.00764 0.02276 0.0032 PY ring (3, +1) 0.02111 0.17759 TS ring (3, +1) 0.02079 0.16179 BZ ring (3, +1) 0.02079 0.16179 [BPY]*[BF4] ⁻ - DBT F4H2 (3, -1) 2.212 0.01445 0.05040 0.0104 F2H1 (3, -1) 2.526 0.00827 0.03002 0.0009 F3H1' (3, -1) 2.365 0.01029 0.03987 0.0052 F3C2 (3, -1) 2.870 0.01000 0.03990 0.0072 F3H81 (3, -1) 2.880 0.00364 0.01700 0.00052 F3H9' (3, -1) 2.869 0.00355 0.03818 0.0040 C8'H91		C3' C5	(3, -1)	2.889	0.00771	0.02404	0.0002
C7a-C4 (3, -1) 3.214 0.00764 0.02276 0.0032 PY ring (3, +1) 0.02211 0.17759 TS ring (3, +1) 0.03735 0.25561 BZ ring (3, +1) 0.02079 0.16179 [BPY]*[BF4] ⁻ – DBT F4H2 (3, -1) 2.116 0.01774 0.06064 0.0145 F4H81 (3, -1) 2.212 0.01445 0.05040 0.0100 F2H3 (3, -1) 2.526 0.00827 0.03984 0.0014 F2H1' (3, -1) 2.642 0.00657 0.03002 0.0099 F3H1' (3, -1) 2.365 0.01029 0.03887 0.0052 F3H2 (3, -1) 2.870 0.01000 0.03990 0.0072 F3H81 (3, -1) 2.369 0.00938 0.03995 0.0027 F3H9' (3, -1) 2.369 0.00935 0.03818 0.0040 C8''H91 (3, -1) 2.729 0.00741 0.02512 0.0021		C4'H4	(3, -1)	2 837	0.00547	0.02133	0.0000
$\begin{bmatrix} BPY \end{bmatrix}^* [BF_4]^ DBT & F4 \cdots H2 & (3, +1) & \cdots & 0.02211 & 0.17759 & \cdots \\ BZ ring & (3, +1) & \cdots & 0.02079 & 0.16179 & \cdots \\ BZ ring & (3, +1) & \cdots & 0.02079 & 0.16179 & \cdots \\ F4 \cdots H2 & (3, -1) & 2.116 & 0.01774 & 0.06064 & 0.0145 \\ F4 \cdots H81 & (3, -1) & 2.212 & 0.01445 & 0.05040 & 0.0100 \\ F2 \cdots H3 & (3, -1) & 2.526 & 0.00827 & 0.03784 & 0.0014 \\ F2 \cdots H1' & (3, -1) & 2.642 & 0.00657 & 0.03002 & 0.0009 \\ F3 \cdots H1' & (3, -1) & 2.365 & 0.01029 & 0.03987 & 0.0052 \\ F3 \cdots H2' & (3, -1) & 2.870 & 0.01000 & 0.03990 & 0.0072 \\ F3 \cdots H81 & (3, -1) & 2.880 & 0.00364 & 0.01700 & 0.0005 \\ F3 \cdots H91 & (3, -1) & 2.880 & 0.00364 & 0.01700 & 0.0005 \\ F3 \cdots H91 & (3, -1) & 2.369 & 0.00353 & 0.03818 & 0.0040 \\ C8' \cdots H91 & (3, -1) & 2.729 & 0.00741 & 0.02512 & 0.0021 \\ C4 \cdots C11' & (3, -1) & 3.205 & 0.00754 & 0.02489 & 0.0028 \\ PY ring & (3, +1) & \cdots & 0.02210 & 0.17737 & \cdots \\ TS ring & (3, +1) & \cdots & 0.02210 & 0.17737 & \cdots \\ TS ring & (3, +1) & \cdots & 0.02210 & 0.17737 & \cdots \\ BZ ring1 & (3, +1) & \cdots & 0.02094 & 0.16305 & \cdots \\ BZ ring2 & (3, +1) & \cdots & 0.02097 & 0.16353 & \cdots \\ BZ ring2 & (3, +1) & \cdots & 0.02097 & 0.16353 & \cdots \\ \end{bmatrix}$		C7aC4	(3, -1)	3 2 1 4	0.00764	0.02276	0.0032
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		PY ring	(3, +1)		0.02211	0.17759	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		TS ring	(3, +1)		0.03735	0.25561	
