



Account/Revue

Stereochemistry of nitrogen E lone pair in NH₃E, NOFE, N₂O₃E₂, AgNO₂E, and NCl₃E

Jean Galy^a, Guillaume Couégnat^a, Eladio Vila^b, Samir F. Matar^{c,*}^a CNRS–LCTS, Université de Bordeaux, 33600 Pessac, France^b CSIC–ICMM, Cantoblanco, 28049 Madrid, Spain^c CNRS–ICMCB, Université de Bordeaux, 33600 Pessac, France

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ABSTRACT

We revisit nitrogen based simple fundamental molecules in their solid state structures, with the purpose of casting new light on the stereoactivity of valence lone pairs (LPs)—formally N(2s²)—in different crystal geometries. Based on coupled investigations of crystal chemistry and ab initio DFT calculations providing the electron localization function (ELF), LP behavior is analyzed precisely by finding its position E, orientation and “volume of influence” which consists in an electronic cloud generated around the so-called ‘centroïd’ Ec of the electronic doublet. The results show the paramount importance of the role of N(2s²) LP in the crystal network architecture through the different case studies pertaining to ammonia (NH₃), nitrosyl fluoride (NOF), nitrosyl nitrite (N₂O₃), silver nitrite (AgNO₂), and nitrogen trichloride (NCl₃). An unexpected direct ionic interaction between [NO]⁺ or Ag⁺ and the centroïd Ec of the [NO₂Ec][−] nitrite group has been evidenced in N₂O₃E₂ and AgNO₂, respectively.

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1. Introduction

Several elements of the periodic table exhibit a peculiar electronic structure when they retain their last s² electron pair, not involved in the bonding, from {He}2s² up to {Xe}4f¹⁴5d¹⁰6s² for Po⁴⁺; such elements characterized by their lone pair E ns² (2 ≤ n ≤ 6) are designated hereafter by M*. They show generally a one sided coordination to their ligands 2 ≤ CN ≤ 5, E completing a polyhedron which surrounds M* up to CN = 6. In molecular chemistry, the Valence Shell Electron Pair Repulsion (VSEPR) model has been well established [1,2].

In solid state chemistry, M* elements give a very rich family of compounds with crystal structures always revealing original characteristics with empty channels, thick layers separated by impenetrable volumes excluding any

other atoms thanks to E with its peculiar stereochemistry. In this field, for oxides, fluorides and oxyfluorides, an original approach was proposed by considering E as having a volume, non-compressible and analogous to oxygen or fluorine anions; the so-called “volume of influence” likely contributes to hcp or ccp packing [3].

A simple test was done to control the reality of E volume occupancy by calculating Vr, a reduced volume by dividing V cell volume by the Z number of O (or F) as well as E contained in the cell. As a consequence, approximate coordinates of E were obtained on the basis of the average E–O ~ O–O (or F) distance to the one sided coordinated atoms, such geometric calculation allowing to estimate M*–E distance and direction for these M* E units [4].

Recently, a new approach of M* and E stereochemistry of 6s² elements by a joint crystal chemistry and ab initio analyses has been developed by two of us for Tl^I, Pb^{II}, Bi^{III} and Po^{IV}, covering all polyhedral M*X_nE possibilities essentially for oxides, fluorides and oxyfluorides [5,6]. In

* Corresponding author.

E-mail address: Samir.Matar@icmcb.cnrs.fr (S.F. Matar).

most of the environments except for octahedral and cubic ones, E volume departs from spherical.

The localization and size of E and its volume of influence were clearly specified. If VSEPR general rules are followed, LP–LP repulsion stronger than LP–BP, must be strictly applied in close M* bonding because there are many examples where LP packing participates in network building by their various associations in tetrahedral chains or double layers. In these series of M* elements, positions and sizes of E lone pairs have been defined. It was surprising but clearly established that the widest E belongs to Tl⁺, its electronic doublet 6s² generating an electronic cloud (its sphere of influence) with a radius: $r_{Tl^+} = 1.40 \text{ \AA}$.

Our aim in this work is to focus on the nitrogen lone pair, formally 2s², with the objective of precisely determining its location with respect to its carrier atom, i.e. its Ec centroid. We also aim at defining the LP form, size and coordinates of its volume of influence E, which is in fact the electronic cloud generated by Ec, and the final geometry of NX_nE. For this purpose, the stereochemistry of four compounds has been revisited and analyzed in the light of quantum density functional theory (DFT) [7,8] completed by fine analyses of electron localization functions (ELF) [9]: NH₃E, ammonia; NOFE, oxyfluoride; N₂O₃E₂, oxide; AgNO₂, silver nitrite and NCl₃E, nitrogen trichloride. For details on the methodology and the theory regarding DFT and ELF, the reader is kindly referred to the Annex for a brief overview and former accounts on the topic [5,6].

2. NH₃E

Ammonia is a colorless gas, lighter than air, easily solidified below 195 K.

2.1. Crystal structure

As shown for the first time in 1925, NH₃ crystallizes in the cubic system; its unit cell contains four molecules [10]. These molecules are in a nearly perfect cubic close-packing. N atoms are located on the threefold rotation axis (4a Wyckoff site) and hydrogen atoms in 12b sites; they build typical NH₃ tetrahedral isolated molecules. More recently, the refinement of the structure was published together with its electron density distribution [11]. These last crystal data are summarized in Table 1.

Based on these X-ray data, a perspective view of this molecular structure is presented in Fig. 1 in which, as a first approximation, a nitrogen lone pair E has been added to get

a general picture. Nitrogen sits on A3 threefold rotational axis and is bonded to three hydrogen atoms, being one side coordinated and making a trigonal pyramid NH₃. Owing to this symmetry, the E lone pair which, in such tetrahedral coordination, is actually an sp³ hybrid orbital, achieves a quasi-perfect model of CN = 3 + 1 tetragonal geometry for NH₃E; E was set up on A3 crystal axis using a dedicated software [12] with an approximate H–E distance of ~1.6Å, giving N–E ~ 0.96Å.

In their detailed X-ray crystal structure analyses completed by some ab initio calculations, the authors [11] have particularly emphasized the problem of N–H bending and incidentally indicated lone pair direction along A3 with N–E = 1 Å. E lone pair must be influential on N–H bond bending as well as on ∠HNH angle evolution even if other solutions are preferred. Nevertheless, the E stereo-structural effect is of paramount importance as shown for 6s² lone pairs replaced in their structural environment [5,6].

2.2. DFT and electron localization function (ELF)

Based on accurate high Brillouin zone integration, the ELF's are first used to produce the three-dimensional 3D isosurfaces shown in Fig. 2. The tetramolecular NH₃E structure is then shown with a close arrangement to that shown in Fig. 1 then the 3D ELF's in panel b) clearly highlight the E development observed on top of nitrogen.

To refine lone pair localization, precise sections through the electron localization function ELF were of paramount interest in order to define an Ec centroid position of the electron doublet on one hand, and the volume size of the electronic cloud generated by Ec centered in E on the other hand. For this purpose, electronic localization sections of NH₃E–ELF defined by (H–N–H) and (H–N–A3) planes have been realized using dedicated software built by one of us [13]. They are reported in Fig. 3. Red, green and blue areas correspond to strong, free electron gas and zero localizations, respectively. This color scheme is respected in all ELF projections.

As expected, the HNH section shows one of the faces of the NH₃ trigonal pyramid with N–H = 1.010 Å and the ∠HNH = 109.8°. Therefore, there also appears a slice of the electronic cloud E. Isodensity curves around H atom show in their center their maximum i.e. 0.99.

The following section, which contains the threefold rotation axis of the molecule, reveals precisely the lone pair:

Table 1
NH₃E crystal and DFT data [11].

NH ₃ E – Cubic, space group P2 ₁ 3 (N° 198), T = 160 K									
a (Å)	b (Å)	c (Å)	V (Å ³)	Z	Vr(H,E) (Å ³)				
5.1305	5.1305	5.1305	135.05	4	8.4				
5.1328	5.1328	5.1328	135.23	4	8.5				
Interatomic distances (Å) and angles (°)									
N–H	1.010	H–H	1.646	∠HNH	109.2				
Data from DFT-ELF analyses									
N–H	1.030	H–H	1.662	∠HNH	107.5	N 0150Na,b,c	3.320	Ha 0150Hb,c	2.559
N–Ec	0.79	Ec–H	1.51	∠HNEc	111.4	Ec 0150Ha,b,c	1.79	H 0150Ha	2.342
N–E	0.65	E–H	1.40	∠HNE	111.4	E 0150Ha,b,c	1.87	H 0150Hb	2.758

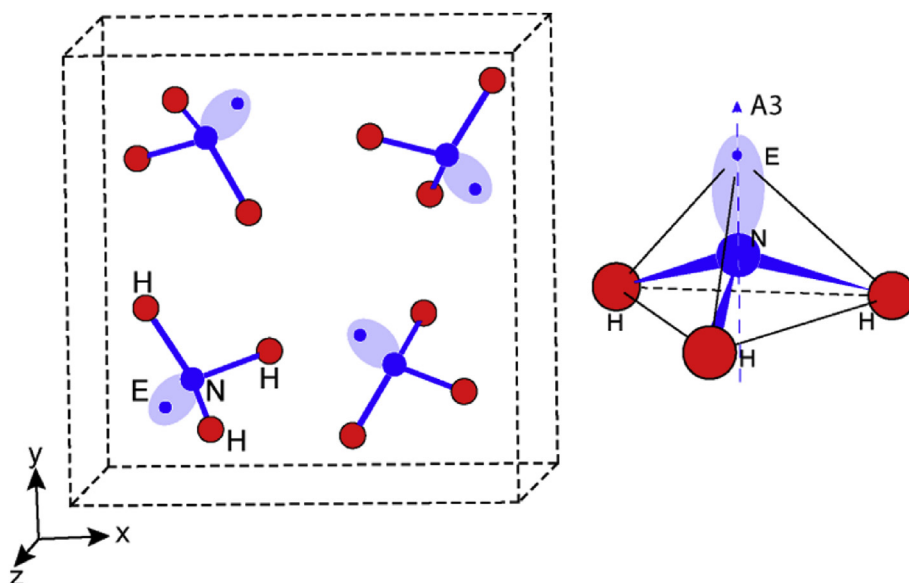


Fig. 1. Perspective view of the NH_3E molecular structure; E lone pair is represented schematically by an elongated ellipse whose axis indicates the N–E direction along threefold rotation axis (A3) and a blue dot indicates the center of its volume of influence. On the right hand side, the tetrahedral geometry of $[\text{NH}_3\text{E}]$ is shown, with N atoms enclosed in a tetrahedron built by the three H atoms making an equilateral base and E situated at the apex. N and E sit on the A3 axis.

