



ELSEVIER

Contents lists available at [SciVerse ScienceDirect](http://SciVerse.ScienceDirect.com)

Comptes Rendus Mecanique

www.sciencedirect.com

Combustion, flow and spray dynamics for aerospace propulsion

Compressible and low Mach number LES of a swirl experimental burner

David Barré^{a,*}, Matthias Kraushaar^a, Gabriel Staffellbach^a, Vincent Moureau^b,
Laurent Y.M. Gicquel^a^a CERFACS, 42, avenue G. Coriolis, 31057 Toulouse cedex 01, France^b CORIA, campus du Madrillet, 76801 St Etienne du Rouvray, France

ARTICLE INFO

Article history:

Available online 10 January 2013

Keywords:

Large-Eddy Simulation
Wall treatment
Pressure drop

Mots-clés:

Simulation aux Grandes Échelles
Traitement des parois
Perte de charge

ABSTRACT

Large-Eddy Simulations (LES) of a swirl experimental burner are performed using a compressible and a low Mach number solver. The investigations are focused on the modeling strategies in LES aimed at validating the flow predictions and principally the associated pressure losses. Accurate prediction of pressure drop through complex geometries, such as those typically encountered in industrial swirlers, is indeed of paramount importance to design and optimize the engine efficiency. LES is here probed and tested to identify the model parameters affecting pressure losses: grid resolution, wall treatment or solver accuracy, with the aim of highlighting the requirements for accurate pressure drop predictions. Results show that for the high Reynolds number flow considered, the wall law model provides the best predictions and minimizes the error compared to experimental findings with a reasonable overall CPU cost.

© 2012 Académie des sciences. Published by Elsevier Masson SAS. All rights reserved.

R É S U M É

Des Simulations aux Grandes Échelles d'un brûleur expérimental swirlé sont réalisées au moyen de deux codes, l'un compressible et l'autre bas Mach. Les simulations sont obtenues utilisant les deux codes pour évaluer leur performance et déduire une stratégie potentielle de modélisation. Les champs moyens de vitesse sont comparés aux résultats expérimentaux. La suite de cet article s'oriente sur la détermination des pertes de charge au travers du système d'injection, fortement dépendantes de paramètres tels que la résolution du maillage, le traitement des parois et le code. Deux approches numériques sont disponibles, soit le choix de résoudre entièrement l'écoulement, soit d'utiliser une loi de paroi. Les résultats montrent que pour des écoulements à nombres de Reynolds élevés, la loi de paroi fournit de meilleures prédictions en réduisant l'erreur par rapport aux résultats expérimentaux avec un coût global de calcul raisonnable.

© 2012 Académie des sciences. Published by Elsevier Masson SAS. All rights reserved.

1. Introduction

Although LES is becoming a routine CFD tool for engineers and researchers, predicting accurately pressure drops in complex industrial geometries still remains a challenge. Within the framework of the KIAI¹ European project, we intend

* Corresponding author.

E-mail addresses: barre@cerfacs.fr (D. Barré), Matthias.Kraushaar@cerfacs.fr (M. Kraushaar), gabriel.staffellbach@cerfacs.fr (G. Staffellbach), vincent.moureau@coria.fr (V. Moureau), laurent.gicquel@cerfacs.fr (L.Y.M. Gicquel).¹ KIAI: Knowledge for Ignition, Acoustics and Instabilities.

to investigate this topic on an academic methane/air single-burner operating under premixed conditions targeting ignition phenomena as they occur in real gas turbine engines. Prior to this specific transient flow context, non-reacting simulations of the experimental KIAI burner are carried out using two different LES codes, namely the compressible solver AVBP and the low Mach number code YALES2, in order to assess the different modeling strategies as well as their performance. AVBP is a massively-parallel finite-volume code for compressible reacting flows [1] developed by CERFACS and IFPEN, which solves the Navier–Stokes equations explicitly on unstructured and hybrid grids. It relies on the cell-vertex discretization method [2]. Lartigue [3] added characteristic decomposition according to the Navier–Stokes Characteristic Boundary Condition (NSCBC) formalism [4] and extended the code to handle multi-component flows [5]. The LES code YALES2 is also a finite-volume code for massively parallel computations [6–8] developed at CORIA, Rouen. It uses a vertex-centered method and is conceived for two-phase combustion simulations on massive complex meshes. Each solver owns different abilities which could be used in the investigation of pressure loss predictions. YALES2 possesses an automatic homogeneous mesh refinement algorithm allowing to achieve very high resolution especially in the near wall regions. Although this creates very large meshes, its low Mach number approach keeps the computational costs reasonable due to the larger time step. As for AVBP, it has the advantage of handling hybrid meshes and also benefits from multiple LES models, wall treatments and has demonstrated its capacity on many industrial applications. Comparing these two LES codes in the context of pressure loss predictions seems therefore judicious for proper understanding of the leading parameters.

Section 2 introduces theoretical considerations of pressure loss. Section 3 of this article is dedicated to the presentation of the swirl experimental burner and the validation of the flow by comparing averaged flow quantities to experimental measurements. In Section 4, pressure drop predictions are gauged through two different approaches, the wall-resolved LES or the use of a wall law model.

2. Pressure loss qualification and quantification

The objective of this section is to present the basic notions in fluid dynamics with the introduction of the Bernoulli equation and the concept of pressure loss. Bernoulli's principle states that the kinetic, potential and flow energies of a fluid particle are constant along a streamline for steady flows with compressibility and frictional effects are negligible. Therefore, the kinetic and potential energies of the fluid can be converted into flow energy, causing the pressure to change (and vice versa). Mathematically, this can be expressed as follows:

$$P + \frac{\rho V^2}{2} + \rho g z = \text{constant} \quad (1)$$

where P and V are respectively the pressure and the fluid flow speed at a point on a streamline, g is the acceleration due to gravity, z is the elevation above a reference plane, and ρ the density of the fluid. Each term of Eq. (1) represents some kind of pressure: P is the static pressure, $\frac{\rho V^2}{2}$ is the dynamic pressure and corresponds to the pressure rise when the fluid in motion is brought to a stop. Finally, $\rho g z$ is the hydrostatic pressure term and takes into account the elevation effects which are neglected thereafter. The sum of the static and dynamic pressures is usually called stagnation or total pressure and is defined by:

$$P_{stagn} = P + \frac{\rho V^2}{2} \quad (2)$$

The stagnation pressure of a compressible flow represents the pressure at a point where the fluid is brought to a complete stop isentropically. It is the highest pressure found anywhere in the flow field, and it occurs at the stagnation point where all kinetic energy has been converted into pressure. Bernoulli's equation for steady, isentropic and incompressible flows obtained for an ideal gas along a streamline translates the fact that no losses occur so $P_{stagn} = C^{ste}$. This principle of energy conservation can be extended to simple compressible flows [9]. In this case, stagnation pressure can be written as a function of the flow Mach number M :

$$\frac{P_{stagn}}{P} = \left(1 + \frac{\gamma - 1}{2} M^2\right)^{\frac{\gamma}{\gamma - 1}} \quad (3)$$

where T is the temperature and γ the ratio of specific heat capacities. This relationship describes the variation of the static pressure as the velocity (Mach number) changes under isentropic conditions in simple flows. It therefore includes thermodynamic effects that are not present in Bernoulli's expression.