$ \begin{bmatrix} BPY \end{bmatrix}^* \begin{bmatrix} BF_4 \end{bmatrix}^ DBT & F4 \cdots H2 & (3, -1) & 2.116 & 0.01774 & 0.06064 & 0.0145 \\ F4 \cdots H81 & (3, -1) & 2.212 & 0.01445 & 0.05040 & 0.0100 \\ F2 \cdots H3 & (3, -1) & 2.526 & 0.00827 & 0.03784 & 0.0014 \\ F2 \cdots H1' & (3, -1) & 2.642 & 0.00657 & 0.03002 & 0.0099 \\ F3 \cdots H1' & (3, -1) & 2.365 & 0.01029 & 0.03987 & 0.0522 \\ F3 \cdots C2 & (3, -1) & 2.870 & 0.0100 & 0.03990 & 0.0072 \\ F3 \cdots H81 & (3, -1) & 2.445 & 0.00938 & 0.03995 & 0.0027 \\ F3 \cdots H9' & (3, -1) & 2.369 & 0.00364 & 0.01700 & 0.0005 \\ F3 \cdots H9' & (3, -1) & 2.369 & 0.00354 & 0.01700 & 0.0005 \\ F3 \cdots H9' & (3, -1) & 2.369 & 0.00741 & 0.02512 & 0.0021 \\ C4 \cdots C11' & (3, -1) & 2.729 & 0.00741 & 0.02512 & 0.0021 \\ C4 \cdots C11' & (3, -1) & 3.205 & 0.00754 & 0.02489 & 0.0028 \\ PY ring & (3, +1) & \cdots & 0.02210 & 0.17737 & \cdots \\ TS ring & (3, +1) & \cdots & 0.03529 & 0.23886 & \cdots \\ BZ ring1 & (3, +1) & \cdots & 0.02207 & 0.16353 & \cdots \\ BZ ring2 & (3, +1) & \cdots & 0.02097 & 0.16353 & \cdots \\ \end{bmatrix} $		BZ ring	(3, +1)		0.02079	0.16179	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	[BPY] ⁺ [BF₄] [−] – DBT	F4H2	(3, -1)	2.116	0.01774	0.06064	0.0145
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1 11 41	F4…H81	(3, -1)	2.212	0.01445	0.05040	0.0100
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		F2…H3	(3, -1)	2.526	0.00827	0.03784	0.0014
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		F2…H1′	(3, -1)	2.642	0.00657	0.03002	0.0009
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		F3…H1′	(3, -1)	2.365	0.01029	0.03987	0.0052
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		F3…C2	(3, -1)	2.870	0.01000	0.03990	0.0072
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		F3…H81	(3, -1)	2.445	0.00938	0.03995	0.0027
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		F3…H101	(3, -1)	2.880	0.00364	0.01700	0.0005
C8'H91 (3, -1) 2.729 0.00741 0.02512 0.0021 C4C11' (3, -1) 3.205 0.00754 0.02489 0.0028 PY ring (3, +1) 0.02210 0.17737 TS ring (3, +1) 0.03529 0.23886 BZ ring1 (3, +1) 0.02094 0.16305 BZ ring2 (3, +1) 0.02097 0.16353		F3…H9′	(3, -1)	2.369	0.00935	0.03818	0.0040
C4C11' (3, -1) 3.205 0.00754 0.02489 0.0028 PY ring (3, +1) 0.02210 0.17737 TS ring (3, +1) 0.03529 0.23886 BZ ring1 (3, +1) 0.02094 0.16305 BZ ring2 (3, +1) 0.02097 0.16353		C8'H91	(3, -1)	2.729	0.00754	0.02512	0.0021
FT ring (3, +1) 0.02210 0.17/37 TS ring (3, +1) 0.03529 0.23886 BZ ring1 (3, +1) 0.02094 0.16305 BZ ring2 (3, +1) 0.02097 0.16353		C4…CII′	(3, -1)	3.205	0.00/54	0.02489	0.0028
BZ ring1 (3, +1) 0.02094 0.16305 BZ ring2 (3, +1) 0.02097 0.16353		r i illig TS ring	(3, +1) (3 ±1)		0.02210	0.17/3/	
BZ ring2 (3, +1) ···· 0.02097 0.16353 ···		R7 ring	$(3, \pm 1)$		0.03323	0.23000	
		BZ ring2	(3, +1)		0.02097	0.16353	