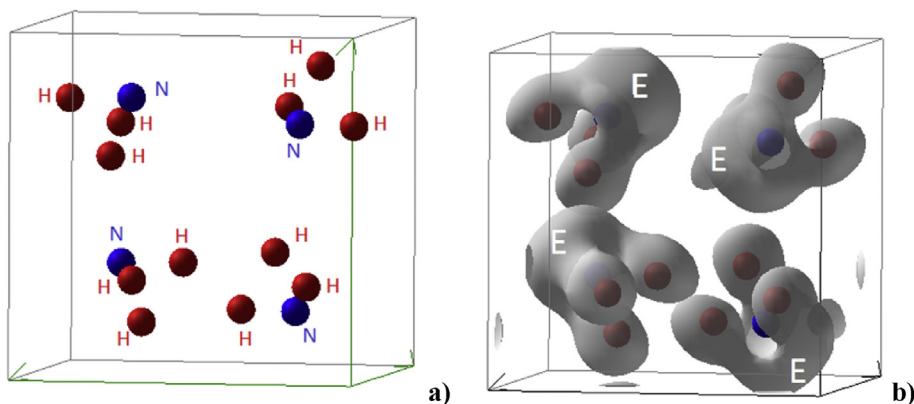


Fig. 2. Tetramolecular NH_3E structure from ELF calculation reproducing the schematic view in Fig. 1 (a) and the corresponding three-dimensional 3D ELF isosurfaces highlighting E volume development (b).

- the volume of E, spherical with its center onto A3 axis of course delimited in the vicinity of N atom, is roughly enclosed by the dotted blue circle with $\phi = 1.45 \text{ \AA}$ ($r_E = 0.73 \text{ \AA}$) and even appears bigger than H ions;
- E isodensity curves more spread out indicate a maximum around 0.97 which is attributed to centroid Ec (little red circle);
- like in other cases, the center of E volume (little blue circle) is somewhat displaced towards N ($\text{Ec}-\text{E} = 0.14 \text{ \AA}$);

Then, NH_3E shows the classical geometry where H and E define a tetrahedral geometry including N atoms as represented in (Fig. 4 left), where N and E are shown with radii, $r_N \sim 0.38 \text{ \AA}$ and $r_E = 0.73 \text{ \AA}$, the hydrogen atoms being a smaller size for the sake of clear representation. This drawing shows that E sitting above the N–H bonds has an

electrostatic potential perturbing the N–H bond: i) by eventually expanding N–H by LP–BP repulsion and/or lowering the $\angle \text{H-N-H}$ angle; ii) by acting simultaneously on N–H bonding electrons and H atoms therefore with different repulsive forces then bending N–H bond.

Fig. 4 (right) shows that three other NH_3E molecules surrounding each NH_3E , one hydrogen of each (Ha, Hb, and Hc) designing with the base of the former molecule, a distorted trigonal antiprism. Nitrogen and its lone pair E appear encapsulated in an H octahedron shaded in yellow in Fig. 4; pertinent distances are given in Table 1. This description is in agreement with the fact that E, the center of the electronic cloud which is largely bigger than an Ec electron doublet, is sensible to Ha,b,c repulsive effect. Consequently it is slightly pushed towards N; then a short $\text{Ec}-\text{E}$ distance has been noticed: 0.14 \AA .

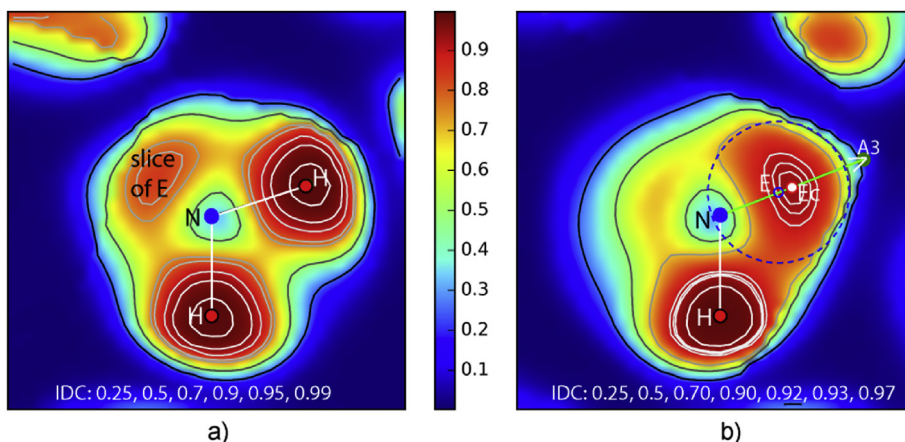


Fig. 3. a) Section of the DFT–ELF density by the plane (HNH), one face of the NH_3 trigonal pyramid; worthy to note opposite to N–H bonds a weak density which is a slice cut in electronic cloud volume of lone pair E. The density around H atoms reaches the maximum value (0.99). b) This second section based on one H and N includes also the A3 rotation axis, showing the huge E lone pair volume. Isodensity curves permit to detect a maximum in E volume, clearly evidenced with its maximum (little red circle). The blue dotted circle delimitates lone pair electronic cloud with its E center (little blue circle).

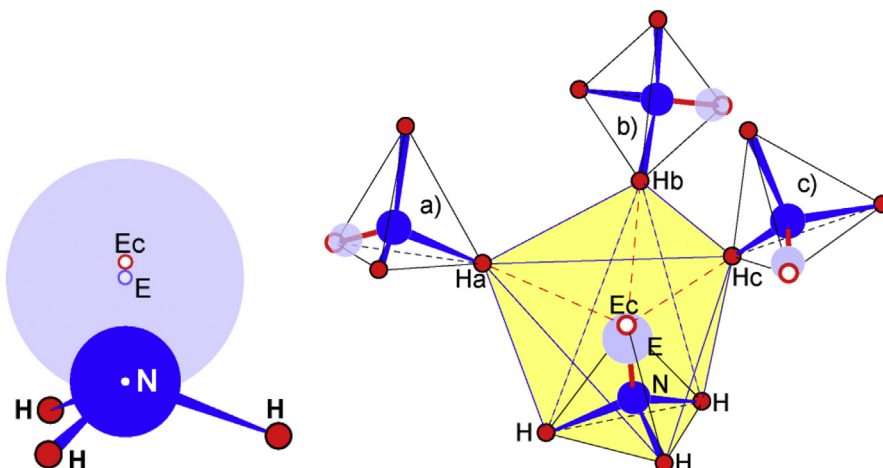


Fig. 4. Schematic drawing of the NH_3E molecule (left hand side) and immediate surroundings of NH_3E by three other molecules (a, b, c) making a large N_4 tetrahedron (right hand side). Hydrogen atoms Ha, Hb and Hc build a distorted triangular antiprism with the ones of the base of the trigonal MH_3E (shaded in yellow) encapsulating the unit NEEc .

3. NOFE or $[\text{NOE}]^+\text{F}^-$, nitrosyl fluoride

Nitrosyl fluoride was prepared by the interaction of NO with KF leading to the oxyfluoride NOF [14]. Then it was solidified below 150 K, re-crystallized and a single crystal maintained at 123 K for X-ray data collection. The NOF crystal structure belongs to an orthorhombic system. The crystallographic data are provided in Table 2.

3.1. Crystal structure

Before drawing the detailed molecular packing of this oxide fluoride, an approximate position of the E lone pair associated with the nitrogen atom and its resulting shape are shown in Fig. 5 (therefore with ultimate values). The figure also shows a perspective view of the crystal network (left hand side) and the sketch of the molecular entity (right hand side).

Table 2
NOFE crystal and DFT data [14].