Losses are, however, inevitable in real applications and these origins are multiple. Viscosity and non-isentropicity are typical sources. Friction by viscous effects will carry out energy from the incompressible flow even along a streamline so the Bernoulli constants upstream and downstream differ, which can be simply expressed as:

$$P_{stagn_2} = P_{stagn_1} + \Delta P \quad (4)$$

where ΔP is called a head loss. The main consequence of pressure losses is the transformation of mechanical energy linked to fluid transport into thermal energy. In complex flows, which are usually bounded by walls, two kinds of losses are

possible: the linear loss and the singular loss. Linear loss is induced by friction through the length of the system, caused by viscosity while a singular loss results from a flow perturbation in magnitude or direction as encountered when rotation appears. These losses or flow adaptations often occur because of sudden or gradual geometrical changes of the boundaries. Typical examples are sudden or smooth geometrical restrictions of the configuration through which the fluid has to flow. In extreme cases singular losses find their origin in the wall boundary layer transitional state (attached or detached flows) as well as recirculation bubbles encountered in current swirled combustor flows. Numerous studies were carried out to qualify and measure the different types of pressure losses. Julius Weisbach in 1855 was the first to find a relation for the head losses [10]. Henry Darcy contributed to the application of the derived relation, therefore commonly known as the Darcy–Weisbach formula. It links the head loss in a smooth pipe ΔP_f , the friction coefficient, the bulk flow velocity V and the pipe dimensions:

$$\Delta P_f = f_D \frac{L}{D} \frac{\rho V^2}{2} \quad (5)$$

where f_D is called the Darcy friction factor and is a complicated function of the Reynolds number and the relative wall roughness. L and D are respectively the length and the diameter of the pipe. The Darcy–Weisbach equation is valid for fully developed, steady state and incompressible flows. Head losses due to flow singularities ΔP_m are commonly termed minor head losses and can be expressed as:

$$\Delta P_m = K_m \frac{L}{D} \frac{\rho V^2}{2} \quad (6)$$

where K_m is the singular head loss coefficient. More generally, the global pressure losses are expressed as the sum of these two expressions:

$$\Delta P = f_D \frac{L}{D} \frac{\rho V^2}{2} + K_m \frac{L}{D} \frac{\rho V^2}{2} \quad (7)$$

although for complex flows f_D and K_m are difficult to determine independently. From an engineering point of view, it is convenient to use a discharge coefficient in an equivalent simpler configuration to characterize an element in a hydraulic circuit for which a pressure drop appears in a streamtube of velocity V . However, the determination of each contribution of singular and linear losses with their respective discharge coefficients in the swirler system turns out to be an intricate task. The main reason stems from the difficulty of determining clearly the relationship between f_D and K_m . In the case of swirlers, these relationships essentially result from the potential interactions between the different passages. Therefore, this study will remain concentrated only on the industrial objective which is to obtain a global estimation of head loss through this complex geometry. The global pressure loss will hence be evaluated from LES by the differential stagnation pressure between two points in the flow field:

$$\Delta P = \left(P + \frac{\rho V^2}{2} \right)_2 - \left(P + \frac{\rho V^2}{2} \right)_1 \quad (8)$$

subscript (1) being relative close to the swirler inlet (common to all passages) and subscript (2) relates to the combustion chamber.

3. LES of the KIAI burner

The objective of this section is to provide a detailed comparison of the two codes for the single burner configuration of the KIAI project. This is assured by keeping the numerical setup identical wherever possible. If exactly matching numerical settings are not possible due to code maturity or code design, default recommended settings are retained.

3.1. Description of the experimental setup: the KIAI burner

The burner configuration comprises four major components (cf. Fig. 1): A *plenum* which serves to tranquilize the flow before entering the injection system. A grid placed in the lower part of the plenum destroys the large structures of the flow initiated by the air feeding lines. Note that this grid is not taken into account in the numerical simulations. The *swirl injection system* is composed of two admissions. In the center a tube ($d = 4$ mm) acts as fuel injector, which is surrounded by a radial air swirler ($D = 20$ mm). The latter one is composed of 18 channels inclined at 45° . The *combustion chamber* has a square cross section with an edge length of 100 mm, assuring a symmetric flow field, and a total chamber length of 260 mm. Synthetic quartz is used to provide an optical access of 228×78 mm² on at least three sides of the chamber, allowing to perform diagnostics such as PIV and PLIF. Finally, the *convergent exhaust* avoids negative mean axial velocities. During the cold flow simulations, the temperature is at $T = 298$ K and the pressure in the combustion chamber is at ambient pressure $P = 101325$ Pa.

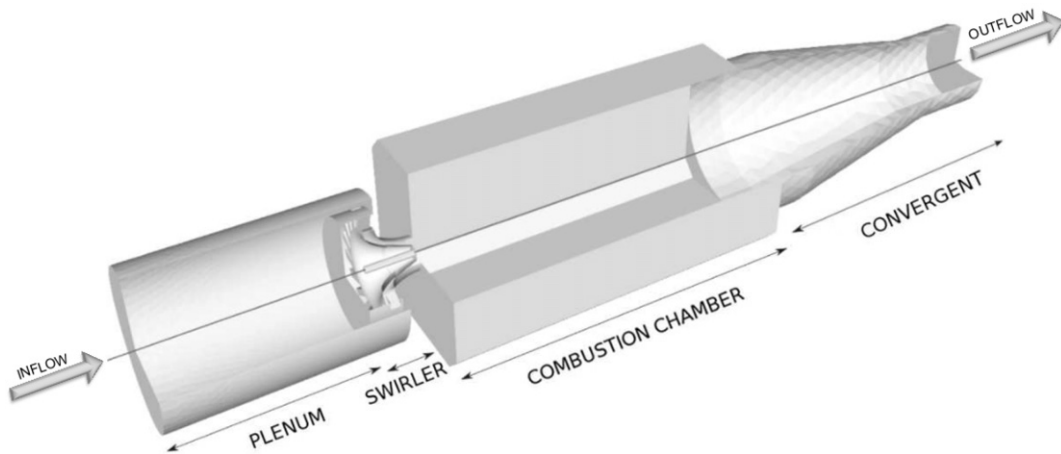
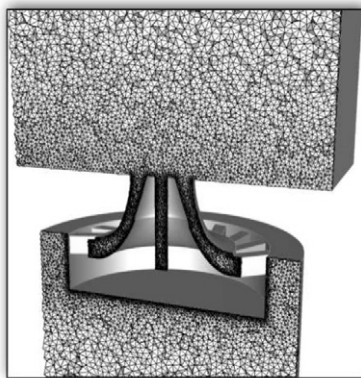


