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Superconductivity of strongly correlated systems / Supraconductivité des systèmes fortement corrélés

NMR studies on iron-pnictide superconductors:  $LaFeAs(O_{1-x}F_x)$  and  $BaFe_2(As_{1-x}P_x)_2$ 

Études par RMN des supraconducteurs pnictures à base de fer LaFeAs $(O_{1-x}F_x)$ et BaFe<sub>2</sub> $(As_{1-x}P_x)_2$ 

Kenji Ishida<sup>a,b,\*</sup>, Yusuke Nakai<sup>a,b</sup>, Shunsaku Kitagawa<sup>a,b</sup>, Tetsuya Iye<sup>a,b</sup>

<sup>a</sup> Department of Physics, Graduate School of Science, Kyoto University, Kyoto 606-8502, Japan

<sup>b</sup> Transformative Research-project on Iron Pnictides (TRIP), Japan Science and Technology Agency (JST), Sanban-cho bldg., 5, Sanban-cho, Chiyoda, Tokyo 102-0075, Japan

ARTICLE INFO

*Article history:* Available online 25 May 2011

Keywords: Nuclear magnetic resonance Iron pnictides superconductors Pairing mechanism Order parameter symmetry

Mots-clés :

Résonance magnétique nucléaire Supraconducteurs pnictures à base de fer Mécanisme d'appariement Symétrie du paramètre d'ordre

### ABSTRACT

This review presents a summary of our NMR experiments on LaFeAs( $O_{1-x}F_x$ ) and BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>. The authors introduce the key NMR experimental results which reveal their physical properties in the normal and superconducting states. From the comparison of the NMR results between the two systems, we point out that the superconducting gap structure and the relationship between superconductivity and magnetic fluctuations probed with NMR are quite different between the two systems.

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# RÉSUMÉ

Cet article de revue couvre nos résultats obtenus par RMN sur les supraconducteurs pnictures à base de fer LaFeAs $(O_{1-x}F_x)$  et BaFe $_2(As_{1-x}P_x)_2$ . Nous introduisons les mesures clefs qui ont sondé leurs propriétés tant normales que supraconductrices. La comparaison des deux systèmes montre que la structure du gap supraconducteur ainsi que la relation entre supraconductivité et fluctuations magnétiques, telles que vue par la RMN, sont très différentes dans les deux cas.

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### 1. Introduction

The discovery of iron-oxypnictide superconductor LaFeAs( $O_{1-x}F_x$ ) with  $T_c = 26$  K [1] surprised physicists and chemists studying superconductivity all over the world. This is because Fe metal is a ferromagnet and the Fe site is thought to play an important role for such an unexpectedly high  $T_c$ . Shortly after this discovery, application of pressure increases  $T_c$ in LaFeAs( $O_{1-x}F_x$ ) even further to 43 K [2], and the replacement of the nonmagnetic La by magnetic rare earth elements enhances  $T_c$  up to 56.3 K, which is the current record of the iron-pnictide superconductor [3–6]. This extraordinary high  $T_c$ attained by iron-based superconductors has demonstrated that high- $T_c$  superconductivity is more general than previously thought. It is quite important to investigate physical properties of the iron-pnictide superconductivity in order to understand the mechanism of high- $T_c$  superconductivity.

<sup>\*</sup> Corresponding author at: Department of Physics, Graduate School of Science, Kyoto University, Kyoto 606-8502, Japan. *E-mail address:* kishida@scphys.kyoto-u.ac.jp (K. Ishida).

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Fig. 1. Crystal structures (a) LaFeAsO (refereed to as "1111" in the article) and (b) BaFe<sub>2</sub>As<sub>2</sub> ("122").

We have studied normal and superconducting (SC)-state properties on two iron-pnictide systems; LaFeAs( $O_{1-x}F_x$ ) with the "1111" structure [7–9] and BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> with the "122" structure [10,11]. Their crystal structures are shown in Fig. 1.

Superconductivity in the two systems appears upon F- or P-doping in close proximity to parent phases which exhibit stripe-type antiferromagnetic (AFM) order, along with structural distortion from tetragonal to orthorhombic phases [12,13,7]. Then it is natural to inquire an interplay between superconductivity and spin fluctuations associated with the magnetic ordering. In addition, since electron–phonon coupling is too weak to account for the high  $T_c$  [14], it has been invoked that the spin fluctuations due to nesting between the disconnected Fermi surfaces (FSs) are the source of the pairing interaction [15–17]. We consider that investigations on doping dependence of the normal and SC state properties will provide crucial information concerning the relationship between superconductivity and spin fluctuations in the iron-pnictide superconductor.

In this article, we review our NMR studies on LaFeAs $(O_{1-x}F_x)$  and BaFe<sub>2</sub> $(As_{1-x}P_x)_2$ , which have been performed to investigate systematic evolution of spin fluctuations in the two systems. Our NMR results show that the SC gap structure and the relationship between superconductivity and spin fluctuations probed by NMR measurements are quite different between LaFeAs $(O_{1-x}F_x)$  and BaFe<sub>2</sub> $(As_{1-x}P_x)_2$ , although superconductivity emerges in the similar situation.

### 2. Experimental results

### 2.1. NMR in LaFeAs( $O_{1-x}F_x$ ) [7–9]

Superconductivity in LaFeAs( $O_{1-x}F_x$ ) emerges at around x = 0.04. The F-doping, corresponding to electron doping, suppresses the nesting between hole and electron pocket FSs and would alter the low-lying excitations originating from the nesting-related magnetic fluctuations. We performed systematic studies on LaFeAs( $O_{1-x}F_x$ ) through <sup>75</sup>As and <sup>139</sup>La NMR in a wider F-doping range in order to understand the entire nature of the spin dynamics upon F-doping.

Polycrystalline samples of LaFeAs( $O_{1-x}F_x$ ) (x = 0.0, 0.04, 0.07, 0.11, 0.14) synthesized by solid-state reactions [1] were ground into a powder for the NMR measurements. All the samples were examined using powder X-ray diffraction (XRD; Bruker D8 Advance TXS) with Cu K $\alpha$  radiation, indicating that all the samples are mostly composed of a single phase. The contents of the dopant (x) were determined from lattice constants using Vegard's volume rule [18]. Electrical resistivity ( $\rho$ ) measurements were performed using a usual four-probe technique, and the temperature dependence of  $\rho$  in these samples is shown in Fig. 2. The  $T_c$ 's determined from the zero-resistivity are 16.3, 22.5, 22.5, 12.5 K for x = 0.04, 0.07, 0.11, 0.14, and the  $T_c$  determined by the onset of the Meissner signal are 17.5, 22.5 and 22.7 K for x = 0.04, 0.07 and 0.11, respectively. Two independent measurements reasonably coincide with each other.