NOFE – Orthorhombic, space group $P2_12_12_1$ ($N^\circ 19$), $T = 123$ K.						
a (Å)	b (Å)	c (Å)	V (Å ³)	Z	$V(\text{O,F,E})$ (Å ³)	
4.1099	4.3910	10.202	184.11	4	15.3	
4.1838	4.4310	10.4134	193.05	4	16.1	
Interatomic distances (Å) and angles (°) – crystal.						
N–F	1.651	O···O in ils	3.159	$\angle \text{ONF}$	109.7	
N–O	1.084	O···F in ils	3.308	$\angle \text{ONE}$	134.2	
O–F	2.260			$\angle \text{FNE}$	116.0	
N–E	0.65	E–O	1.61	E–F	2.02	
E–Fa	2.52	E–Ea, Eb	2.92	E–Fb, c	3.01	
ils: inter layer space						
Data from DFT-ELF analyses						
N–F	1.639	N–E	0.66	E–O	1.66	$\angle \text{ONF}$ 109
N–O	1.139	N–Ec	0.70	E–F	2.02	$\angle \text{ONE}$ 134
O–F	2.293	Ec–E	0.13	r_E	0.78	$\angle \text{FNE}$ 117
E ellipsoid parameters of: $a = 0.75$ Å, $b = 0.67$ Å, $c = 0.97$ Å						

The NOFE molecule is a typical triangular molecule M^*X_2E (Fig. 5 right hand side). The N–F bond is longer in NF_3E by 0.28 Å and the angle $\angle FNO = 109.7^\circ$ is larger than $\angle FNF = 102.2^\circ$. Therefore, it was difficult to propose a value for the N–E distance and also for $\angle FNE$ or $\angle ONE$ angles. This problem is solved hereafter by DFT-ELF analyses.

The molecules packed along [100] are set up in planes parallel to (001). They delimitate two empty interlayers spaces (ils), one bordered by lone pairs (1.46 Å) centered at $z = 0$ and $1/2$ (shaded in pale blue color) and the second by oxygen atoms centered in $1/4$ and $3/4$ (2.09 Å) (pale red color). The lone pairs E directed towards blue ils planes, point to each other making a double layer of lone pairs separating NOF molecules. Interactions $E \cdots E_{a,b}$ and $E \cdots F_{a,b,c}$ marked by dashed red lines organize the packing of the NOFE molecules along the three directions making a double layer associated by E interactions with F and E in which NOFE molecules are packed and separated by 2.09 Å then associated by Van der Waals bonding.

3.2. ELF calculations

The calculated ELF at high precision is plotted in Fig. 6 along a projection close to Fig. 5 qualitative description. A slice crossing N–O–F is shown in panel a). The dominant blue zone around the NOF moiety clearly highlights the molecular character of NOF. Then within the molecule, red areas around the chemical constituents point to the electron localization and to the chemical bonding between them. Notice however the continuous red areas within NO whereas a discontinuity/separation is clearly observed between N and F. On top of N the red ELF highlights the LP. In panel b) the 3D isosurfaces are shown, highlighting further the LP (E) development. In panel c) at large isosurface values a clear observation of E (N) is exhibited spatially in the form of covering cloud.

We now turn to a more precise analysis of the ELF. Sections containing a plane with a NOF molecule and another one perpendicular to it allow appreciating the real

chemical nature of this oxide fluoride by showing clearly three zones (Fig. 7 left):

- the angular ONF geometry being drawn, a consequent cloud of electronic localization is noticed, opposed to N one sided coordination, which is of course the remarkable trace of the lone pair E completing the triangular geometry of NOFE with N found inside the OEF triangle;
- the $N \cdots O$ bond with 1.14 Å magnitude indicates a strong bond intermediate between a triple bond (1.10 Å) a double bond (1.20 Å) and shows in its center a maximum density (~ 0.80) slightly blown off towards F side by E repulsive influence;
- then we note that $N \cdots F$ line does not show any electronic concentration, indicating an $N \cdots F$ ionic bonding with a large distance of 1.65 Å [18]. Consequently NOFE appears as an ionic molecule with a nitrosyl $[NOE]^+$ cation and $[F]^-$ as a counter anion.

Then it was important to analyze in detail the cloud around the lone pair to appreciate its behavior. Isodensity curves show that there is a clear maximum, which is attributed to the presence of Ec centroid. Alike in all the previous investigations [5,6], Ec generates around it an electronic cloud, the so-called sphere of influence; its E center can be slightly displaced compared to Ec. Therefore, in such a case, there is no symmetry axis favoring spherical geometry; then E is obviously deformed, its volume been assimilated to an ellipsoid, dotted blue traces in Fig. 7 (left) from which the ellipse parameters were deduced: $a = 0.75$ Å and $b = 0.67$ Å in the section plane NOF and in the perpendicular plane; the third parameter $c = 0.97$ Å Fig. 7 (right).

An average sphere of influence for E is derived with $r_E = 0.78$ Å its center being displaced at 0.13 Å from Ec. This analysis provides also the angle values: $\angle EcNF = 107^\circ$, $\angle ENF = 117^\circ$, $\angle ENO = 134^\circ$, $\angle ONF = 109^\circ$. It is worth noting how F^- anion pushes and deforms the E

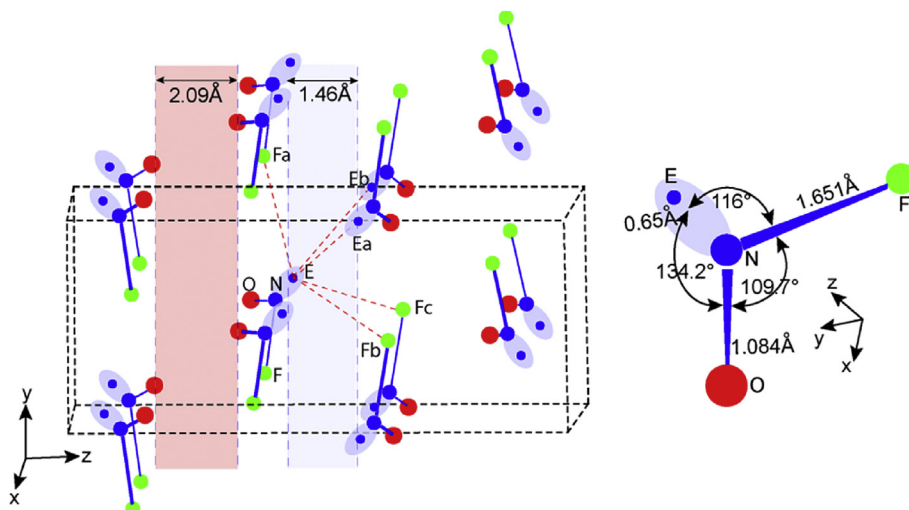


Fig. 5. Perspective view of the NOFE crystal framework and NOFE molecule.

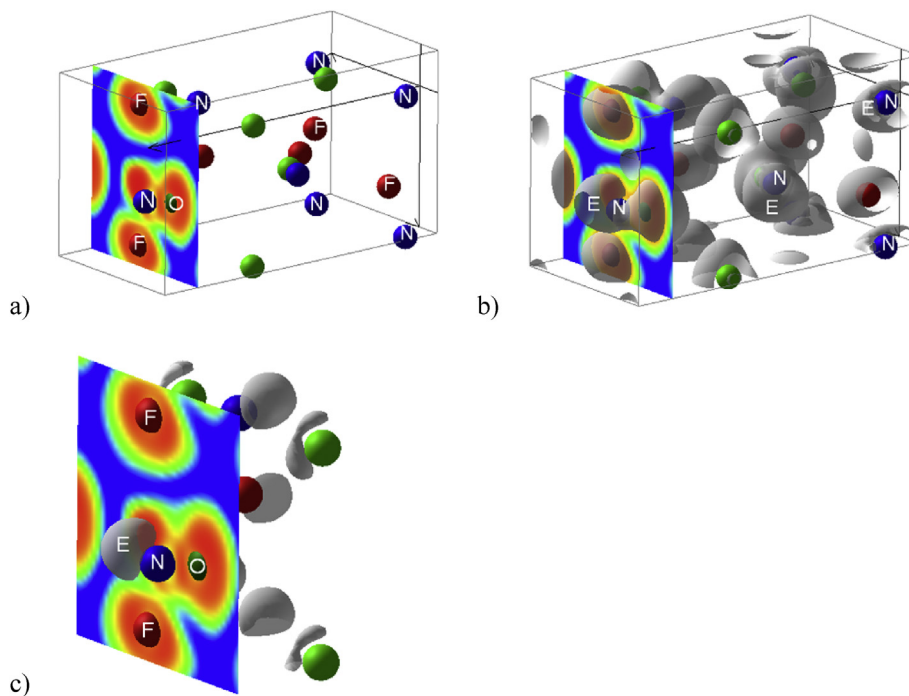


Fig. 6. NOF. ELF 2D slice crossing NOF angular molecule (a) and the corresponding 3D ELF isosurfaces, highlighting the E position at N and its spatial development (b) reproducing the schematic view in Fig. 5. Panel c) illustrates further the stereospecificity of E at large isosurface values (0.89).

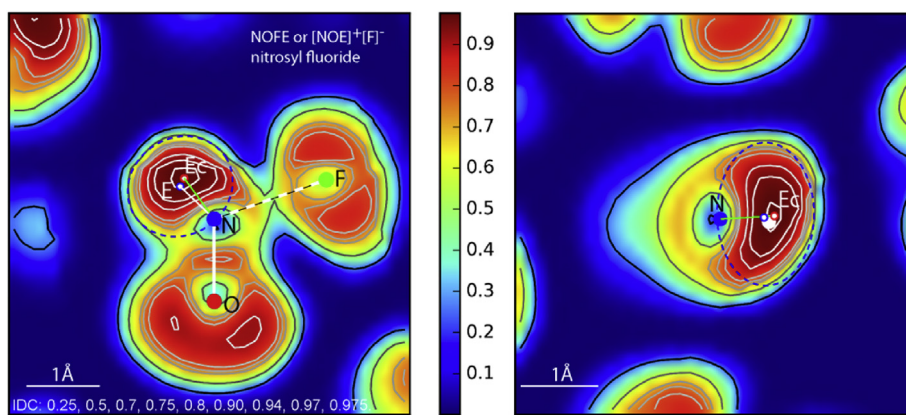


Fig. 7. ELF sections of the $[\text{NOE}]^+[\text{F}]^-$ molecule in its plane and perpendicular aligned to N–Ec (IDC: iso-density curves). Dotted blue ellipses roughly limit the ellipsoid shapes of E electronic cloud.

electronic cloud towards $\text{N}=\text{O}$ while encountering a strong repulsive resistance which maintains high $\angle\text{ENO} = 134^\circ$ angle. In spite of these repulsive and attractive forces, E electronic cloud, if deformed—attesting to its plasticity—is by no means broken up. Note also that its volume (radius $r_E = 0.78 \text{ \AA}$) is slightly bigger than NH_3E one (radius $r_E = 0.73 \text{ \AA}$).