Fig. 1. Global view of the KIAI burner: computational domain retained for LES.

Table 1

Computational parameters of the different LES. Left: Computational mesh, Right: Computational parameters.



Numerical parameters	AVBP	YALES2
Numerical scheme	TTG4A	TRK4
CFL	0.7 (acoustic)	1.5 (convective)
SGS-model	WALE	Dynamic Smagorinsky
Boundary conditions		
Inlet swirler	$\dot{m} = 5.248 \cdot 10^{-3} \text{ kg s}^{-1}$	
Inlet jet	$\dot{m} = 0.2371 \cdot 10^{-3} \text{ kg s}^{-1}$	
Outlet	$p = 101325 \text{ Pa}$	
Central injection tube	Adiabatic slip wall	
Plenum	Adiabatic no-slip wall	
Combustion chamber	Adiabatic no-slip wall	
Swirler	Adiabatic no-slip wall	
Exhaust cone	Adiabatic no-slip wall	

3.2. Numerical setup

The mesh is unstructured, composed of 4 million tetrahedral elements, refined in the injector region, where the mesh size is set to 0.3 mm. The computational grid, the boundary conditions and the numerical setup are presented in Table 1. For the AVBP simulation, inlet and outlet conditions are of the characteristic NSCBC type [4], defined by imposing the volumetric mass flow rates and the pressure, respectively. The wall boundary conditions are specified as wall no-slip conditions on all walls except for the central injection and the surrounding crown for which a slip condition is used. AVBP provides high-order numerical schemes of the Taylor–Galerkin family, namely TTGC [11] and TTG4A [12,13]. The latter one is used for the simulations presented in the following. This finite-element scheme is fourth-order accurate in time and third-order accurate in space on uniform meshes. The WALE [14] model is used as subgrid scale model.

For the YALES2 simulations, the inlet and outlet boundary conditions are adapted to the low Mach number approach. Throughout the whole domain, the pressure gradient at the boundaries is set to 0. At the inlet, the volumetric mass flow rate is imposed. The *convective boundary condition* is used at the outlet [15]. YALES2 solves the incompressible Navier–Stokes equations with a projection method [16]. The first step of this fractional step method, which consists in computing a velocity predictor, is advanced explicitly in time with the TRK4 scheme [17], which is fourth-order accurate. The spatial discretization of YALES2 is also fourth-order accurate. For the closure of the subgrid-scales, the localized dynamic Smagorinsky model [18] is chosen.

3.3. Preliminary validations

The accuracy of the LES predictions is evaluated by comparing mean and fluctuation velocity profiles to experimental data for 5 axial positions (cf. Fig. 2) downstream of the swirler exit at $z/D = \{0.25, 0.5, 1, 1.5, 2\}$. Figs. 3 and 6 display the comparison of the different components of the velocity fields and RMS.

The profiles of the averaged axial and tangential velocity components are presented in Figs. 3(b) and 4(b). The magnitude of the mean velocity is globally close to experimental measurements. Differences occur near the central jet where the axial

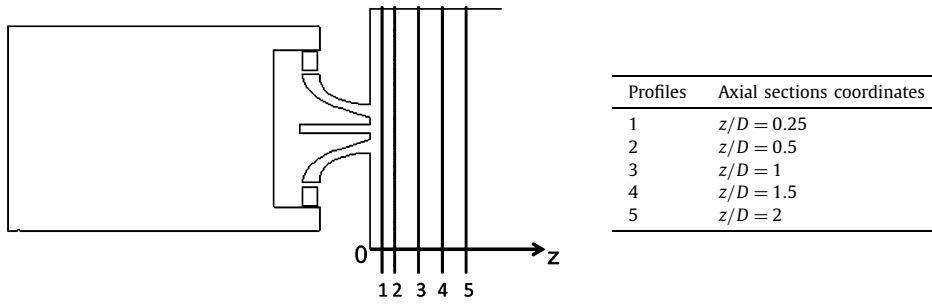


Fig. 2. Position of the measurement cross-sections $z/D = \{0.25, 0.5, 1, 1.5, 2\}$.