### 2.1.1. Undoped LaFeAsO

Fig. 3 shows <sup>139</sup>La (I = 7/2)-NMR spectra for undoped LaFeAsO obtained by sweeping an external field at a fixed frequency 15.35 MHz. In general, when an electric field gradient is present at the La site, a La NMR spectrum consists of seven peaks arising from ( $m \leftrightarrow m - 1$ ) (m = 7/2, 5/2, ... and -5/2) transitions due to the electric-quadrupole interaction [19]. However, a quite different <sup>139</sup>La NMR spectrum is observed in the undoped LaFeAsO at 10 K; the central peak arising from the  $1/2 \leftrightarrow -1/2$  transition is split due to internal magnetic field at the La site. With increasing temperature, the splitting of the NMR spectrum denoted by the two red arrows in Fig. 3 decreases gradually and typical powder-pattern spectra consisting of seven transitions were observed above 150 K. The observed spectrum for the undoped LaFeAsO suggests an antiferromagnetic ordering below ~ 150 K, which is consistent with an anomaly of the electrical resistivity and susceptibility around 150 K [1]. Similar temperature variation of the <sup>139</sup>La-NMR spectra in LaFeAsO was also observed by Mukuda et al. [20]. The <sup>139</sup>La NMR spectrum clearly indicates that the undoped LaFeAsO is in a magnetically ordered state below ~ 150 K.



**Fig. 2.** The temperature dependence of resistivity  $\rho$  in LaFeAs(O<sub>1-x</sub>F<sub>x</sub>) [8]. The insert is the plot of  $\rho$  against  $T^2$ . Copyright 2009, the IOP Publishing Ltd.



**Fig. 3.** Field-sweep <sup>139</sup>La-NMR spectra at a series of temperatures through  $T_N \sim 142$  K in undoped LaFeAsO [8]. The spectra have been offset vertically. The arrows indicate the fields at which we measured the internal magnetic field. (For interpretation of the references to color in this figure, the reader is referred to the web version of this article.) Copyright 2009, the IOP Publishing Ltd.



**Fig. 4.** *T*-dependence of  $1/T_1$  of <sup>139</sup>La ( $\bigcirc$ ) and the internal magnetic field ( $\textcircled{\bullet}$ ) of undoped LaFeAsO (x = 0) [8]. The dotted line is a fit to the SCR theory for weak itinerant antiferromagnets (see text). Copyright 2009, the IOP Publishing Ltd.

The internal field at the La site arises from the hyperfine field from adjacent Fe atoms, and is related with the Fe ordered moments. The internal field  $H_{int}$  determined from the half width of the splitting is shown in Fig. 4 (filled circles). From the As-NMR study on single-crystal BaFe<sub>2</sub>As<sub>2</sub> shown later, it was revealed that the *c*-axis internal field arises at the As site in the ordered state with the stripe-type magnetic structure [21,22] suggested from the neutron-scattering measurement [12]. Thus, the direction of  $H_{int}$  is considered to be the *c*-axis, since the La site is the same geometrical configuration as the As site with respect to the magnetic Fe site. The dashed line in Fig. 4 is a fitting to the following



**Fig. 5.** *T*-dependence of  $1/T_1$  of <sup>139</sup>La, resistivity ( $\rho$ ) and *T* derivative of  $\rho$  ( $d\rho/dT$ ) in LaFeAsO in the *T* range of 100–200 K [8]. Copyright 2009, the IOP Publishing Ltd.

expression,  $M(T)/M_0 = [1 - (T/T_N)]^{0.15}$ . The growth of  $M(T)/M_0$  below  $T_N$  is much steeper than the 3D mean field value (0.5), and the transition to the antiferromagnetic state is almost first-order like. We consider that two-dimensionality of magnetic fluctuations is also responsible for the reduced value of the critical exponent, since similar rapid growth was actually reported in the cuprate antiferromagnet La<sub>2</sub>CuO<sub>4</sub> with a critical exponent  $\beta \sim 0.1$  [23], which possesses magnetic fluctuations with 2D nature.

Further insight into the magnetic properties in the undoped LaFeAsO is obtained from  $1/T_1$  measurements. Fig. 4 shows the temperature dependence of  $1/T_1$  of <sup>139</sup>La, which was measured at H = 2.54 T in the <sup>139</sup>La NMR spectrum.  $1/T_1$  exhibits a divergence at  $T_N = 142$  K, and the overall temperature dependence of  $1/T_1$  in Fig. 4 is fitted to the SCR theory for weak itinerant antiferromagnets [24]:

$$\frac{1}{T_1} = \begin{cases} aT + bT/\sqrt{T - T_N}, & T > T_N \\ cT/M(T), & T < T_N \end{cases}$$
(1)

where  $a = 0.005 \text{ s}^{-1} \text{ K}^{-1}$ ,  $b = 0.13 \text{ s}^{-1} \text{ K}^{-1/2}$  and  $c/M_0 = 0.02 \text{ s}^{-1} \text{ K}^{-1}$  are fitting parameters, and  $M(T) = M_0(1 - T/T_N)^{0.15}$  is an antiferromagnetic order parameter as mentioned above. The first term in (1) comes from usual Korringa relaxation expected in a metal. It is noteworthy that  $1/T_1$  related to the *q*-averaged dynamical susceptibility shows a divergence at 142 K whereas a clear anomaly is not observed in the static susceptibility. These are the characteristic features of an itinerant antiferromagnet observed in V<sub>3</sub>Se<sub>4</sub>, in which the ordered **q**-vector is far from **q** = 0 [25].

Although the SCR expression roughly captures the behavior of  $1/T_1$  in the undoped LaFeAsO, the sharp decrease of  $1/T_1$  below  $T_N$  cannot be reproduced by the expression. The discontinuous decrease of  $1/T_1$  and abrupt increase of  $H_{int}$  was observed in single-crystal BaFe<sub>2</sub>As<sub>2</sub> and CaFe<sub>2</sub>As<sub>2</sub> [21,22,26] in which the structural and magnetic transitions occurs simultaneously with a first-order character. Therefore, the sharp decrease of  $1/T_1$  and abrupt increase of  $H_{int}$  below  $T_N$  also suggest the magnetic transition in LaFeAsO possesses a first-order-like character, although a hysteresis behavior at about the magnetic transition was not reported. It should be noted that the divergence of  $1/T_1$  is affected by a structural phase transition from the tetragonal (P4/nmm) to orthorhombic (Cmma) occurring at 165 K upon cooling, which was observed by synchrotron X-ray diffraction in the same batch sample as ours [13]. In fact, as shown in Fig. 5,  $1/T_1$  starts to increase just below 160 K, where the resistivity shows a kink due to this structural transition. It was found that the temperature derivative of the resistivity shows a sharp peak at  $T_N$  determined by the peak of  $1/T_1$ . The  $1/T_1$  result indicates that a characteristic frequency of the magnetic fluctuations start to decrease below 160 K where the structural transition occurs, and becomes static below 142 K. The relationship between the structural and magnetic transition suggests the importance of the spin Jahn-Teller effect in LaFeAsO, where the direction of the ordered moments is determined due to the crystal distortion. To understand the origin of magnetic ordering, it is desired to investigate the relationship between the structural transition temperature and  $T_N$  with the same technique in various samples.