Using this piece of information it was possible to precisely determine the direction and size of nitrogen lone pair associated with crystal network features and to calculate x, y, and z coordinates of E. Data of the $[\text{NOE}]^+[\text{F}]^-$ molecule in the crystal structure are given in Table 2 and reported also in Fig 5 (right-hand side).

4. $\text{N}_2\text{O}_3\text{E}_2$ or $[\text{NOE}]^+[\text{NO}_2\text{E}]^-$ the nitrosyl nitrite

Delicate crystal growth from the liquid around 100 K allowed obtaining single crystals suitable for X-ray analysis. At low temperatures there is a complicated phase transition system which has been described in detail [15]. Crystallographic data are summarized in Table 3.

4.1. Crystal structure

Two N_2O_3 varieties have been well identified, one orthorhombic B, the second tetragonal A. The former cell, orthorhombic, exhibits four independent molecules (Table

Table 3*B* N₂O₃E₂ crystal and DFT data [15].

B N₂O₃E₂ – Orthorhombic, space group <i>P2₁2₁2₁</i> (No. 19), <i>T</i> = 113 K.					
<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	<i>V</i> (Å ³)	<i>Z</i>	<i>V</i> (O,E) (Å ³)
5.0686	6.4796	8.6326	283.52	4	14.2
5.1763	6.6028	8.8633	302.9	4	15.1
Interatomic distances (Å) and angles (°)					
N1–O1	1.121	N2–O2	1.207	O2–N2–O3	128.6
O1–O2	2.634	N2–O3	1.209	N1–N2–O1	105.1
N1–N2	1.890	O2–O3	2.176	N1–N2–O3	119.5
N1–E	0.64	N2–E2	0.54	N2–E2–N1	179.4
				∠E1N1O1	146.0
				∠E1N1N2	108.7
Data from DFT-ELF analyses					
N1–Ec1	0.67	N2–Ec2	0.58	∠O1N1N2	107.1
N1–E1	0.57	N2–E2	0.44	∠E1N1O1	144.9
N1–O1	1.159	N2–O2	1.227	∠E1N1N2	108.0
N1–Ec2	1.38	N2–O3	1.225		
“N1–N2”	1.958	O2–O3	2.211	∠O2N2Ec2	111.4
<i>r</i> _{E1}	0.77	<i>r</i> _{E2}	0.66	∠O3N2Ec2	119.9
Ec1–E1	0.10	Ec2–E2	0.13		

3). A schematic drawing of the quasi planar N₂O₃ molecule according to [15] is given in Fig. 8a. Usually it is expected to have two lone pairs one for each nitrogen, leading to N₂O₃E₂ formula the authors do not mention the lone pair existence, they nevertheless indicate the “extraordinarily long N1–N2 bond” and suggest an evolution towards a “hypothetical nitrosyl nitrite” compound.

Then a more complete shape was elaborated for the N₂O₃E₂ molecular structure as shown in Fig. 8b, based for N1 coordination on the NOE nitrosyl group well defined in NOFE (see above). For N2 it was more difficult to propose a position for E2 taking into account the established “N2–N1 bond”, so, proposals like i) E2 above and below the molecule plane (50% statistically) or ii) delocalization in a torus close to N2 having N2–N1 as an axis, were not reliable.

To clear up our view of the nitrogen lone pair problem in the N₂O₂E₂N1OE1 molecular structure pertaining to

- their existence;
- their position;
- their volume
- and finally their outstanding role in molecular shape and crystal packing, ab initio calculations within Density Functional Theory (DFT) and Electron Localization Functions (ELF) were realized followed by precise planar sections to show via iso-density curve analyses the details of bonding scheme.

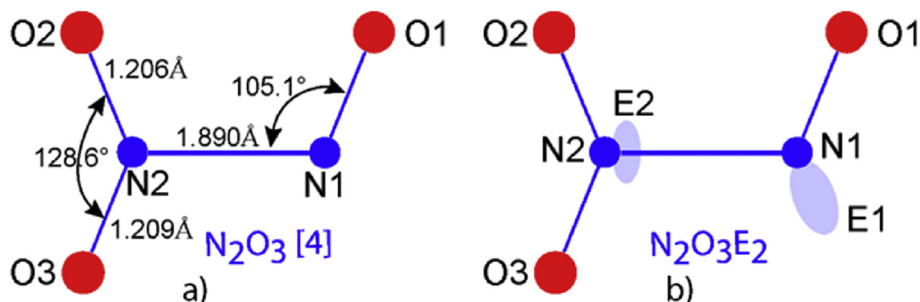


Fig. 8. a) N₂O₃ molecule scheme according to [15]; b) our starting scheme with E1 roughly alike in nitrosyl fluoride and E2 grafted onto N2.

4.2. ELF calculations

Fig. 9 shows the 3D ELF isosurfaces highlighting E volume development on N1 and N2 within nitrosyl NO group and nitrite NO₂ motifs, respectively (cf. Table 3).

Starting with the ELF full three dimensional data producing the above Fig. 9, four sections were realized. The full molecule as said above is quasi-planar as shown by both Fig. 10a and c depicted by their iso-density curves (IDCs). In the former section (Fig. 10a), the nitrite group NO₂ shows its two short N2–O double bonds (2.226 Å) with in their middle their trace define by an IDC around 0.75e⁻/Å³. But the major indication is the presence of an intense localization, opposite to the oxygen atoms O2 and O3 of nitrite group and right in the direction of N1, clearly showing the site of lone pair E2. There is a maximum density in this area which reaches 0.90e⁻/Å³, marked by a red circle which could be attributed to the centroid of lone pair Ec2. Then the whole volume defined by a dotted blue ellipse in this plane corresponds to the electronic cloud generated, so-called in our papers [5,6] the ‘sphere of influence’ of E the lone pair (ellipse parameters: *a* = 0.57 Å, *b* = 0.54 Å). To clarify this volume close to an ellipsoid, a section by a vertical plane passing through N2–Ec (Fig. 10b) has been drawn, giving the third parameter (*c* = 0.93 Å). Then an average spherical volume for E2 is estimated with a radius of *r*_{E2} = 0.66 Å.

In Fig. 10a the distance N2–Ec is 0.58 Å and shows that the N2–N1 direct bond does not exist. It has been demonstrated that these lone pair electron clouds, if they are not compressible, can be deformed by various atomic interactions. In Fig. 10a, NO₂ nitrite group ‘wings-like’ N2–O2 and N2–O3 as well as the presence of the nitrosyl ion, are a barrier to E2 expansion itself strongly associated to its cation. Therefore these constraints leave more freedom in the vertical plane. But an electronic cloud bending towards N₂O₂ plane is noticed. Then E2 makes a kind of electronic cap on the top of [N₂O₂E₂]⁻ nitrite anion (relevant data are given in Table 3).

To define E1 lone pair the ELF section by N2N1O1 plane shows a large electron cloud whose center, defined as previously, exhibits Ec1 maximum at N1–Ec1 = 0.67 Å with an IDC around 0.96e⁻/Å³. The E1 cloud appears somewhat distorted in its part pointing towards O3 being elongated up to the line N1–N2. Anyhow, one can admit that an ionic bond is established between N1 and Ec2.

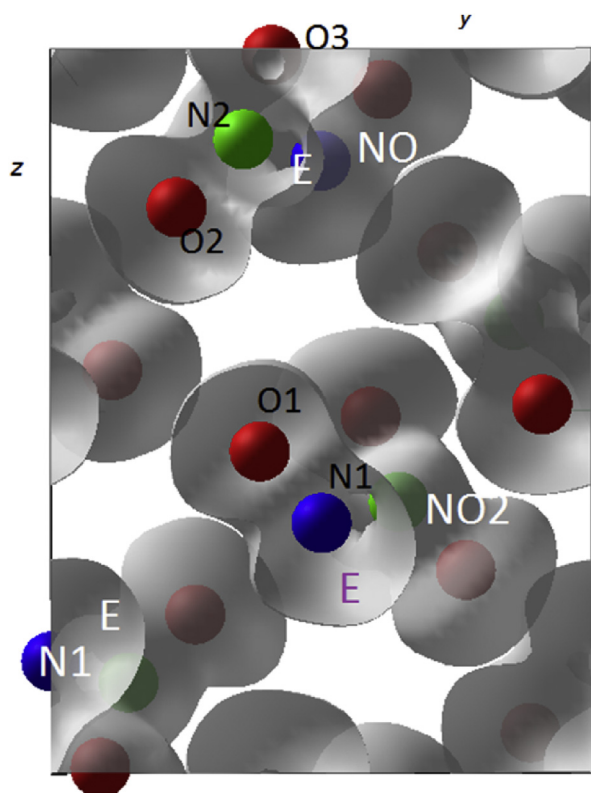


Fig. 9. N₂O₃: 3D ELF isosurfaces highlighting E volume development on N1 and N2 forming “NO2” and “NO” entities (cf. Table 3).