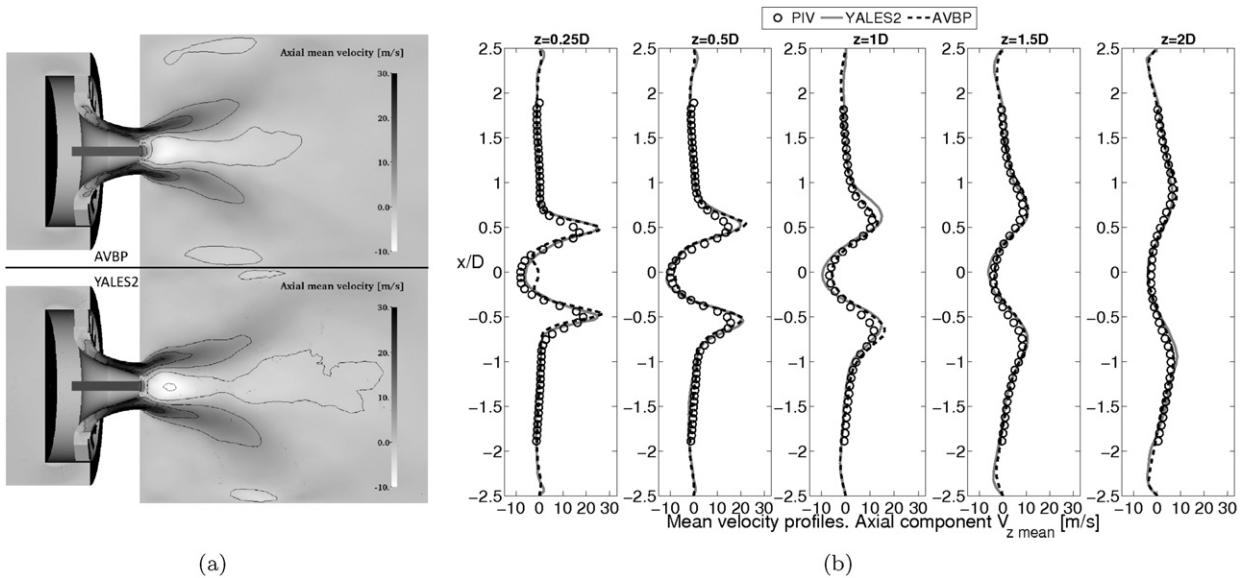


Fig. 3. (a) Comparison of the mean axial velocity fields obtained with the two solvers and (b) the mean axial velocity profiles compared to experimental data.

velocity peak is reproduced accurately by YALES2 and overestimated by AVBP. The sensitivity of the central zone leads to different predictions of the jet penetration in part due to the numerical approaches. Furthermore, both codes overpredict the lateral peaks of the tangential mean velocity. A similar behavior can be observed for the velocity fluctuation profiles shown in Figs. 5(b) and 6(b), which suitably follow experimental values but still overpredict measurements. Note that the computational grid remains too coarse for the no-slip condition, which requires a good refinement close to the wall to resolve accurately the boundary layers [19]. Regarding performance, the KIAI experimental burner represents a low-Mach number flow ($M_{injector} = 0.064$) and therefore the time needed for one through-flow is in favor to YALES2 which is approximately 10 times faster than AVBP for this simulation.

4. Pressure drop LES predictions

A crucial ingredient for many LES applications in internal flows is the capacity of the method to provide a correct prediction of the pressure drop, in particular in complex geometries. This part of the study consists in evaluating the influence of the grid resolution and wall treatment on the pressure loss predictions, produced by both linear and singular pressure losses through the swirler system. The probes, for which the mean quantities are evaluated are placed in relatively calm zones in the plenum and the chamber (cf. Fig. 7). At these points, the velocity field does not contribute to head losses so that the relative pressure drop is defined by Eq. (8).

The evolution of the stagnation pressure along a streamline obtained based on the AVBP prediction of this low Mach number flow (cf. Fig. 8) shows a decrease due to friction. In parallel, the dynamic pressure has increased because of the flow acceleration in the swirler system inducing a reduction of the static pressure. We can also notice that as fluid moves through the expansion area in the combustion chamber, the static pressure tends to the stagnation pressure where kinetic energy has become negligible. Finally, the injection system proves to be the location of mechanisms affecting the flow dynamics.

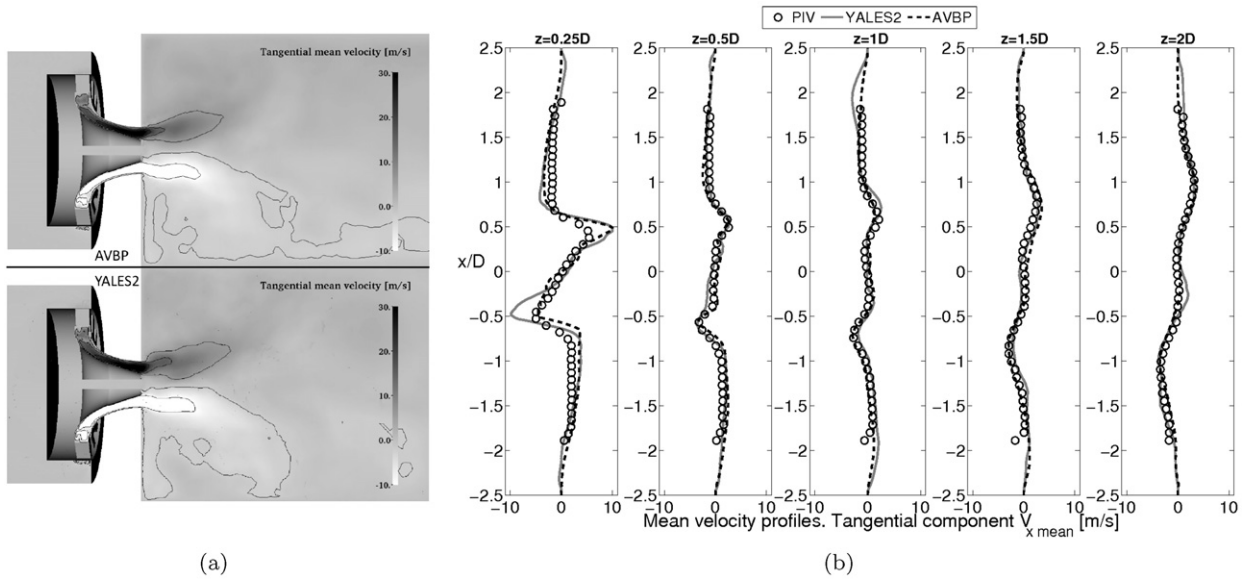


Fig. 4. (a) Comparison of the mean tangential velocity fields obtained with the two solvers and (b) the mean tangential velocity profiles compared to experimental data.