The present <sup>139</sup>La NMR results are in good agreement with the neutron-scattering results [12]. The neutron-scattering measurements revealed a small ordered moment  $0.37\mu_B$ /Fe with the stripe-type magnetic structure  $\mathbf{Q} = (\pi, 0), (0, \pi)$  in the "*unfolded*" Brillouin zone in the undoped LaFeAsO below 134 K, which is slightly lower than the lattice anomalous temperature 155 K.





**Fig. 6.** Field-swept <sup>75</sup>As-NMR spectrum of powdered LaFeAs( $O_{0.89}F_{0.11}$ ) obtained with a fixed frequency f = 72.1 MHz and at 30 K [8]. The insert shows the <sup>75</sup>As-NQR spectrum obtained by sweeping frequency at 5 K. Copyright 2009, the IOP Publishing Ltd.

**Fig. 7.** Doping dependence of <sup>75</sup>As  $1/T_1T$  [8]. The black (green) arrows denote  $T_c$  ( $T^*$ ) (see text). The broken (dotted) line is a fitting to the data for x = 0.11 (0.14). The red arrows indicate  $T_N$ .

# 2.2. <sup>75</sup>As NMR in the normal state of LaFeAs( $O_{1-x}F_x$ )

We move to  $^{75}$ As (I = 3/2) NMR results on the SC compounds.  $1/T_1$  of  $^{75}$ As was obtained by fitting the time dependence of the magnetization recovery after a saturation pulse at the intense peak of the central  $(1/2 \Leftrightarrow -1/2)$  transition (corresponding to  $H_{\parallel}$  the *ab*-plane) in  $H \simeq 9.89$  T at a fixed frequency of 72.1 MHz (see Fig. 6) [7]. A systematic doping evolution of spin dynamics in the normal state is observed in the T-dependence of  $1/T_1T$  at the As site in LaFeAs( $O_{1-x}F_x$ ) as shown in Fig. 7. Similar results were also reported by Nakano et al. [27]. In undoped LaFeAsO, a clear critical slowing down due to the AFM ordering with  $\mathbf{q}_{\text{stripe}}$  is observed at 142 K. For x = 0.04,  $1/T_1T$ , which is the sum of low-lying dynamical susceptibility  $\chi(\mathbf{q})$  over the Brillouin zone, follows a Curie–Weiss temperature dependence down to 30 K. In contrast, the magnetic susceptibility  $\chi(\mathbf{q}=0)$  of LaFeAs( $O_{1-x}F_x$ ) decreases with decreasing temperature [28]. Their contrasting behavior is a clear indication of the development of AFM fluctuations away from  $\mathbf{q} = 0$  at x = 0.04. At x = 0.07,  $1/T_1T$  remains nearly constant down to  $T^* \simeq 40$  K, then decreases rapidly.  $T^*$  can be ascribed neither to a magnetic anomaly nor to an SC transition; invariant <sup>75</sup>As-NMR spectra rules out the former, and the absence of Meissner signal excludes the latter. The reduction of  $1/T_1T$ below  $T^*$ , approximately 20 K higher than  $T_c$ , is reminiscent of the pseudogap behavior observed in the cuprates [29]. The pseudogap-like behavior is more pronounced for x = 0.11 and 0.14, where  $1/T_1T$  decreases on cooling, approaching nearly constant values, as shown in Fig. 8. By fitting the data to  $1/T_1T = a + b \exp(-\Delta_{PG}/T)$ , we obtained a = 0.04 (s<sup>-1</sup> K<sup>-1</sup>),  $b = 0.19 \text{ (s}^{-1} \text{ K}^{-1})$  and  $\Delta_{PG} = 172 \pm 12 \text{ K}$  for x = 0.11, and  $a = 0.012 \text{ (s}^{-1} \text{ K}^{-1})$ ,  $b = 0.18 \text{ (s}^{-1} \text{ K}^{-1})$  and  $\Delta_{PG} = 165 \pm 15 \text{ K}$ for x = 0.14, yielding almost the same pseudogap energies  $\Delta_{PG}$  for x = 0.11 and 0.14 within experimental uncertainty. On the basis of our present results along with those reported previously, we generate the phase diagram for LaFeAs( $O_{1-x}F_x$ ) shown in Fig. 9. The doping dependence of  $1/T_1T$  indicates that the nature of the pseudogap in LaFeAs( $O_{1-x}F_x$ ) and the cuprates differs significantly: (1) In the cuprates,  $1/T_1T$  decreases from temperatures well above  $T_c$  and no clear anomaly is observed at  $T_c$ . In contrast, a clear anomaly in  $1/T_1T$  is found at  $T_c$  for x = 0.11, and Korringa behavior ( $T_1T = \text{const.}$ ), suggestive of a Fermi-liquid (FL) state, is observed at low temperatures, which may be related to the  $T^2$  behavior of the resistivity. Considering the multi-band nature of LaFeAs( $O_{1-x}F_x$ ) and electron doping, these results suggest that the hole FS sheets exhibit pseudogap behavior while others contribute to the FL state. (2) The pseudogap behavior in LaFeAs( $O_{1-x}F_x$ ) becomes more pronounced with F-doping, opposite to the behavior observed in the cuprates. There, the pseudogap behavior is most pronounced near the AFM phase boundary, and it is most likely that AFM correlations may be responsible for the pseudogap behavior. In LaFeAs( $O_{1-x}F_x$ ), however, low-energy AFM correlations are unlikely to yield the pseudogap behavior since no apparent AFM fluctuations are observed via  $^{75}$ As NMR for x = 0.11 and 0.14. Furthermore, almost the same  $\Delta_{PG}$  is observed through <sup>57</sup>Fe-NMR measurements, suggesting that the pseudogap does not have **q**-dependence [32]. From the theoretical point of view, lkeda suggested that the pseudogap behavior in  $1/T_1T$  may originate from band structure effects near Fermi energy [33]. The existence of a high density of states (DOS) just below the Fermi level, which is assigned to a hole FS around  $\Gamma'$  consisting of  $d_{x^2-y^2}$  orbitals in the *unfolded* Brillouin zone, gives rise to a *T*-dependent DOS, and the calculated T-dependence of  $1/T_1T$  is consistent with our results. Thus, the pseudogap behavior originates from its characteristic band structure in LaFeAs( $O_{1-x}F_x$ ).