The sum of the two distances N1–Ec2 = 1.38 Å and Ec2–N2 = 0.58 Å amounts to 1.96 Å, which corresponds to the “long bond N2–N1 = 1.958 Å”.

Then the nitrosyl group [NOE]⁺ is now well defined (data in Table 3) and N₂O₃E₂ appears as a real nitrosyl nitrite [NOE]⁺[NO₂E][−] entity which is represented in Fig. 11b and also in its molecular crystal network (Fig. 11a).

5. Comparison with N₂O₄ and NOFE

The nitrosyl nitrite molecule, like N₂O₄, is quasi planar (small torsion angle ~3.2° between the two angular and triangular groups) – Fig. 12, therefore by comparison some remarkable differences must be noted showing an E stereochemical role. In N₂O₃E₂ molecule N2–O2 and N2–O3 bonds are slightly longer, around 0.03 Å, but the ∠O2N2O3 angle is pinched evolving from 134.3° to 128.6°, an effect directly linked to LP–BP repulsion exerted by Ec2 on N–O bonding. Note also that the N2–Ec2–N1 long interatomic distance, partly ionic (N1–Ec2), is enlarged up to 1.890 Å compared to the real bond N–N' = 1.758 Å in N₂O₄ [16].

Interesting also to compare the NOE nitrosyl part of N₂O₃E₂ with the one of NOFE (Fig. 12) both exhibiting typical angular geometry. N1–E1 and N–E show the same value of ~0.68 Å but if N1–O1 = 1.159 Å indicating a double bond character in NOFE, N–O = 1.084 Å tends to a triple bond. The ionic bonding N1–Ec2 = 1.38 Å is markedly shorter than N–F = 1.651 Å, inducing an

inverted conclusion when ∠ENO angle is considered: 144.9° for N1 and 134° for N. This lets suggest that the repulsion of F[−] anion bigger than the concentrated Ec2 has a more effective impact attached to its size on O and E in spite of being at a larger distance. The same effect touches the ∠ENF and ∠ONF angles considerably enlarged in NOFE (Fig. 12).

Note

It is important to underline for this molecule the phase transition giving at higher temperature a new polymorphic phase A–N₂O₃E₂ crystallizing in tetragonal system space group I4₁/a with $a = b = 16.2557$ Å, $c = 8.8049$ Å, and $Z = 32$). This large cell exhibits two independent N₂O₃E₂ molecules in asymmetric units, A and B, this last unit showing two conformations B1 and B1'. These molecules are very similar to the one in B–N₂O₃E₂ form with their [NO₂E][−] nitrite ion, the nitrosyl group [NOE]⁺ in the B unit flipping between two positions (50% occupancy). The fact that these three forms of N₂O₃E₂ molecules show similar crystallographic parameters (bonds and angles) testifies that the ionic interaction N1–Ec2 underlined above linking up nitrite [N2O₂E][−] and nitrosyl [N1OE]⁺ group is well established supporting phase transition with a full molecule dispatching in various positions.

This N1–Ec ionic bonding appears rather unusual because the electronic doublet 2s² plays the role of an anion like a fluoride for example, well illustrated by [NOE]⁺F[−] here above.

To verify if such a possibility exists under other conditions, we have analyzed silver nitrite AgNO₂E crystal structure and calculated its ELF.

6. Comparison of silver nitrite AgNO₂E with [N2O₂E][−] [N1OE]⁺

AgNO₂E crystallizes in the orthorhombic system [17]. The data are reported in Table 4.

A view of the crystal network is given in Fig. 13. Six nitrite groups NO₂E all parallel to the (100) plane are distributed at the apices of an octahedron encapsulating the silver atom. In the equatorial plane four oxygen atoms of four different NO₂ groups form the rectangular base of a large square prism on the top of which sit Oe and Of of the NCo₂E group. Finally there is an oxygenated hexahedron surrounding Ag with relatively large Ag–O interatomic distances. It is worthy noting that in the [001] direction there is a sixth NO₂E group showing an Ag–N distance of 2.471 Å therefore including in between the E lone pair; then deducing that the sixth nitrite group should be linked to Ag by ionic bonding Ag–E.

Consequently calculations were of paramount importance to establish this sequence N–E–Ag by comparison with N2–Ec2–N1 found in N₂O₃E₂. The DFT and ELF resulting data are given in Table 4.

Fig. 14 shows the extended cell of AgNO₂ with grey 3D ELF isosurfaces around NO₂– nitrite entities, around electropositive Ag alike an alkaline cation characterized by the absence of electron localization (no isosurface). Note the close relationship with the schematic view in Fig. 13.

Two sections were done in the three dimensional ELF, one following the plane formed by N, O and Ag atoms which shows the presence of E, the second perpendicular,

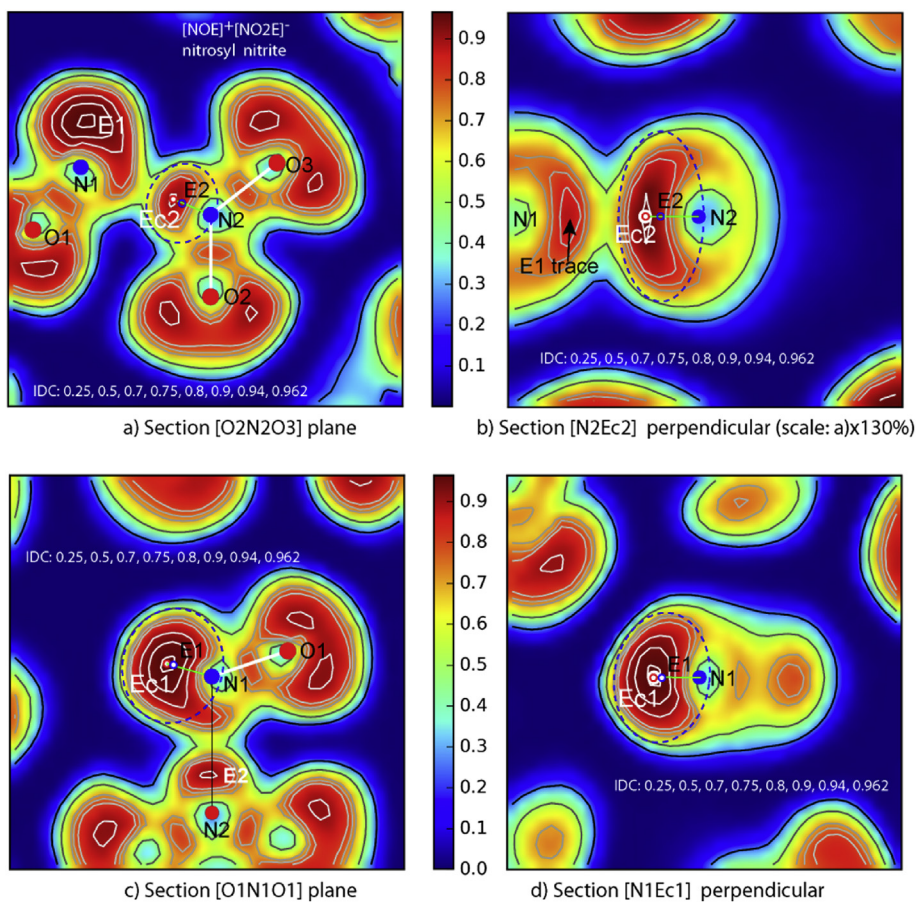


Fig. 10. ELF sections: a) Nitrite group plane N2O2O3; b) perpendicular plane to a) passing via N2–E2; c) nitrosyl group N1O1 + N2, d) perpendicular plane passing via N–E1.

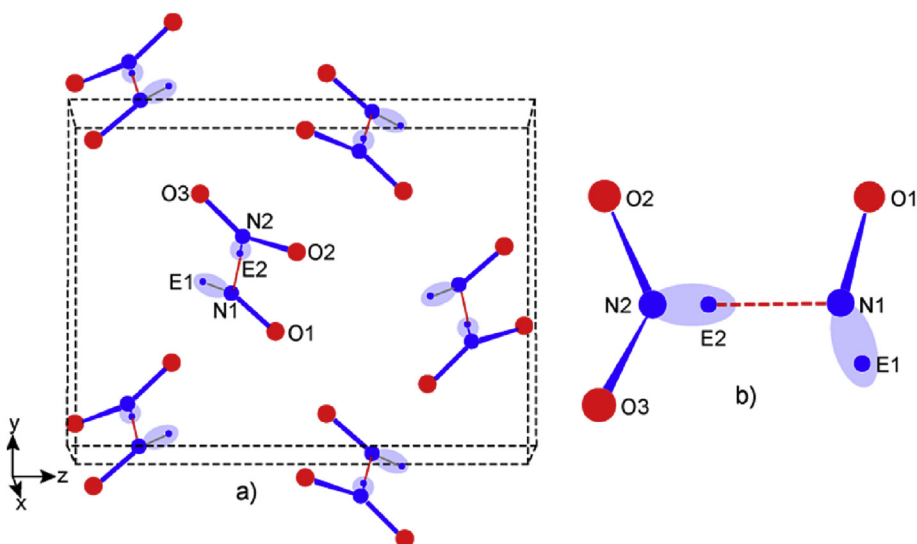


Fig. 11. Perspective views: a) orthorhombic $N_2O_3E_2$ network; b) $[NOE]^+[NO_2E]^-$ nitrosyl nitrite molecule (dotted red stick indicates the ionic interaction N1 to Ec2 which firmly associate nitrite triangular unit and angular nitrosyl one).

