

Physics/Mathematical physics, theoretical physics

Corrigendum to the Note “Time inversion in the representation analysis of magnetic structures” [C. R. Physique 6 (2005) 375–384]

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In the article [1], the magnetic little group $G_{\mathbf{k}}^{\ominus}$ of the \mathbf{k} vector was introduced. It was correctly stated that the operators of $G_{\mathbf{k}}^{\ominus}$ act on a space whose dimension (or number of basis vectors) is twice as large than for the ordinary little group $G_{\mathbf{k}}$. Unfortunately, it was incorrectly stated that when the magnetic corepresentation and the irreducible corepresentations are real, one can choose real basis vectors and this remove the factor two. As a matter of fact, this reduction is not possible. However, the method proposed in [1] can be used, but the results, in the case of a ‘black and white’ group, may be different.

In the example of CeAl_2 treated in [1], the transformation operators of $G_{\mathbf{k}}^{\ominus}$ act on $\mathbf{m}_{j\alpha}^{\mathbf{k}}$ and $\mathbf{m}_{j\alpha}^{-\mathbf{k}}$, i.e., on 12 components. The corresponding corepresentation $c\Gamma$ is therefore of dimension 12. Table 8 of [1] has to be corrected as follows:

- (i) The caption should be “action of the operators of $G_{\mathbf{k}}^{\ominus}$ on the components $\mathbf{m}_{j\alpha}^{\mathbf{k}}$ and $(\mathbf{m}_{j\alpha}^{\mathbf{k}})^*$ of CeAl_2 ”;
- (ii) in the last two columns, the components $\mathbf{m}_{j\alpha}^{\mathbf{k}}$ should be replaced by $(\mathbf{m}_{j\alpha}^{\mathbf{k}})^*$;
- (iii) 6 additional lines should be inserted, which describe the action of the 4 operators on the 6 components $(\mathbf{m}_{j\alpha}^{\mathbf{k}})^*$;
- (iv) in the last line the character χ is 12 for h_1 (instead of 6) and 0 for the other 3 operators.

The decomposition of the corepresentation is

$$c\Gamma = 3c\tau_1^+ + 3c\tau_1^- + 3c\tau_2^+ + 3c\tau_2^-$$

The basis vectors for each irreducible corepresentation $c\tau_v^{\pm}$ are:

$$\mathbf{m}_{v\pm}^{\mathbf{k}1} = (\mathbf{m}_{1x}^{\mathbf{k}} + \varepsilon' \mathbf{m}_{2y}^{\mathbf{k}}) + \varepsilon (\mathbf{m}_{1y}^{\mathbf{k}} + \varepsilon' \mathbf{m}_{2x}^{\mathbf{k}})^*; \quad \mathbf{m}_{v\pm}^{\mathbf{k}2} = \varepsilon (\mathbf{m}_{v\pm}^{\mathbf{k}1})^*; \quad \mathbf{m}_{v\pm}^{\mathbf{k}3} = (\mathbf{m}_{1z}^{\mathbf{k}} + \varepsilon' \mathbf{m}_{2z}^{\mathbf{k}}) + \varepsilon (\mathbf{m}_{1z}^{\mathbf{k}} + \varepsilon' \mathbf{m}_{2z}^{\mathbf{k}})^*$$

where $\varepsilon = +1$ for $c\tau_v^+$, $\varepsilon = -1$ for $c\tau_v^-$ and where $\varepsilon' = -1$ for $c\tau_1^{\pm}$ and $\varepsilon' = +1$ for $c\tau_2^{\pm}$. Contrarily to what was written in [1], corepresentations $c\tau_1^+$ and $c\tau_1^-$ are equivalent (as well as $c\tau_2^+$ and $c\tau_2^-$).

The magnetic structure, as deduced from the experiment, corresponds to corepresentation $c\tau_1^+$. It is defined by:

$$m_{2x}^{\mathbf{k}} = -m_{1y}^{\mathbf{k}}; \quad m_{2y}^{\mathbf{k}} = -m_{1x}^{\mathbf{k}}; \quad m_{2z}^{\mathbf{k}} = -m_{1z}^{\mathbf{k}}$$

in agreement with [1]. However, the additional condition [1] $m_{1x}^{\mathbf{k}} = m_{1y}^{\mathbf{k}}$ is wrong and should be replaced by

$$m_{1x}^{\mathbf{k}} = \varepsilon (m_{1y}^{\mathbf{k}})^*$$

Concerning CeAl₂, this replacement is the essential point of this appendix.

More details will be presented elsewhere [2].

Acknowledgements

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References

- [1] J. Schweizer, C. R. Physique 6 (2005) 375–384.
- [2] J. Schweizer, J. Villain, A.B. Harris, in preparation.