**Fig. 8.** *T*-dependence of  $1/T_1T$  of  $^{75}$ As at x = 0.07, 0.11, and 0.14 [8]. The broken (dotted) line is a fitting to  $1/T_1T$  of  $^{75}$ As for x = 0.11 (x = 0.14) (see text). Copyright 2009, the IOP Publishing Ltd.



**Fig. 9.** Phase diagram of LaFeAs( $O_{1-x}F_x$ ) [8]. The closed (open) triangle designates the pseudogap energy determined from  $1/T_1$  of  $^{75}$ As (Knight shift of  $^{19}$ F cited from Ref. [30]). The blue triangle indicates  $T^*$  below which the pseudogap behavior was observed. The closed square indicates the magnetic ordering temperature  $T_N$  determined from  $^{139}$ La and  $^{75}$ As NMR. The open square indicates the onset temperature of spin-glass-like magnetism determined from  $\mu$ SR. [31]  $T_c$  (closed circle) is determined from the temperature where  $\rho$  becomes half as that at the onset temperature [1]. (For interpretation of the references to color in this figure, the reader is reference to the web version of this article.) Copyright 2009, the IOP Publishing Ltd.



**Fig. 10.** *T*-dependence of (a) resistivity, (b)  $1/T_1$  of <sup>75</sup>As, (c) the FWHM of the <sup>75</sup>As NMR spectra and (d) <sup>75</sup>As-NMR spectrum where  $H_{\parallel}$  the *ab*-plane in LaFeAs(O<sub>0.96</sub>F<sub>0.04</sub>). The spectrum at 20 K is shifted to be conformed to the spectral peak at 150 K.

# 2.2.1. <sup>75</sup>As NMR in the superconducting state of LaFeAs( $O_{1-x}F_x$ )

Next, we discuss the F-doping evolution of SC features in LaFeAs( $O_{1-x}F_x$ ). The x = 0.04 sample (LaFeAs( $O_{0.96}F_{0.04}$ )) locates near the boundary between the AFM and SC phases, which would help us elucidate an interplay between magnetism and superconductivity in LaFeAs( $O_{1-x}F_x$ ). Fig. 10 displays the *T*-dependence of resistivity  $\rho$ ,  $1/T_1$  of <sup>75</sup>As, the full width







**Fig. 11.** *T*-dependence of  $1/T_1$  of  $^{75}$ As measured at the peak corresponding to  $H_{\parallel}$  the *ab*-plane [8]. Copyright 2009, the IOP Publishing Ltd.

**Fig. 12.** *T*-dependence of  $1/T_1$  of <sup>75</sup>As in LaFeAs( $O_{0.89}F_{0.11}$ ) under 5.2, 9.9 and 12 T [8]. The dashed curve is a calculation with assuming a line node gap  $\Delta(\phi) = \Delta_0 \sin(2\phi)$  with  $\Delta_0 = 2k_BT_c$ . Copyright 2009, the IOP Publishing Ltd.

at half maximum (FWHM) of the <sup>75</sup>As-NMR spectra at x = 0.04. Fig. 2 indicates that the resistivity of  $x \ge 0.07$  samples exhibits a metallic behavior ( $\rho \propto T^2$  holds below 150 K), but that at x = 0.04, it exhibits a nonmetallic behavior below 70 K.  $\rho$  at x = 0.04 starts to increase with lowering temperature, and then drops below 30 K (Fig. 10 (a)).  $1/T_1$  is determined with a single component above 30 K, and the T-dependence of  $1/T_1T$  follows the Curie–Weiss law  $1/T_1T \propto 1/(T+\theta)$  with  $\theta = 10.3 \pm 2$  K between 30 K and 200 K [7], which is a characteristic features of the development of AFM fluctuations. Below 30 K, a short  $T_1$  component appears, and the longer  $T_1$  component that exhibits a superconducting anomaly at  $T_c$ is plotted in Fig. 10(b);  $1/T_1$  decreases suddenly below 30 K and then exhibits superconductivity below  $T_c \simeq 16$  K. This anomaly at 30 K cannot be ascribed to the occurrence of superconductivity because ac susceptibility does not exhibit any anomaly near 30 K. Instead, this is attributed to a weak magnetic ordering, because the line width increases gradually below 30 K (Fig. 10(c), (d)). The ordered moment is very small because the broadening of the <sup>75</sup>As and <sup>139</sup>La NMR spectra is much smaller than that of the undoped LaFeAsO [7,20]. A divergence of  $1/T_1$  was observed at  $T_N \simeq 142$  K in LaFeAsO due to the occurrence of the AFM ordering. In contrast, we did not find such a huge increase of  $1/T_1$  but just a decrease of  $1/T_1$ , indicating that the magnetic anomaly becomes weakened upon F-doping. As noted above, there emerges a short component of  $1/T_1$  below 30 K whose value is approximately 65% at 3 K. Since it is difficult to attribute such a large amount to inhomogeneous F-concentration, this distribution of  $1/T_1$  implies a phase separation into the magnetically ordered and SC phases. Indeed, recent µSR measurements suggest the presence of a phase separation into SC and spin-glass-like magnetic phases in LaFeAs( $O_{0.94}F_{0.06}$ ) near the phase boundary [31]. Our x = 0.04 result is consistent with this  $\mu$ SR experiment. It is considered that there exist AFM and SC regions and thus phase separation occurs in underdoped LaFeAs $(O_{1-x}F_x)$ .

Next, we discuss the SC-gap properties from the *T*-dependence of  $1/T_1$  in the SC state. Fig. 11 shows the *T*-dependence of  $1/T_1$  of <sup>75</sup>As for x = 0.04, 0.07 and 0.11, which was measured in  $H \sim 9.9$  T. As mentioned above, a short component of  $T_1$  appears gradually in all samples below 30 K and its fraction increases with decreasing *T*. The appearance of the short component of  $T_1$  is considered to be due to a tiny amount of a spin-glass-like magnetic region. However, the fraction of the longer component of  $T_1$  is dominant even at low temperatures, and thus the longer component is shown in Fig. 11.