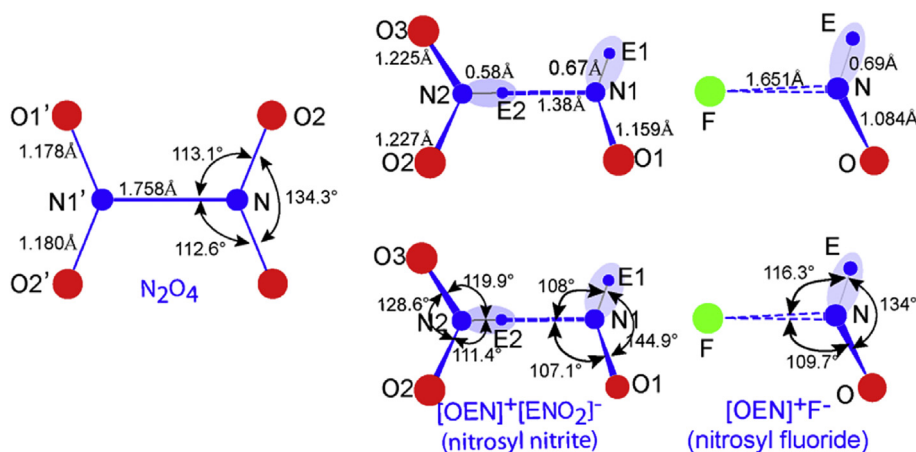


Fig. 12. Comparison of N_2O_4 , $\{E1O1N1-E2N2O_2\}$ and $\{EON-F\}$ molecules (ELF data).

Table 4

$AgNO_2E$ crystal data [17] and DFT data.

$AgNO_2E$ – Orthorhombic, space group $Im\bar{m}2$ (No. 44).					
a (Å)	b (Å)	c (Å)	V (Å ³)	Z	$V(Ag,O,E)$ (Å ³)
3.528	6.171	5.17	112.56	2	14.1
3.613	6.452	5.122	119.4	2	14.9
Interatomic distances (Å) and angles (°)					
N–O	1.154	N–Ag	2.471	Ag–Oef	2.425
O–O	2.074	Ag–O	3.153	$\angle ONO$	127.9
N–Oabcd	3.410	Ag–Oabcd	2.732	$\angle OeAgOf$	50.6
N–E	0.61	Ag–E	1.861	E–Oabcd	3.077
Data from DFT-ELF analyses					
N–Ec	0.62	N–Ag	2.240	Ec–Oabcd	3.084
N–E	0.57	Ag–Ec	1.620	r_E	0.68
N–O	1.266	Ag–Oef	2.449	Ec–E	0.13
O–O	2.137	Ag–Oabcd	2.837	$\angle ONO$	115.1
N–Oabcd	3.385	Ag–O	3.108	$\angle OeAgOf$	51.7

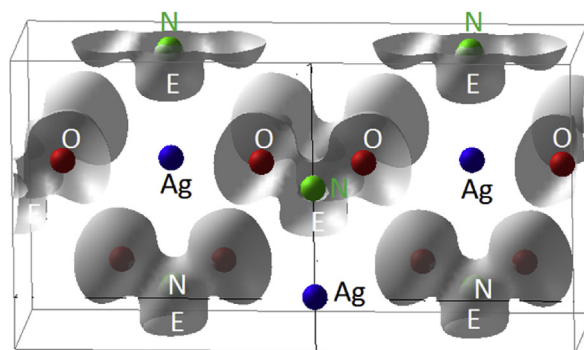


Fig. 14. $AgNO_2$. Calculated 3D ELF isosurfaces reproducing the schematic view in Fig. 13.

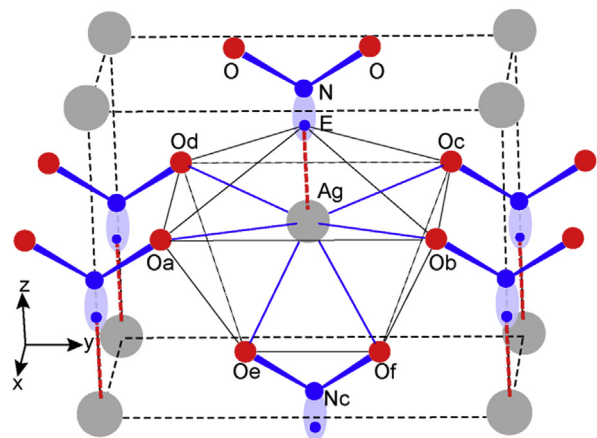


Fig. 13. Perspective view of $AgNO_2E$ crystal structure.

including N–E in order to appreciate E extension in the [100] direction (Fig. 15).

DFT data show that a and b cell parameters are slightly bigger while c is shorter than for X-ray crystal data. Therefore if Ag–Oef and Ag–Oabcd distances are similar, the distance N–Ag is shorter. E is clearly evidenced in

Fig. 15a and b with a density maximum attributed to LP centroid Ec. N–Ec = 0.62 Å and the generated electron cloud is centered in E at -0.13 Å from Ec. Between Ag and Ec, an ionic interaction is established, fixing NO_2^- on the top of the octahedron (Oef)OabcdE. This bonding shows that Ag–Ec = 1.620 Å and Ec–N = 0.62 Å, corresponding to the distance Ag–N = 2.24 Å. This scheme recalls the one in $N_2O_3E_2$ even if the distances are bigger.

From these sections an E volume, approximated as an ellipsoid, was evaluated with $a = 0.66$ Å, $b = 0.44$ Å, and $c = 1.06$ Å, grossly corresponding to a sphere of influence $r_E = 0.68$ Å, a value close to the one of E2 in $N_2O_3E_2$, i.e. $r_{E2} = 0.66$ Å.

7. NCl_3E

NCl_3 is an oily liquid at room temperature, with a yellow color. It crystallizes at low temperature below 233 K. X-ray data have been collected at 148 K as reported in Table 4 [18].

7.1. Crystal structure

The NCl_3 crystal network contains three independent NCl_3E molecules which are organized in separated layers

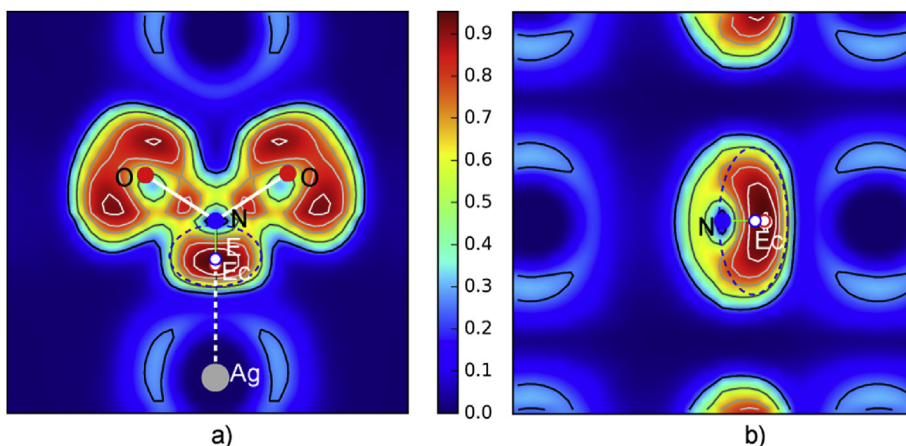


Fig. 15. ELF sections: a) section plane containing N, O and silver atoms showing the whole nitrite group with its lone pair E; b) the perpendicular plane passing through N–E.

parallel to the (010) plane centered onto mirror planes in $y = 1/4$ and $3/4$ as shown in Fig 16a (projection along [001]). Their thickness amounts to $\Delta L = 2.813 \text{ \AA}$; the empty space slab showing a $\Delta i = 0.185 \text{ \AA}$ value. To make a clear drawing of these layers, the one lying along the mirror in $y = 1/4$ has been isolated; it is reported in Fig. 16b. The three molecules N1Cl_3 , N2Cl_3 and N3Cl_3 show a triangular prismatic shape. Then they have the classical NCl_3E tetrahedral geometry with their lone pairs opposite their one sided coordination to chlorine atoms. All of them exhibit very similar N–Cl bonds which evolve between 1.712 \AA and 1.786 \AA (see Table 4). The molecules $\text{N1Cl}_3\text{E}$ and $\text{N2Cl}_3\text{E}$ appear more condensed via large interactions (dotted lines values evolving from 3.190 \AA up to 3.917 \AA) in the first half part of the cell along [001]. $\text{N3Cl}_3\text{E}$ molecules assume their interconnection and therefore the stability of the network. It is important to note the chlorine encapsulation of N1E1 ,

N2E2 and N3E3 , the former showing a $[\text{N1E1}]\text{Cl}_6$ octahedron, the next two $[\text{N2E2}]\text{Cl}_6$ and $[\text{N3E3}]\text{Cl}_6$ being in triangular prisms more or less distorted. In our search for lone pair size, position and influence of the $2s^2$ lone pair in this nitrogen trichloride was an interesting prototype to enrich our examples (see Table 5).

7.2. ELF calculation

After DFT-ELF calculations, pertinent parameters are shown in Table 4.

Fig. 17 shows the 3D ELF isosurface of NCl_3 . The projection is presented at high isosurface value of 0.881 for the sake of clarity due to the large number of atoms in the unit cell. E on top of N is clearly shown. At such a high isosurface value, the ELF around Cl is observed as a torus enclosing the non bonded Cl electrons.