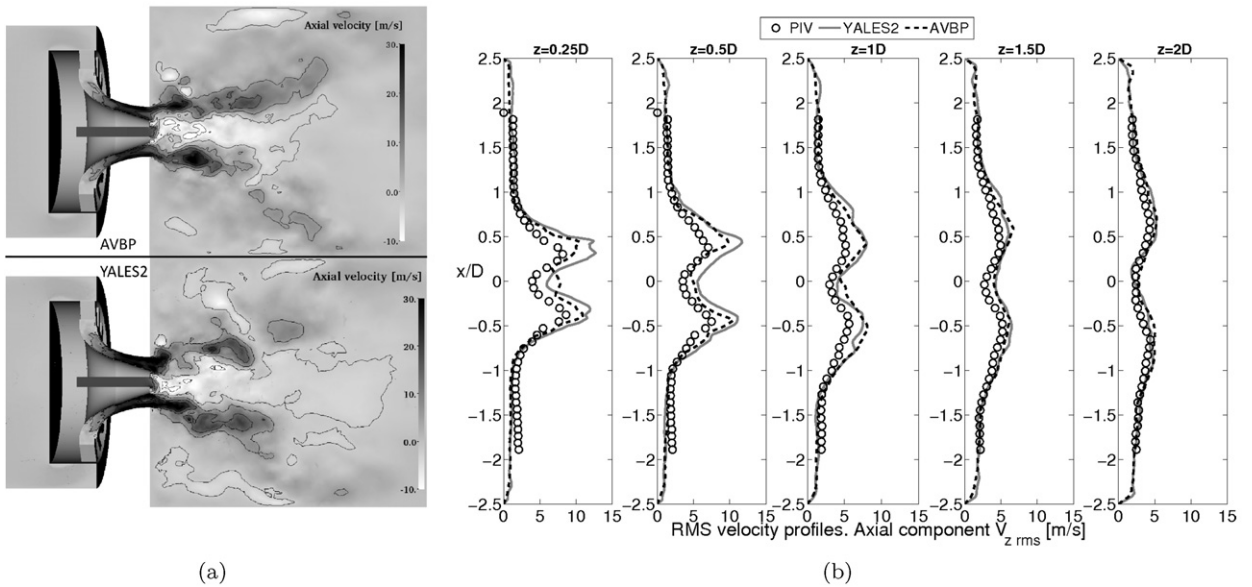


Fig. 5. (a) Comparison of the instantaneous axial velocity fields obtained with the two solvers and (b) the axial velocity fluctuation profiles compared to experimental data.

Numerical difficulties lie in the turbulence modeling of the near wall region usually used to evaluate the wall friction, which can then affect linear and singular losses. The quality of the mesh combined with a suitable boundary condition in the swirler is hence susceptible to be a critical contributor to the quality of the results. For a clearer understanding and an evaluation of grid/modeling issues, two boundary conditions associated with an adequate SGS model and several meshes are tested in Section 4.1.

4.1. Influence of the mesh and boundary conditions

The wall treatment combined with the mesh resolution is known to influence on the accuracy of the pressure loss prediction. Two strategies are relevant to LES: first, a wall resolved LES where all the scales of importance of the boundary layer [20] are aimed to be adequately resolved within the limits of the subgrid-scale model and second, a simulation using wall layer models to reproduce the flow close to solid boundaries. While the first approach is computationally intensive, the

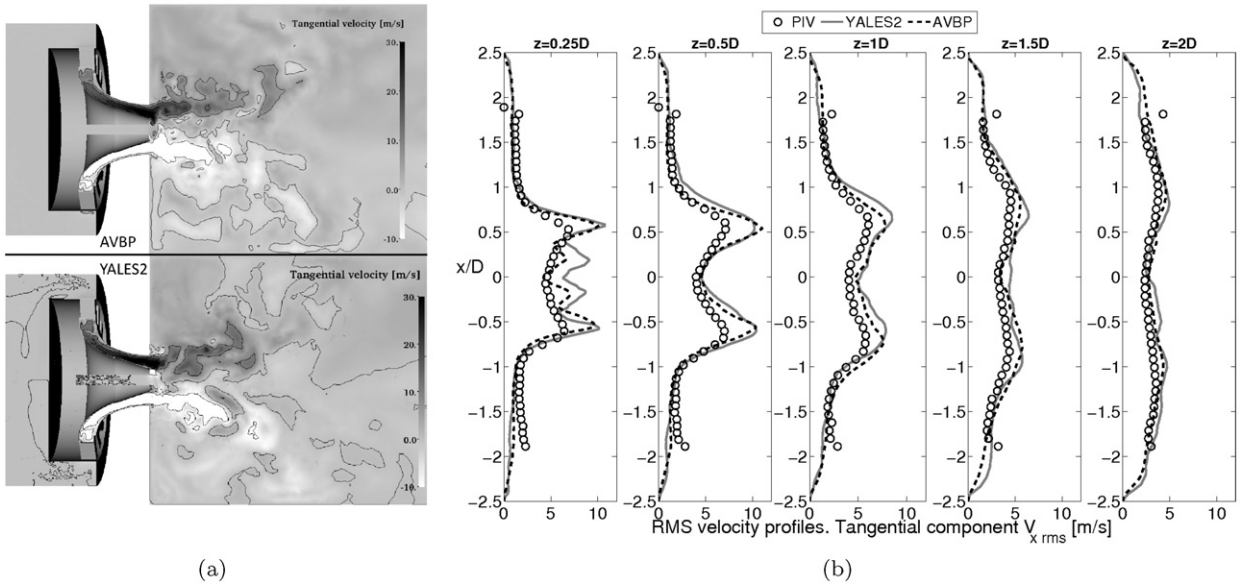


Fig. 6. (a) Comparison of the instantaneous tangential velocity fields obtained with the two solvers and (b) the tangential velocity fluctuation profiles compared to experimental data.



Fig. 7. Probe locations for the pressure drop determination.

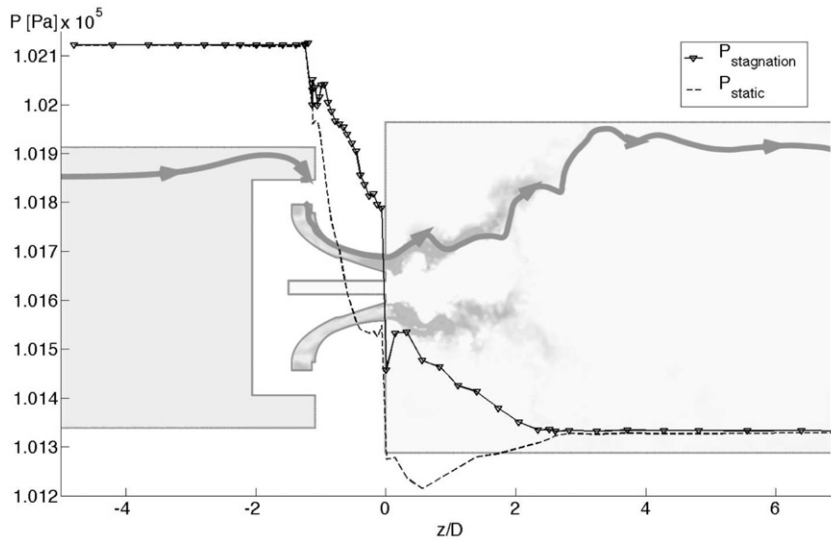


Fig. 8. Evolution of the stagnation pressure and static pressure along a streamline (gray shaded solid line).

second one is subject to all the hypotheses needed to derive the log-law. To reduce the computational costs, the commonly chosen strategy is to decrease the refinement close to the wall and use a wall law model [21]. However, note that a conflict may occur between a wall law, which demands grid cells that lie in the logarithmic layer (typically $\Delta y^+ \approx 100$ where a stationary quasi 1D flow is assumed) and LES, which is fully unsteady and demands very small, relatively isotropic grid cells that diminish in size towards the wall. Therefore, the comparison of the wall law (WL) and the no-slip wall

Table 2
Wall mesh resolutions used for the cold flow simulations (reference case in bold).