It was found that  $1/T_1$  at x = 0.04, 0.07, and 0.11 decreases suddenly without showing a Hebel–Slichter (coherence) peak just below  $T_c$ , and that the  $T^3$  dependence of  $1/T_1$  was observed in the SC state for all samples. Although the absence of the coherence peak and  $T^3$  dependence observed in  $1/T_1$  strongly suggest the presence of the linenodes, various experimental results are inconsistent with the presence of the linenodes. It is known in anisotropic superconductors with nodes that an applied magnetic field induces the extra relaxation rate originating from the Volvik effect [34]. It was pointed out that the quasiparticle states are extended outside the vortex cores with ungaped spectrum in a *d*-wave superconductor, which gives rise to a field-induced relaxation rate. However, such field-induced relaxation rate was not observed in

LaFeAs( $O_{1-x}F_x$ ) as shown in Fig. 12. It was found that the  $T^3$  behavior holds down to 4 K (~  $0.2T_c$ ) in the field range of 5.2–12 T within the experimental error (typically  $\Delta T_1 \sim 10\%$ ), indicative of the absence of the field-induced  $1/T_1$ . We also point out that a residual density of states (DOS) suggested from the low-temperature Korringa behavior was not observed in the x = 0.04, 0.07 and 0.11 samples. In non-s-wave superconductors with line nodes, it is well known that the residual DOS is easily induced by a tiny amount of impurities and crystal imperfections, and was observed in most of unconventional superconductors [35,36]. It seems that the absence of the residual DOS is contrary to non s-wave models, since the LaFeAs( $O_{1-x}F_x$ ) is considered to possess the randomness related to the F substitution. Furthermore, various experimental results, such as penetration-depth and photo-emission measurements in the FeAs superconductors, suggest the presence of a finite superconducting gap, which is inconsistent with the our NMR results [37,38].

To reconcile with these experimental results, the  $s_{\pm}$  state with the anisotropic gap are considered as a most promising state in the FeAs superconductors at present. In this state, the superconducting gap is sign reverse between hole and electron FSs across the nesting vector. In a case of the anisotropic *s*-wave gap ( $\Delta(\phi) = |\Delta_0 \sin(2\phi)|$  [39]) and  $s_{++}$ -wave gap, a coherence peak remains since the coherence factor does not vanish when the gap function is integrated over the FSs. However, the resistivity follows a  $T^2$  dependence in a wide temperature range between  $T_c$  and 150 K in x = 0.07 and 0.11; it is hard to consider that the quasiparticle damping suppresses the coherent peak just below  $T_c$ .

Alternatively, the absence of the coherence peak is consistently understood by the sign-changed superconducting gaps realized in the  $s_{\pm}$  state [40–42]. Furthermore, it was reported that the  $T^3$  dependence in the superconducting state can be reproduced with the  $s_{\pm}$  state with an anisotropic character of the superconducting gap at the electronic FSs together with some impurity effect [43]. However, since the exponential temperature dependence of  $1/T_1$  should be observed in a impurity-free sample with the  $s_{\pm}$  pairing, further NMR measurements using high-quality samples are important, in particular,  $1/T_1$  measurements at low temperatures are crucial.

We point out that the  $T^3$  dependence is observed even in the x = 0.04 sample located in the boundary of two phases. This behavior is in contrast to that of the superconductors which coexist with magnetism such as the pressure-induced heavy-fermion superconductor CeRhIn<sub>5</sub> [44]. In CeRhIn<sub>5</sub> near the critical pressure, although  $1/T_1$  decreases sharply just below  $T_c$ ,  $1/T_1$  becomes proportional to T far below  $T_c$ . It is reported that the  $1/T_1 \propto T$  behavior does not originate from residual density of states (DOS) but from the gapless nature in the low-lying excitation due to the microscopic coexistence of antiferromagnetism and superconductivity in CeRhIn<sub>5</sub> [44]. The different behaviors of  $1/T_1$  suggest that the nature of coexistence is different for the two superconductors. In addition to the emergence of a short component of  $1/T_1$  below  $T_N$  as discussed above, the robust  $T^3$  dependence of  $1/T_1$  at x = 0.04 also supports a phase separation into the magnetically ordered and SC phases because the magnetic ordering would affect the  $T^3$  behavior if the magnetic order and superconductivity coexist microscopically.

Here, we discuss the relationship between magnetic fluctuations and superconductivity. Since the electron-phonon coupling was shown to be too weak to account for the high  $T_c$  of the iron-oxypnictide superconductors [14,45], spin fluctuation is one of the plausible candidates for the pairing interaction [15–17]. Due to the disconnected FSs in the iron oxypnictide, nesting-related spin fluctuations would be the origin of the pairing interaction. F-doping (corresponding to electron doping) is likely to enhance a mismatch between the FSs, leading to the suppression of the spin fluctuations. This is actually observed in the present NMR study; the significant antiferromagnetic fluctuations in x = 0.04 are suppressed in x = 0.07. It should be noted that  $1/T_1$  in the SC state of x = 0.07 is identical to that in x = 0.11, although  $1/T_1$  in the normal state is different with each other. An almost constant value of  $T_c$  against the F concentration, irrelevant to the drastic change of  $1/T_1T$  in the normal state, suggests that the spin fluctuations observed through the  $1/T_1$  measurements do not play a vital role for the superconductivity. However, it should be noted that  $1/T_1$  measurements can detect the low-energy magnetic fluctuations (typically  $\sim$  mK order), and might fail to detect important magnetic fluctuations if their characteristic energy exceeds the limitation of the NMR experiments. Therefore, the inelastic neutron experiments over a wide *q*-space and energy range are needed for uncovering magnetic fluctuations thoroughly, and are important for clarifying the relationship between the superconductivity and magnetic fluctuations.

#### 2.3. NMR study in the 122 system

Superconductivity in  $AFe_2As_2$  (A = Ba, Sr and Ca) with the "122" structure appears where antiferromagnetism is suppressed via chemical substitution or pressure. The well-known systems are  $(Ba_{1-x}K_x)Fe_2As_2$  [46] and  $Ba(Fe_{1-x}Co_x)_2As_2$  [47], in which superconductivity is induced by hole and electron doping, respectively. In these systems, the existence of an AFM quantum critical point has been suggested, and much attention has been paid to the relationship between quantum critical magnetic fluctuations and superconductivity [48–51]. In this section, we introduce the NMR results on the parent compound  $BaFe_2As_2$  [21] and review our NMR studies on  $BaFe_2(As_{1-x}P_x)_2$  [10,11].

### 2.3.1. BaFe<sub>2</sub>As<sub>2</sub> [21]

Careful As-NMR measurements on single-crystals of BaFe<sub>2</sub>As<sub>2</sub> were performed by Kitagawa et al. [21]. In the following, their NMR results are introduced.