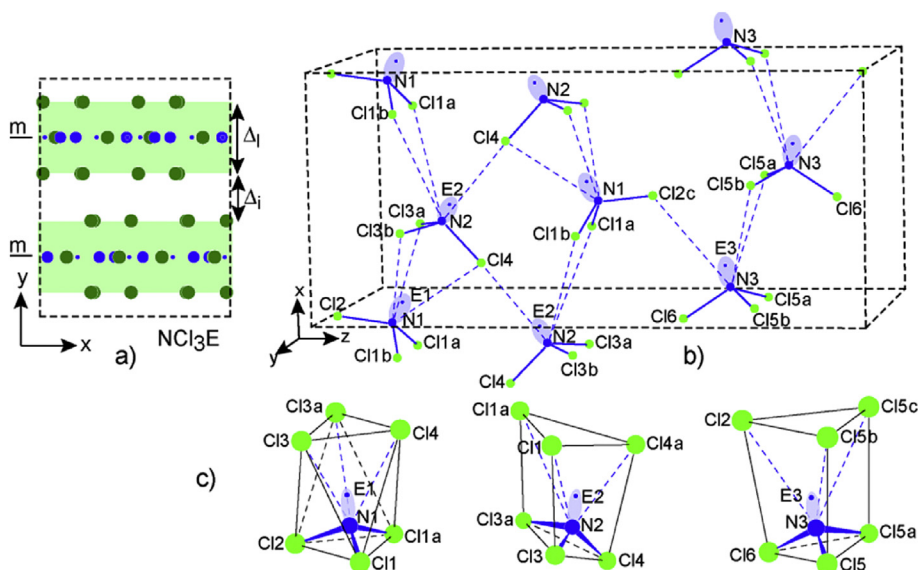


Fig. 16. a) View along [001] of the NCl_3 network; b) perspective view of the layer parallel to the (010) plane formed by NCl_3E molecules and their interactions (dotted blue sticks); c) Coordination chlorine polyhedra around each independent $[\text{N1E1}]$, $[\text{N2E2}]$ and $[\text{N3E3}]$.

Table 5
NCl₃E crystal and DFT data [18].

NCl ₃ E – Orthorhombic, space group <i>Pnma</i> (No. 62), <i>T</i> = 148 K									
<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	<i>V</i> (Å ³)	<i>Z</i>	<i>V</i> (Cl,E) (Å ³)				
7.48	9.35	16.48	1152.6	12	24				
7.609	9.480	16.699	1204.6	12	25.1				
Interatomic distances (Å) and angles (°)									
N1–Cl1	1.731	N2–Cl3	1.786	N3–Cl5	1.786	∠Cl1a,bN1Cl2	107.4		
	a,b	a,b	a,b	a,b					
N1–Cl2	1.772	N2–Cl4	1.712	N3–Cl6	1.712	∠Cl1aN1Cl1b	109.5		
N1–Cl3	3.298	N2–Cl1	3.917	N3–Cl5	3.685	∠Cl3a,bN2Cl4	108.1		
	a,b	a,b	a,b	a,b					
N1–Cl4	3.360	N2–Cl4a	3.190	N3–Cl2c	3.631	∠Cl3aN2Cl3b	105.2		
						∠Cl5a,bN3Cl6	108.5		
N1–E1	0.70	N2–E2	0.67	N3–E3	0.69	∠Cl5aN3Cl5b	104.8		
E1–Cl3a,	2.70	E2–Cl1a,	3.48	E3–Cl5a,	3.12				
3b		1b		5b					
E1–Cl4	2.79	E2–Cl4	2.56	E3–Cl2	3.07				
Data from DFT-ELF analyses									
N1–Ec1	0.68	N2–Ec2	0.70	N3–Ec3	0.68				
N1–E1	0.55	N2–E2	0.57	N3–E3	0.61				
N1–Cl1a,b	1.778	N2–Cl3a,b	1.783	N3–Cl5a,b	1.781				
N1–Cl2	1.779	N2–Cl4	1.782	N3–Cl6	1.808				
<i>r</i> _{E1}	0.73	<i>r</i> _{E2}	0.76	<i>r</i> _{E3}	0.75				
∠Cl1a,bN1Cl2	107.9	∠Cl3a,bN2Cl4	107.7	∠Cl5a,bN3Cl6	107.3				
∠Cl1aN1Cl1b	107.4	∠Cl3aN2Cl3b	107.1	∠Cl5aN3Cl5b	106.3				

Then sections with iso-density curves throughout ELF data were performed right in the mirror plane of each molecule. They are illustrated in Fig. 18. Visibly they show that the three NCl₃E molecules are quasi-identical. Therefore they were precisely analyzed in order to determine the position of the lone pair E and eventually if a maximum was detectable to show its maximal density concentration

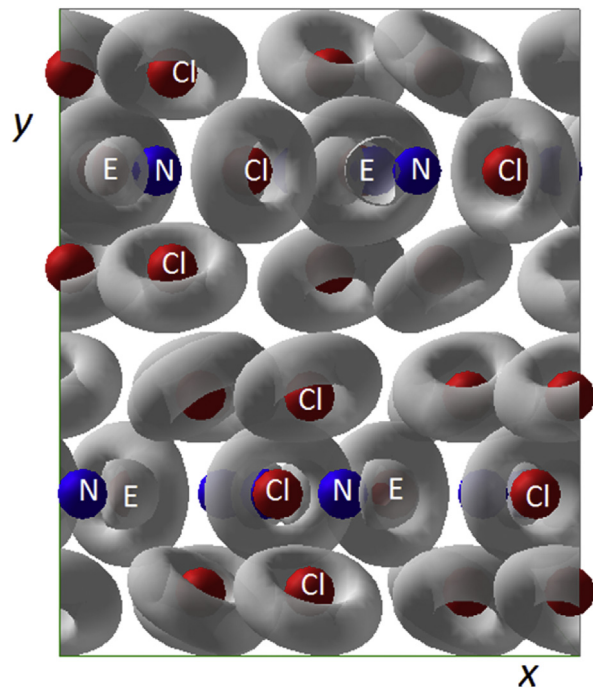


Fig. 17. NCl₃: 3D ELF view along xOy in a similar fashion to that in Fig. 16a.

(reasonably its centroid Ec), the N–Ec distance and assuming an ellipsoid shape, its two parameters a and b in the mirror, the third being determined in Fig. 18b,d,f the perpendicular sections to N–Ec.

N–Ec distances were readily measured as well as N-Cl ones allowing to determine the crystallographic coordinate of Ec. Then ellipses surrounding the electronic density [N–Ec] were made around each molecule giving the following *a/b/c* parameters: 0.79/0.67/0.75 Å for [N1–Ec1], 0.81/0.69/0.78 Å for [N2–Ec2] and 0.81/0.68/0.77 Å for [N3–Ec3]. Roughly, they correspond to lone pair spheres of influence with *r*_{E1} = 0.73 Å, *r*_{E2} = 0.76 Å and *r*_{E3} = 0.75 Å. E centers of the ellipsoids, like in the other examples, are slightly off centered from the centroid Ec of lone pair, their large volume showing a less electronic density than the centroid Ec, rather well condensed, are more sensitive to the various repulsions of the network surroundings. Therefore it is worth noting the small distance between Ec and E ~0.12 Å.

From these experiments, an average distance N–Cl = 2.10 Å to chlorine atoms of triangular prismatic NCl₃ molecule base has been extracted and transferred to crystal data to localize E1, E2 and E3 lone pairs by using their coordinates. To control that, their volumes of influence are well set up in [NE] coordination polyhedra, and distances with remaining chlorines were calculated. They show an average value of 3.00 Å, much higher than E–Cl = 2.10 Å, making this insertion acceptable (Table 4).

Therefore, data of the NCl₃E crystal structure have been completed (blue printed values) favoring a full understanding of its atomic architecture, the molecules being put together to build layers [NCl₃E]_{*n*}, by a cobweb of long N–Cl weak bonds. The layers packed along [010] are held by Van der Waals interactions.

8. Conclusion

This work was devoted to the formal 2s² lone pair (LP) behavior in simple fundamental molecules. The aim was to find LP position, to evaluate its “volume of influence” which consists in an electron cloud generated around the centroid Ec of the electronic doublet. We considered basic molecules formed around nitrogen atom: NH₃E ammonia, [NOE]⁺F[−] the nitrosyl fluoride, [NOE]⁺[NO₂E][−] nitrosyl nitrite (plus AgNO₂E silver nitrite) and NCl₃E nitrogen trichloride.

Like in our approach of these problems with the 6s² elements (Tl, Pb, Bi, Po), the LP role in the crystal network architecture is of paramount importance [1–3,5,6]. Using new analytic software, it has been possible to complete electron localization function (ELF/DFT) calculations by making precise sections within three dimensional electron localization which allowed setting up Ec, a small volume of maximum intensity in an E electron cloud.

Ec position was then determined, cloud volume and its center E always with a position slightly distinct from Ec (~0.12 ± 0.02 Å) and closer to N. The size of the lone pair in all these compounds does not show strong differences: *r*_{ENH₃} = 0.65 Å, *r*_{EAgNO₂} = 0.77 Å and 0.66 Å, *r*_{EAgNO₂} = 0.68 Å, *r*_{ENOF} = 0.78 Å and *r*_{EN₁Cl₃} = 0.73 Å, *r*_{EN₂Cl₃} = 0.76 Å, and *r*_{EN₃Cl₃} = 0.75 Å.