MESH	M1	M2	M3	M4
Characteristics	Tetra 2M	Tetra 4M	Tetra 24	Tetra 35M
y^+	~60	~30	~20	~15

Table 3
Summary of the pressure drop predictions – experimental pressure loss $\Delta P_{exp} = 594$ Pa.

Pressure drop predictions ΔP [Pa]				
Configuration	AVBP		YALES2	
	No-slip wall	Wall law	No-slip wall	Wall law
Tetra Mesh 2M	1220	800	1200	/
Tetra Mesh 4M	945	790	1010	740
Tetra Mesh 24M	900	700	/	/
Tetra Mesh 35M	/	/	915	/

formulation (*WNS*) are considered for four meshes, whose main characteristics are summarized in Table 2. All meshes are unstructured with tetrahedral elements. The indicated y^+ are the average values of the dimensionless wall distance within the air admission of the swirler. All numerical parameters are identical to the first test cases (cf. Table 1) except for boundary conditions and SGS models. Indeed, it was demonstrated in our case that a better turbulence model (WALE) leads to worse results when used in conjunction with a wall function approach because of an apparent incompatibility [22]. Theoretically, a wall law stems from Reynolds-averaged Navier–Stokes (RANS) technique and is not conceived for LES. A novel concept for the near-wall treatment of wall modeled LES has been recently presented by modifying the LES eddy-viscosity using a dynamic correction based on the resolved turbulent stress near the wall [23–25]. Such researches are however still under development and remains outside of the scope of this work.

4.2. Results and discussion

Before investigating the pressure drop predictions, the LES results are first evaluated by comparing mean axial and tangential velocity profiles to experimental data at $z/D = 0.25$ (cf. Fig. 9).

The no-slip condition requires a good refinement close to the wall to resolve accurately the boundary layers. An impact of this local increase in resolution is seen in the magnitude of the main velocity peak at the jet exit which is clearly affected by this parameter. It is only reproduced with high accuracy with a refined mesh otherwise it is overestimated. For tangential velocities, the mesh refinement has no real influence and all predictions follow the same trend. The lateral mean peaks are globally overestimated compared with experimental results except for the YALES2 simulation using the refined mesh *M4*. Both observations confirm the assumption that a poorly resolved mesh cannot reproduce the physics correctly.

Use of a wall-model shows that the central peak magnitude remains over-estimated for the axial mean velocity on the coarse mesh *M1* as well as on the refined one *M3*. LES establishes a compromise to integrate wall models coherently into a standard LES by requiring a computational grid small enough to capture a sufficient number of turbulent structures as well as large enough to justify the application of a wall model. The wall model demands relatively large grid cells that reach into the logarithmic layer. Note that the characteristic mesh size of mesh *M3* ($y^+ \sim 20$) is in the intermediate part ($5 < y^+ < 30$) of the boundary layer: i.e. between the logarithmic and the linear law domain. The wall law may therefore not correctly model the boundary layer and have an impact on axial velocity profiles near the injector system. Note that experimental uncertainties have also been reported in this specific flow region.

After having analyzed the influence of some parameters on the topology of the flow, this remaining part is dedicated to the influence of the modeling on the determination of the pressure loss. The experimental pressure loss measured by CORIA equals $\Delta P_{exp} = 594$ Pa [26] with an uncertainty of 3 percent. Figs. 10(a) and 10(b) display the evolution of the pressure drop along the central axis with the use of the no-slip wall boundary condition while Figs. 10(c) and 10(d) show the pressure loss profiles with the use of a wall law. First, the results reveal the same trend for both codes. The mesh quality is also seen to have a crucial influence on the accuracy of pressure loss predictions notably with a no-slip boundary condition. Similarly to the remarks made previously regarding the velocity profiles, the determination of pressure losses is directly related to the computational grid resolution combined with the boundary condition. Pressure drop results are summarized in Table 3.

Fig. 11 shows the evolution of the pressure loss as a function of the mean computational y^+ in the swirler. For both codes a quasi linear decrease of the pressure loss towards the experimental finding is observed for the no-slip boundary condition. For equivalent y^+ , the pressure drop estimation is clearly improved if the wall-model is used and proves to be very effective in the logarithmic law domain. In the intermediate part of this model application (here with $y^+ \sim 20$), the boundary layer may not be correctly modeled but results turn out to be better in part because of the number of points for which y^+ is in the linear regime (a switch being included in the wall law formulation).