Fig. 13 shows <sup>75</sup>As-NMR spectra at the fixed frequency of 48.41 MHz obtained by sweeping the magnetic field parallel and perpendicular to the *c*-axis at several different temperatures. The spectra at T = 141 K are representative of the paramagnetic phase, while the spectra at the other temperatures belong to the AFM ordered phase. As <sup>75</sup>As nuclei have spin 3/2,



**Fig. 13.** <sup>75</sup>As-NMR spectra obtained by sweeping the magnetic field at the fixed frequency of 48.41 MHz [21]. In the paramagnetic state at 141 K, the spectrum consists of a sharp central line and two broader satellite lines. Below 135 K, the internal fields along the *c*-axis due to commensurate AFM order splits the NMR spectra for  $H \parallel c$  (red lines) and shifts the spectra to lower fields for  $H \parallel a$ - or *b*-axis (blue lines). The insert shows the angular variation of the NMR spectrum at 20 K for the field rotated in the *ab*-plane. The two sets of satellite lines originate from the twinned structural domains in the orthorhombic phase. The satellite positions are fitted to Eq. (2) with the quadrupole parameters;  $\nu^c = 2.21$  MHz,  $|\nu^a - \nu^b|/\nu^c = 1.18$  (solid lines). Copyright 2008, the Japanese Physical Society.

the NMR frequencies are generally expressed by a perturbation series when the magnetic Zeeman interaction dominates over the quadrupole interaction,

$$\nu_{m \leftrightarrow m-1} = \mu_0^{75} \gamma H_{\text{eff}} + \frac{1}{2} \nu^c \left( m - \frac{1}{2} \right) \left( 3\cos^2 \theta - 1 + \frac{\nu^a - \nu^b}{\nu^c} \sin^2 \theta \cos 2\phi \right)$$
  
+ (second-order correction) (2)

The first term is the Zeeman frequency, where  ${}^{75}\gamma = 7.29019 \text{ MHz/T}$  is the nuclear gyromagnetic ratio and  $H_{\text{eff}}$  is the effective field at the As nuclei. In the PM state, the effective field is expressed as  $H_{\text{eff}} = (1 + K^i)H$ , where H is the external field and  $K^i$  is the Knight shift along the *i*-axis. The second term represents the first-order quadrupolar shift for the three nuclear transitions  $I_z = m \leftrightarrow m - 1$  (m = 3/2, 1/2, or 1/2). The explicit expression for the second-order correction can be found in a standard textbook [19]. The quadrupole splitting parameters  $v^i$  (i = a, b, c) are related to the electric field gradient (EFG) tensor  $V_{\alpha\beta} = \partial^2 V / \partial r_{\alpha} \ \partial r_{\beta}$  at the As nuclei as  $v^i = eV_{ii}Q/2\hbar$ , where Q is the nuclear quadrupole moment of <sup>75</sup>As. Here the crystal axes are defined with respect to the orthorhombic (*Fmmm*) unit cell. Note that the *mm2* symmetry of the As sites in the orthorhombic phase guarantees that the crystalline a, b, and c axes are the principal axes of EFG tensor. The polar angle ( $\theta, \phi$ ) specifies the direction of the magnetic field relative to the crystalline axes. In the tetragonal phase, the NMR spectrum is independent of  $\phi$  since  $v_a = v_b = -v_c/2$ . As shown in Fig. 13, the NMR spectra at T = 141 K show a sharp central line (m = 1/2) with the full width at half maximum (FWHM) of 3.5 kHz and two broader satellite lines (m = 3/2 and 1/2) with the FWHM of 100 kHz. The quadrupole splitting  $v_c$  is determined from the separation between the two satellite lines for  $H \perp c$  ( $\theta = \pi/2$ ), which is half of the separation for  $H \parallel c$  ( $\theta = 0$ ) as expected. The value of  $v_c$  is plotted against temperature in Fig. 14.

When the temperature is lowered below 135 K, the NMR spectrum develops a two-fold splitting for  $H \parallel c$ . This is the direct evidence for a two-sublattice AFM order. The AFM moments generate a spontaneous internal field with alternating sign  $\pm \Delta$ , therefore  $H_{\text{eff}} = H \pm \Delta$  in Eq. (2). The temperature dependence of  $\Delta$  determined from the separation between the split center lines is shown in Fig. 15 by crosses. No splitting was observed when the field is applied along the *a*- or *b*-axis. Instead, the whole spectrum is shifted to lower fields as seen in Fig. 13. This indicates that the internal field is parallel to the *c*-axis. When  $H \perp c$ ,  $H_{\text{eff}}$  is given by the magnitude of the vector sum of the mutually orthogonal external and internal fields,  $H_{\rm eff} = \sqrt{H^2 + \Delta^2}$ , giving positively shifted unsplit resonance lines. In Fig. 15,  $\Delta$  determined also from the shift of the central line for  $H \parallel a$  or b is plotted by squares. The values of  $\Delta$  for the two field orientations show good agreement, indicating that the magnitude and the direction of the AFM moment are independent of the field direction. The behavior in the vicinity of the phase transition was investigated by recording the peak intensity of the Fourier transformed spectrum at the resonance position of the paramagnetic phase with changing temperature as shown in the insert of Fig. 15. The magnetic transition was found to be very sharp with the transition width less than 1 K, indicating good homogeneity of the crystal. It also shows a clear hysteresis in temperature about 4 K wide, providing a conclusive evidence for the first-order transition. This is also inferred from the discontinuous development of the internal field as well as a discontinuous structural transition suggested by a pronounced change of symmetry of EFG. As shown in the insert of Fig. 13, the quadrupole splitting at 20 K varies with the field direction ( $\phi$ ) in the *ab*-plane, indicating that  $v_a \neq v_b$ . This is consistent with the orthorhombic symmetry. The angular variation of the NMR spectra displayed in the insert of Fig. 13 shows two branches of satellite lines, which are shifted



**Fig. 14.** Nuclear quadrupole splitting frequency along the *c*-axis,  $v_c$ , and the asymmetry parameter  $|v_a - v_b|/|v_c|$  are plotted as a function of temperature [21]. The asymmetry parameter is zero in the tetragonal phase. Its emergence below 135 K and a jump in  $v_c$  indicate the first-order structural transition into the orthorhombic phase. Copyright 2008, the Japanese Physical Society.