the bond critical points (BCPs). Covalent bonding is characterized by $\bigtriangledown^2 \rho < 0$, while closed-shell bonding interaction is characterized by density depletion in the region of contact of the two atoms and $\bigtriangledown^2 \rho > 0$. Electron density (ρ) is used to describe the strength of a bond, a stronger bond being associated with a larger value of ρ . The bond characteristics for the TS, BT, DBT, [BPY]⁺[BF4]⁻, BPY]⁺[BF4]⁻, DBT

were provided in Table 2. The evidence of interactions according to the AIM approach is the existence of a bond path between two atoms and the existence of a bond critical point (BCP) [29,30]. From the values of electron density listed in Table 2, it can be concluded that interactions between [BPY]⁺[BF₄]⁻ and TS, BT, DBT are all closed-shell systems in terms of positive values of $\bigtriangledown^2 \rho$. A second AIM criterion to define hydrogen bond is that



Fig. 6. Regression plots between the F···H distances (Å) and the corresponding values of $\ln(\rho_b)$ of (a) $[BPY]^*[BF_4]^-$, (b) $[BPY]^*[BF_4]^- - TS$, (c) $[BPY]^*[BF_4]^- - BT$, and (d) $[BPY]^*[BF_4]^- - DBT$.

electron density (ρ) and the Laplacian of electron density ($\nabla^2 \rho$) at BCP must be within 0.002 ~ 0.035 au and 0.024 ~ 0.139 au ranges, respectively [29,30]. These values are within the commonly accepted values, indicating the occurrence of hydrogen bonding interactions in these systems. Bond critical points are F4…H2', F4…S1, F1…H2', S1…H91, C5'…C4, C2'…C3 in [BPY]⁺[BF₄]⁻ – TS, F1…H7', F4…S1', H91…S1', C3'…C5, C4'…H4, C7a…C4 in [BPY]⁺[BF₄]⁻ – BT, and F2…H1', F3…H1', F3…H9', C8'…H91, C4…C11' in [BPY]⁺[BF₄]⁻ – DBT, demonstrating that $\pi \cdots \pi$ interactions occur between [BPY]⁺[BF₄]⁻ and TS, BT, DBT. The tendency of sulfur-involved interactions between TS, BT, DBT and [BPY]⁺[BF₄]⁻ is BT > TS > DBT, in agreement with NBO analyses.

As can be seen in Table 2, the values of electron density for hydrogen bonding interactions in all configurations decrease with increasing interacting distances. This decrease in electron density in BCPs can be ascribed to a decrease in interaction energy. For hydrogen bonds, there is a correlation between the interaction distances and topological parameters at the BCPs [31,32]. Here, the existence of such a correlation has been checked for configurations [BPY]⁺[BF₄]⁻, [BPY]⁺[BF₄]⁻ – TS, [BPY]⁺[BF₄]⁻ – BT, and [BPY]⁺[BF₄]⁻ – DBT. Fig. 6 presents the linear correlation between F···H distances and their corresponding ln(ρ_b) values in [BPY]⁺[BF₄]⁻ – DBT, [BPY]⁺[BF₄]⁻ – DBT, confirming the dependence of hydrogen bonding strength on their distances.

5. Conclusions

In order to understand the nature of the interactions between N-butylpyridinium tetrafluoroborate ([BPY]⁺ $[BF_4]^-$) and thiophene (TS), benzothiophene (BT), dibenzothiophene (DBT), the structures of [BPY]⁺[BF₄]⁻, $[BPY]^{+}[BF_{4}]^{-} - TS, [BPY]^{+}[BF_{4}]^{-} - BT, and [BPY]^{+}[BF_{4}]^{-}$ - DBT were optimized using density functional theory, and the most stable geometries were discussed in terms of NBO and AIM analyses. The bond length, electron density at bond critical points and Wiberg bond index (WBI) were obtained. The results show that the multiple intermolecular hydrogen bonds play an important role in stabilizing the [BPY]⁺[BF₄]⁻ pair. NBO and AIM analyses proved that the $\pi \cdots \pi$ and hydrogen bonding interactions occur between [BPY]⁺[BF₄]⁻ and TS, BT, DBT. The order of the involved hydrogen interactions between $[BPY]^+[BF_4]^-$ and TS, BT, DBT is DBT > BT > TS in terms of WBI.

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Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at http://dx.doi.org/10.1016/j. crci.2013.05.015.

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