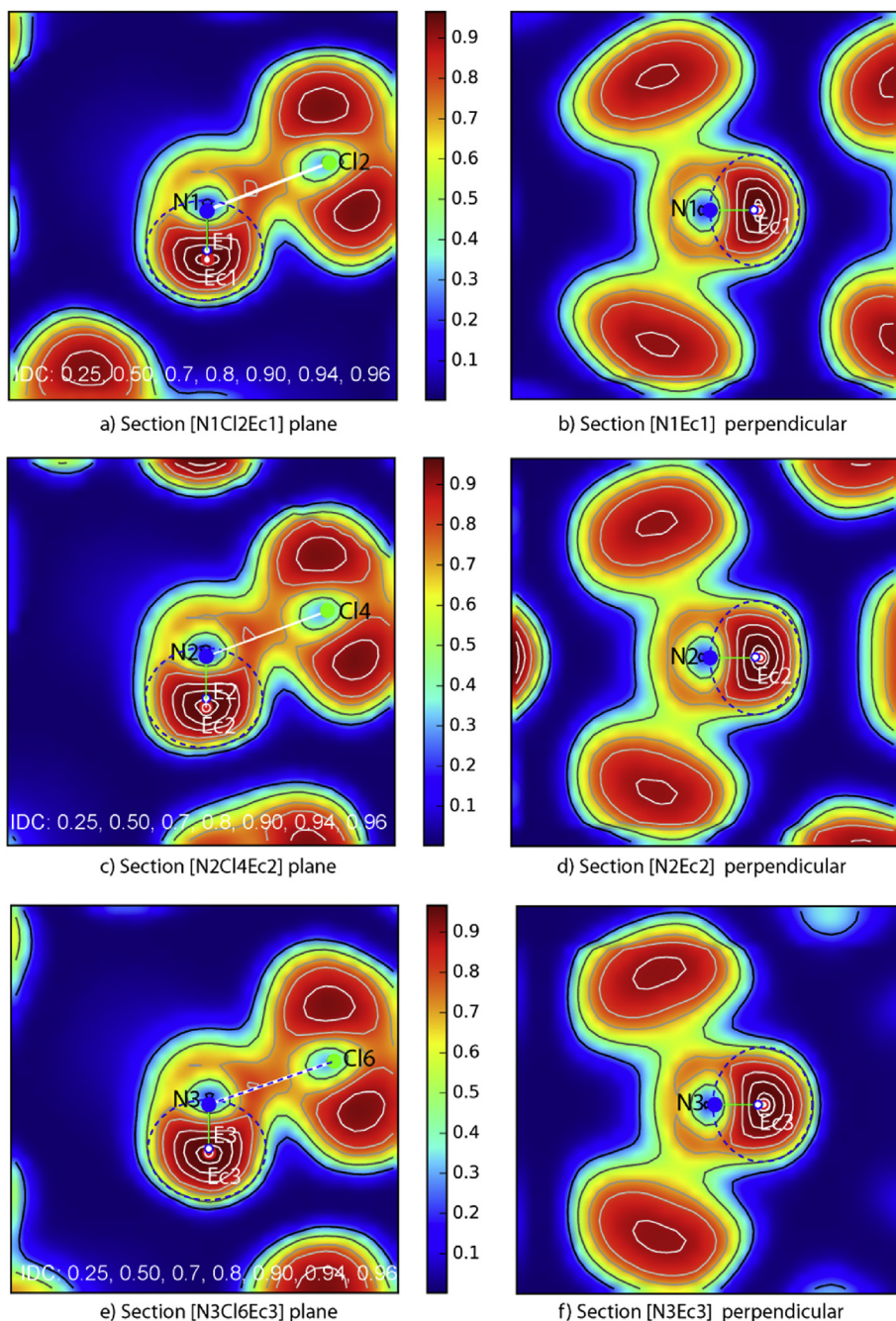


Fig. 18. ELF sections: a,c,e) planar sections containing N, Cl and E atoms in the mirror plane of the three independent molecules N1, N2 and N3; b,d,f) the perpendicular plane to N–Ec in Ec for each molecule.

The determination of the E2 lone pair position in the nitrite group $[\text{N1OE1}]^+[\text{N2O}_2\text{E2}]^-$ of nitrosyl nitrite has evidenced a strong ionic N1–E2 interaction, allowing to understand the stability of the whole molecule even during its crystal structure phase transition, a linear sequence N2–Ec2–N being substituted to the “extraordinary long N2–N1 bond (1.890 Å)”. This direct ionic interaction with lone pair centroïd was unexpected; therefore, an analogous situation occurs in AgNO_2E , silver nitrite, where Ag is directly online with E of nitrite group.

9. Short annex on the theory framework

It is now established in quantum physics and chemistry that an accurate way to account for exchange and correlation (XC) albeit at the local level, is carried out within the density functional theory (DFT) [7,8]. The first account of XC effects was first approximated with the local density approximation (LDA) [19] scheme based on the homogeneous electron gas. However introducing gradients to the electron density was rapidly needed with the GGA

(generalized gradient approximation, used in the present work [20]). The subsequent success of the DFT, in accounting for the physical properties of a broad panel of compounds, led to building many methods around it with different levels of outcomes of electronic and magnetic band structures, chemical bonding properties and other energy related properties as mechanical ones (enthalpies, bulk modules, elastic constants, etc.).

In our work we used the Vienna ab initio simulation package (VASP) code [21,22] to obtain equilibrium crystal structures which are actually close to experimental determination. The purpose is here to subsequently 'build' the electron localization around the chemical constituents: i.e. the atoms with their chemical trend to ionization either positively—decrease of localization—or negatively—increase of localization. This can be done through different schemes such as the electron localization indicator (ELI-D) [23] or the electron localization function (ELF) used here [9]. The ELF scheme is based on the kinetic energy in which the Pauli Exclusion Principle is included: $ELF = (1 + \chi_\sigma^2)^{-1}$ with $0 \leq ELF \leq 1$, i.e. it is a normalized function. In this expression, the ratio $\chi_\sigma = D_\sigma/D_\sigma^0$, where $D_\sigma = \tau_\sigma - \nabla s - \frac{1}{4}(\nabla\rho_\sigma)^2/\rho_\sigma$ and $D_\sigma^0 = 3/5(6\pi^2)^{2/3}\rho_\sigma^{5/3}$ correspond, respectively, to a measure of Pauli repulsion (D_σ) of the actual system and to the free electron gas repulsion (D_σ^0) and τ_σ is the kinetic energy density. Then a normalization of the ELF function between 0 (zero localization) and 1 (strong localization) with the value of $\frac{1}{2}$ corresponding to a free electron gas behavior enables analyzing the contour plots following a color code: blue zones for zero localization, red zones for full localization and green zone for $ELF = \frac{1}{2}$, corresponding to a free electron gas. Besides the 2D ELF representation we mainly consider the 3D iso-surfaces enclosing the electrons of each atomic constituent. This paper shows the usefulness of such 3D representations for the discussion of the lone pair development and stereo-activity.

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References

- [1] R.J. Gillespie, R.S. Nyholm, Q. Rev. Chem. Soc. 11 (1957) 339.
- [2] R.J. Gillespie, I. Hargittai, The VSEPR Model of Molecular Geometry, Allyn and Bacon, 1991, p. 149.
- [3] S. Andersson, A. Aström, Solid State Chemistry, in: Proc. 5th Material Research Symposium, 364, NBS Special Publication, 1972, pp. 3–13.
- [4] J. Galy, G. Meunier, S. Andersson, A. Aström, J. Solid State Chem. 13 (1975) 142.
- [5] S.F. Matar, J. Galy, Prog. Solid State Chem. 43 (2015) 82–97, <http://dx.doi.org/10.1016/j.progsolidstchem.2015.05.001>.
- [6] J. Galy, S.F. Matar, Prog. Solid State Chem. 44 (2016) 35–58 (account).
- [7] P. Hohenberg, W. Kohn, Phys. Rev. B 136 (1964) 864.
- [8] W. Kohn, L.J. Sham, Phys. Rev. A 140 (1965) 1133.
- [9] A.D. Becke, K.E. Edgecombe, J. Chem. Phys. 92 (1990) 5397; Nature, 371 (1994) 683.
- [10] H. Mark, E. Pohland, Z. Kristallogr. 62 (1925) 103.
- [11] R. Boese, N. Niederpruem, D. Blaeser, A.H. Maulitz, M.Y. Antipin, P.R. Mallinson, J. Phys. Chem. 101 (1997) 5794–5799.
- [12] E. Vila, Lone pair coordinates calculation in solid state crystal structures, private communication, ICMM/CSIC, Madrid, Spain.
- [13] G. Couégnat, unpublished results, 2015.
- [14] A. Ellern, K. Seppelt, Z. Anorg. Allg. Chem. 627 (2001) 234–237.
- [15] J. Horakh, H. Borrmann, A. Simon, Chem. Eur. J. 1 (6) (1995) 389–393.
- [16] A. Obermeyer, H. Borrmann, A. Simon, Z. Kristallogr. 196 (1991) 129–135.
- [17] R.E. Long, R.E. Marsh, Acta Crystallogr. 15 (1962) 448–450.
- [18] H. Hartl, J. Schoener, J. Jander, H. Schulz, Z. Anorg. Allg. Chem. 413 (1975) 61–71.
- [19] D.M. Ceperley, B.J. Alder, Phys. Rev. Lett. 45 (1980) 566.
- [20] J. Perdew, K. Burke, M. Ernzerhof, Phys. Rev. Lett. 77 (1996) 3865.
- [21] G. Kresse, J. Furthmüller, Phys. Rev. B 54 (1996) 11169.
- [22] G. Kresse, J. Joubert, Phys. Rev. B 59 (1999) 1758.
- [23] F.R. Wagner, V. Bezugly, M. Kohout, Y. Grin, Chem. Eur. J. 13 (2007) 5724.