**Fig. 16.** Possible spin configurations in the AFM ordered state in  $BaFe_2As_2$ , which is compatible with the <sup>75</sup>As-NMR results [21]. Only one Fe–As layer is drawn for simplicity. The internal field at the As sites are shown by grey arrows. There are two candidates: (a) the stripe AFM order and (b) AFM stacking of the ferromagnetic layers. The former case (a) is realized in  $BaFe_2As_2$  (see text). Copyright 2008, the Japanese Physical Society.



**Fig. 15.** The temperature dependence of the internal field at the As nuclei associated with the antiferromagnetic order [21]. The insert shows the intensity of the central line at the resonance position of the paramagnetic phase for  $H \perp c$ . The abrupt change with hysteresis is the evidence for the first-order magnetic transition. Copyright 2008, the Japanese Physical Society.



**Fig. 17.** Nuclear spin-lattice relaxation rate divided by temperature,  $1/T_1T$ , is plotted as a function of temperature for two field-orientations [21]. The behavior,  $T_1T = \text{const.}$ , at low temperatures indicates the itinerant (Fermi liquid) character of the material. We should remark that the upturn of  $1/T_1T$  in the paramagnetic phase is observed only for  $H \perp c$ . This indicates anisotropic development of the stripe-type antiferromagnetic spin fluctuations perpendicular to both the *c*-axis and the stripe. Copyright 2008, the Japanese Physical Society.

by 90°. This comes from the twinned orthorhombic domains. The  $\phi$  dependence of the satellite lines can be fit to Eq. (2). The extrema of the angular variation correspond to the field directions parallel to either *a*- or *b*-axis. The asymmetry parameter of EFG defined by  $|v_a - v_b|/v_c$  is plotted in Fig. 14. The asymmetry parameter, which is zero in the tetragonal phase, is observed to develop abruptly below the transition temperature, and a jump in  $v_c$  is also observed across the transition. These results establish the simultaneous structural and magnetic transition. The large value of asymmetry parameter, exceeding one in the low-temperature phase, implies that the principal axis for the largest EFG changes by 90° across the transition. This suggests that the band structure or the nature of the Fe–As bonds becomes highly anisotropic in the *ab*-plane.

The <sup>75</sup>As-NMR spectra gives the valuable information about the spin structure in the AFM ordered state. There are two major experimental constraints: (i) the internal field at the As sites is parallel to the *c*-axis; and (ii) the AFM state has a simple two-sublattice structure. There are two possible spin structures compatible with the NMR experiments as shown in Fig. 16, which generate a finite *c*-component of the internal field. In the first configuration (a), the AFM order is described by the wave vector (101) or (100), forming stripes with the AFM moments directed perpendicular to the stripe. (Note that we cannot distinguish the orthorhombic *a*- and *b*-axes by NMR spectra.) In the second configuration (b), ferromagnetic layers in the *ab*-plane stack antiferromagnetically along the *c*-axis. The second structure, however, is highly unlikely since the temperature dependence of the susceptibility rules out ferromagnetic correlation.

The spin-lattice relaxation rate divided by temperature  $1/T_1T$  is shown in Fig. 17. In the PM phase,  $1/T_1T$  shows anisotropic temperature dependence. Substantial enhancement is seen for  $H \parallel a$  or b with decreasing temperature, while

 $1/T_1T$  is nearly constant for  $H \parallel c$ . Across the first-order structural/magnetic transition,  $1/T_1T$  drops discontinuously by a factor of three. At low temperatures,  $1/T_1T$  approaches a constant value for both field orientation expected for a Fermi liquid. This is consistent with the metallic behavior of the resistivity. The low-temperature phase is characterized as an itinerant antiferromagnetic phase. Although the AFM order may be driven by FS nesting, our results demonstrate that the order is commensurate and a sizable density of states at the Fermi level remains down to T = 0.

### 2.3.2. <sup>31</sup> P NMR in the normal state of BaFe<sub>2</sub>( $As_{1-x}P_x$ )<sub>2</sub> [11]

Spin-fluctuation-mediated superconductivity associated with the suppression of the antiferromagnetism is one likely scenario [16], but the identification of the mechanism is far from settled [52,53]. The difficulty in examining the SC mechanism could arise from complexity in the materials that can lead to ambiguous interpretations; e.g., nonuniversal SC gap functions and limited sample quality. It is thus essential to find a suitable model system to examine the mechanism of superconductivity. We have studied isovalent-doped  $BaFe_2(As_{1-x}P_x)_2$  within various SC systems possessing the "122" structure, since isovalent P doping is not expected to add carriers [54], and thus  $BaFe_2(As_{1-x}P_x)_2$  maintains the compensation condition, i.e. the volume of the hole FSs is equal to that of the electron FSs. Therefore, we consider that  $BaFe_2(As_{1-x}P_x)_2$  is an ideal system to investigate relationship between magnetic fluctuations and superconductivity.

We have performed <sup>31</sup>P-NMR measurements on BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> for  $0.2 \le x \le 0.64$  in order to investigate their normalstate spin dynamics. Samples of a mosaic of single crystals were prepared as described elsewhere [54]. The dHvA experiments observed signals in single crystalline samples from the same batch as x = 0.41, 0.56, and 0.64, indicating the excellent quality of our samples [55]. The high quality of our samples is also suggested by the sharp SC transitions [54]. <sup>31</sup>P-NMR spectra (<sup>31</sup> $\gamma/2\pi = 17.237$  MHz/T) were obtained by sweeping frequency in a fixed magnetic field of 4.12 T. The Knight shift *K* was determined with respect to the reference material H<sub>3</sub>PO<sub>4</sub>. The <sup>31</sup>P nuclear spin-lattice relaxation rate  $1/T_1$  was determined by fitting the time dependence of spin-echo intensity after saturation of nuclear magnetization to a theoretical I = 1/2 curve with a single component of  $T_1$ .

Fig. 18 displays <sup>31</sup>P-NMR spectra obtained from the BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> crystals. Each <sup>31</sup>P NMR spectrum consists of a single line, ruling out microscopic inhomogeneity caused by P substitution. *K*, which measures the effective field at the nucleus produced by electrons, is described as  $K = K_{spin} + K_{chem}$ ;  $K_{spin}$  is the spin part of *K* and is related to the uniform spin susceptibility  $\chi(\mathbf{q}) = 0$ , which is proportional to DOS at the Fermi energy  $N(E_F)$ .  $K_{chem}$  is the chemical shift, which is unrelated to  $\chi(\mathbf{q} = 0)$ , and is estimated to be ~ 0.018% as follows. Since no obvious AFM fluctuations were detected by NMR at high temperatures as seen in Fig. 19, it would be a good approximation to assume that  $\sqrt{T_1T}$  is proportional to  $N(E_F)$  at high temperatures, i.e. to assume that the usual Korringa relation holds at 270 K. Based on the plot of  $\sqrt{T_1T}$ against *K* at 270 K for different *x* shown in the insert of Fig. 18, we can estimate  $K_{chem}$  as the intercept. The obtained  $K_{chem}$  would be a reasonable value, since the chemical shift for <sup>31</sup>P in many diamagnetic insulators is of the order of some hundreds of ppm, which is comparable to this  $K_{chem}$  [19]. By assuming  $K_{spin} \propto \chi(\mathbf{q} = 0) = \mu_B^2 N(E_F)$ , the P-substitution dependence of  $K_{spin}$  at 270 K suggests that the change in  $N(E_F)$  would be at most 10% for  $x \leq 0.64$ , which is quantitatively consistent with the result of our band calculation discussed below.