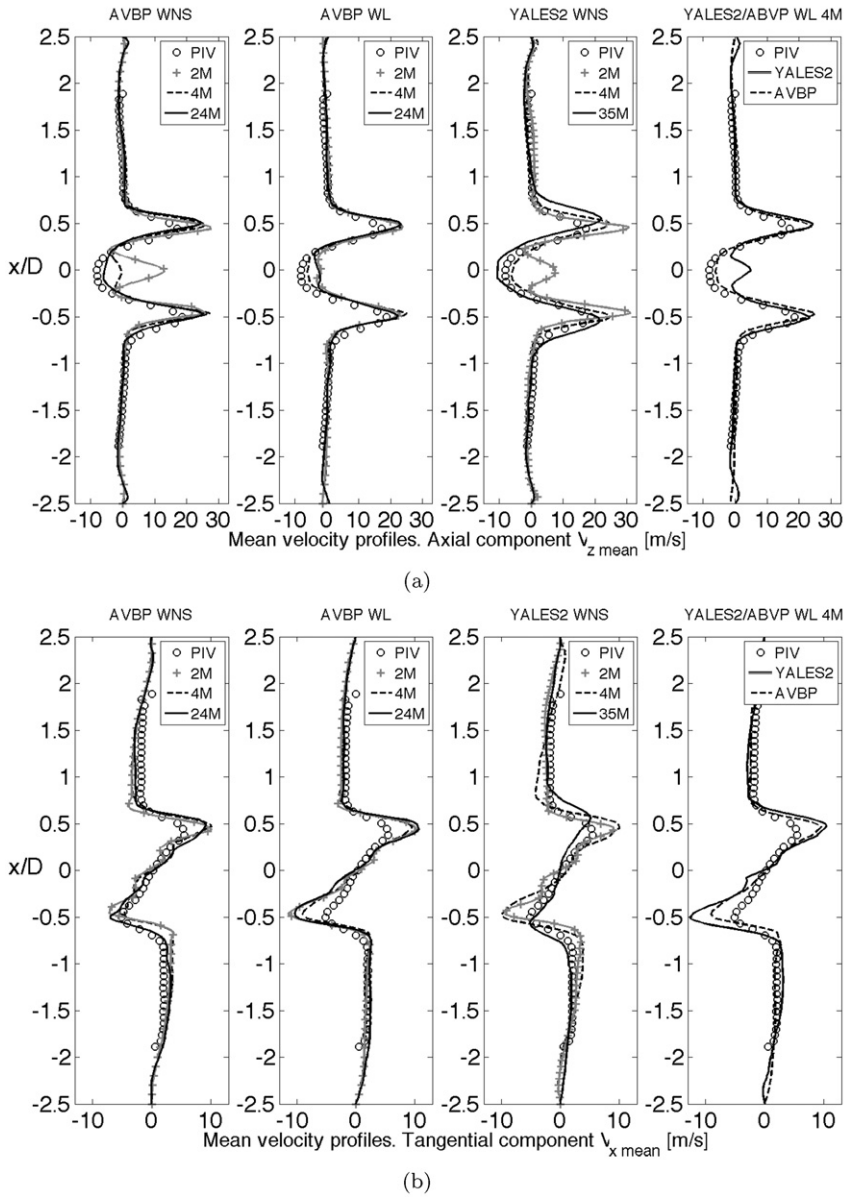


Fig. 9. Influence of the mesh (cf. Table 2) and boundary conditions on the mean axial (a) and tangential (b) velocity profiles at $z/D = 0.25$. The following notations apply: Wall Law (WL) and the No-Slip Wall formulation (WNS).

5. Conclusion and perspectives

LES of a single swirler system is reported under cold flow conditions using the low Mach number code YALES2 and the compressible AVBP code. Flow predictions show that calculations performed for this low Mach number case are appropriate for the mean flow. From a strategic point of view, a no-slip boundary condition requires a mesh refinement of high quality to resolve accurately the boundary layers. Therefore, the use of a wall law model turns out to be a good way to determine approximatively the pressure loss by resolving the problem on a reasonable mesh in terms of discretization. Regarding the global error of the pressure loss prediction, the gain in terms of precision is considerable (with an error near 15% when taking into account the experimental uncertainty). However, it needs to be underlined that the wall law approach suffers from theoretical limitations and may lead to a lack of accuracy in some cases. New perspectives are conceivable by using more sophisticated models such as the implementation method based on the conjugation of wall functions and no-slip condition at the wall, leading to the necessity of using hexahedral or prismatic meshes in near-wall regions [22]. This technique could turn out to be advantageous in terms of the overall number of cells, because the near-wall grid refinement can easily be controlled by adapting the prism aspect ratio without leading to an excessive number of near-wall tetrahedra.

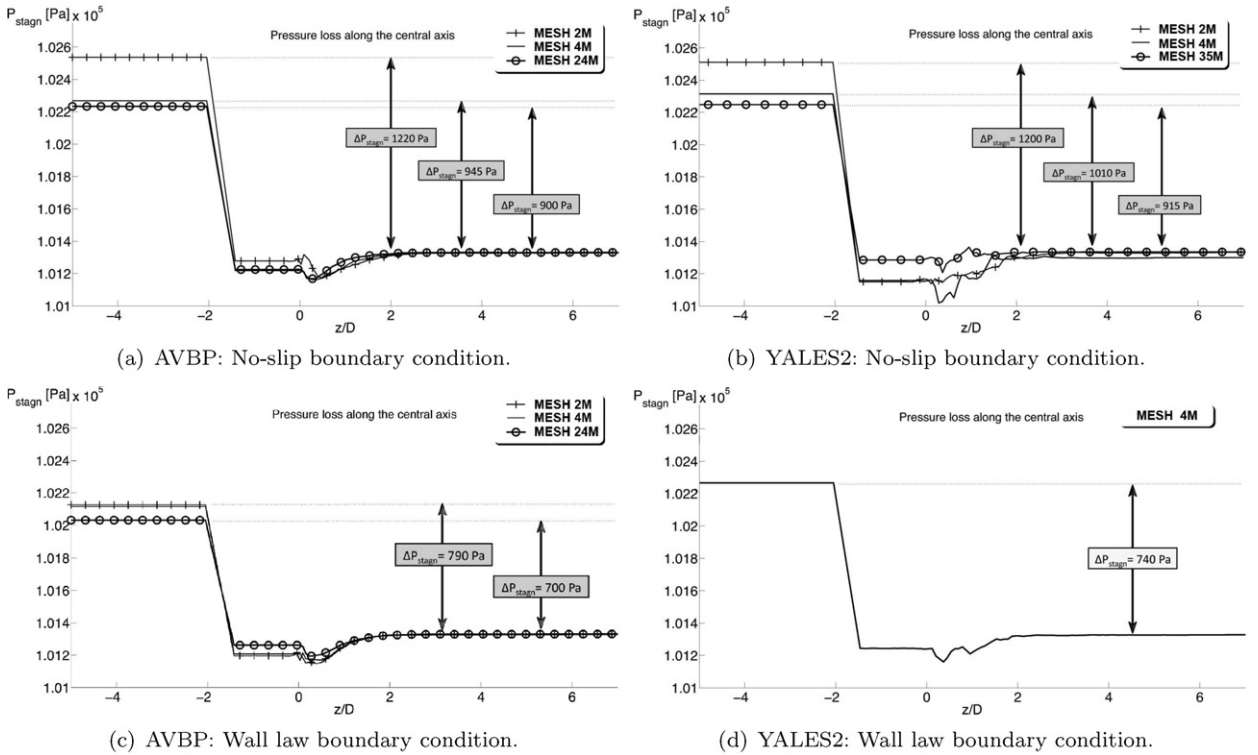


Fig. 10. Influence of the mesh refinement on the pressure loss distribution along the central axis of the configuration: (a) and (c) with the use of a no-slip boundary condition, (b) and (d) with the use of a wall law boundary condition.

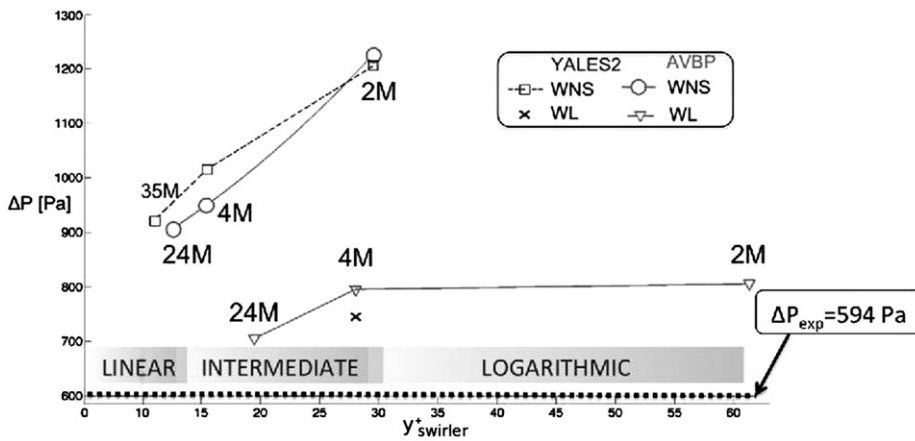


Fig. 11. Evolution of the pressure loss as function of the average values of the dimensionless wall distance y^+ : with the use of a no-slip boundary condition (WNS) and the use of a wall law boundary condition (WL).

Acknowledgements

The research leading to these results has received funding from the European Community’s Seventh Framework Program (FP7/2007-2013) under Grant Agreement n° ACP8-GA-2009-234009. This study is part of the 4-year KIAL project started in May 2009, a European initiative financed under the FP7 and which addresses innovative solutions for the development of new combustors in aero-engines. It aims at providing low NOx methodologies to be applied to design these combustors.

References

[1] M. Rudgyard, Integrated preprocessing tools for unstructured parallel cfd applications, Technical report TR/CFD/95/08, CERFACS, 1995.
 [2] R.-H. Ni, A multiple grid scheme for solving the Euler equations, Am. Inst. Aeronaut. Astronaut. J. 20 (1982) 1565–1571.
 [3] G. Lartigue, Simulation aux grandes échelles de la combustion turbulente, PhD thesis, INP Toulouse, 2004.

- [4] T. Poinso, S. Lele, Boundary conditions for direct simulations of compressible viscous flows, *J. Comput. Phys.* 101 (1) (1992) 104–129.
- [5] V. Moureau, G. Lartigue, Y. Sommerer, C. Angelberger, O. Colin, T. Poinso, Numerical methods for unsteady compressible multi-component reacting flows on fixed and moving grids, *J. Comput. Phys.* 202 (2) (2005) 710–736.
- [6] V. Moureau, P. Domingo, L. Vervisch, Design of a massively parallel cfd code for complex geometries, *C. R. Mécanique* 339 (2–3) (2011) 141–148.
- [7] V. Moureau, YALES2 home page on, www.coria-cfd.fr.
- [8] V. Moureau, P. Domingo, L. Vervisch, From large-eddy simulation to direct numerical simulation of a lean premixed swirl flame: Filtered laminar flame-pdf modeling, *Combust. Flame* 158 (7) (2011) 1340–1357.
- [9] J. Laufer, United States, National Advisory Committee for Aeronautics, The structure of turbulence in fully developed pipe flow, NACA, 1953.
- [10] J. Weisbach, *Die Experimental-Hydraulik*, Engelhardt, 1855.
- [11] O. Colin, M. Rudgyard, Development of high-order Taylor–Galerkin schemes for unsteady calculations, *J. Comput. Phys.* 162 (2) (2000) 338–371.
- [12] L. Quartapelle, V. Selmin, High-order Taylor–Galerkin methods for nonlinear multidimensional problems, *Finite Elem. Fluids* 76 (1993) 90.
- [13] J. Donea, A. Huerta, *Finite Element Methods for Flow Problems*, Wiley, 2003.
- [14] F. Ducros, F. Nicoud, T. Poinso, Wall-adapting local eddy-viscosity models for simulations in complex geometries, in: M.J. Baines (Ed.), *Numerical Methods for Fluid Dynamics VI*, 1998, pp. 293–299.
- [15] Laura L. Pauley, Parviz Moin, William C. Reynolds, The structure of two-dimensional separation, *J. Fluid Mech.* (1990) 397–411.
- [16] A.J. Chorin, Numerical solution of the Navier–Stokes equations, *Math. Comput.* 22 (104) (1968) 745–762.
- [17] M. Kraushaar, Application of the compressible and low-Mach number approaches to Large-Eddy Simulation of turbulent flows in aero-engines, PhD thesis, Université de Toulouse, 2011.
- [18] M. Germano, U. Piomelli, P. Moin, W.H. Cabot, A dynamic subgrid-scale eddy viscosity model, *Phys. Fluids A Fluid Dyn.* 3 (7) (1991) 1760–1765.
- [19] J. Jimenez, P. Moin, The minimal flow unit in near-wall turbulence, *J. Fluid Mech.* 225 (213–240) (1991).
- [20] J. Kim, P. Moin, R. Moser, Turbulence statistics in fully developed channel flow at low Reynolds number, *J. Fluid Mech.* 177 (1987) 133–166.
- [21] U. Piomelli, E. Balaras, H. Pasinato, K.D. Squires, P.R. Spalart, The inner–outer layer interface in large-Eddy simulations with wall-layer models, *Int. J. Heat Fluid Flow* 24 (4) (August 2003) 538–550.
- [22] F. Jaegle, O. Cabrit, S. Mendez, T. Poinso, Implementation methods of wall functions in cell-vertex numerical solvers, *Flow Turbul. Combust.* 85 (2) (2010) 245–272.
- [23] M. Wang, P. Moin, Computation of trailing-edge flow and noise using large-Eddy simulation, *Am. Inst. Aeronaut. Astronaut. J.* 38 (12) (2012).
- [24] J.A. Templeton, G. Medic, G. Kalitzin, An eddy-viscosity based near-wall treatment for coarse grid large-Eddy simulation, *Phys. Fluids* 17 (2005) 105101.
- [25] S. Bocquet, P. Sagaut, J. Jouhaud, A compressible wall model for large-Eddy simulation with application to prediction of aerothermal quantities, *Phys. Fluids* 24 (2012) 065103.
- [26] J.P. Frenillot, Etude phénoménologique des processus d’allumage et de stabilisation dans les chambres de combustion turbulente swirlées, PhD thesis, CORIA, 2011.