Local-density-approximation (LDA) band-structure calculations were performed for non-spin-polarized BaFe<sub>2</sub>As<sub>2</sub> and BaFe<sub>2</sub>P<sub>2</sub>, using the WIEN2k package in the APW + local orbital basis [56]. In addition, to obtain systematic changes of the electronic band structure for BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>, Ikeda et al. performed the LDA calculations for three virtual materials with linearly-interpolated  $z = z_0(1 - x) + z_1 x$ ; (i) BaFe<sub>2</sub>As<sub>2</sub> with fixed  $(a, c) = (a_0, c_0)$ , (ii) BaFe<sub>2</sub>As<sub>2</sub> with linearly-interpolated  $(a, c) = (a_0(1 - x) + a_1x, c_0(1 - x) + c_1x)$ , (iii) BaFe<sub>2</sub>As<sub>2</sub> with fixed  $(a, c) = (a_1, c_1)$ , where  $a_{0,1}$ ,  $c_{0,1}$ , and  $z_{0,1}$  are the experimental values for the crystallographic parameters of BaFe<sub>2</sub>As<sub>2</sub> and BaFe<sub>2</sub>P<sub>2</sub>, respectively [54,57]. Fig. 20 shows the P-doping dependence of the density of states at the Fermi level  $N(E_F)$  plotted on a per formula unit basis, for cases (i), (ii), and (iii).  $N(E_F)$  barely changes for x < 0.5, and then decreases for x > 0.5. Such behavior is consistent with our Knight shift results.

As shown in Fig. 18(b), *K* is almost temperature independent for  $x \le 0.56$ , and that the absolute value of *K* in the normal state decreases only slightly upon P substitution. These data indicate that P substitution does not produce significant changes in  $\chi(\mathbf{q} = 0)$  and  $N(E_F)$ . This is in stark contrast to carrier-doped iron-pnictide superconductors; in electron-doped Ba(Fe<sub>1-y</sub>Co<sub>y</sub>)<sub>2</sub>As<sub>2</sub>, the Knight shift data indicate that  $N(E_F)$  of non-SC y = 0.26 is approximately 50% that of y = 0.08 with the maximum  $T_c$  of 26 K [49]. Such drastic effects on  $N(E_F)$  via electron doping is expected from the characteristic band structure [15,33]; the calculated  $N(E_F)$  rapidly changes near  $E_F$  with a negative gradient, resulting in a rapid decrease of  $N(E_F)$  with electron doping. Large changes in FSs via charge-carrier doping thus necessarily involve dramatic modification in the DOS and FS nesting resulting in changes in spin fluctuations. In addition to possible changes in  $T_c$  due to the modification of spin excitation spectrum [49], drastic changes in  $N(E_F)$  can also affect severely  $T_c$  [58], and the suggested giant magnetoelastic coupling may lead to further suppressions of  $T_c$  [59]. Therefore, the decrease in  $N(E_F)$  as well as the suppression of spin fluctuations should be taken into account for the interpretation of possible changes in  $T_c$  for electron-doped Ba(Fe<sub>1-y</sub>Co<sub>y</sub>)<sub>2</sub>As<sub>2</sub>. In contrast, the nearly unperturbed  $K_{spin}$  by isovalent P-doping demonstrates that BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> is an ideal model system to test the relevance of spin fluctuations to superconductivity.

Significant low-energy AFM fluctuations are probed near the maximum  $T_c$  via  $1/T_1$ .  $1/T_1T$  is described by the wavevector average of the imaginary part of the dynamical susceptibility  $\chi''(\mathbf{q}, \omega_0)$ , i.e.,  $1/T_1T \propto \sum_{\mathbf{q}} |A(\mathbf{q})|^2 \chi''(\mathbf{q}, \omega_0)/\omega_0$ , where  $A(\mathbf{q})$  represents the hyperfine coupling between <sup>31</sup>P nuclear spins and the surrounding electrons, and  $\omega_0$  is the NMR frequency. The Korringa law  $T_1TK^2$  = const. generally holds in a Fermi-liquid (FL) state, but is inapplicable to BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>



**Fig. 18.** P substitution evolution of (a) <sup>31</sup>P-NMR spectra and (b) <sup>31</sup>P Knight shift (<sup>31</sup>K) determined at the spectral peak, obtained in a mosaic of the single crystals at 4.12 T [11]. (b) The arrows indicate the chemical shift  $K_{\text{chem}}$  (see text). The abrupt decrease in <sup>31</sup>K at low temperatures is due to the onset of superconductivity. Inset: <sup>31</sup>K vs  $(T_1T)^{-1/2}$  at 270 K for different P concentrations *x*. Copyright 2010, the American Physical Society.



**Fig. 19.** The <sup>31</sup>P nuclear spin-lattice relaxation rate divided by temperature  $(T_1T)^{-1}$  for BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> at 4.12 T [11]. Solid lines represent fits to  $(T_1T)^{-1} = a + b(T + \theta)^{-1}$  (see text). As AFM fluctuations are suppressed as inferred from the suppression of  $(T_1T)^{-1}$ ,  $T_c$  (denoted by arrows) also decreases. Inset: Fitting parameters of  $(T_1T)^{-1}$ . The fitting parameters *a* and *b* are plotted against P concentration *x*. The *a* and *b* weakly depend on *x*, but  $\theta$  shows a strong *x* dependence (see Fig. 21). The small value of  $\theta$  at x = 0.33 ( $\theta \sim 0$ ) are insensitive to the fitting parameters of *a* and *b*. Copyright 2010, the America Physical Society.



**Fig. 20.** Isovalent P-doping dependence of the density of states at the Fermi level  $N(E_F)$  plotted on a per formula unit basis, for cases (i), (ii), and (iii) [11]. For this calculation, crystallographic parameters determined experimentally for BaFe<sub>2</sub>As<sub>2</sub> (x = 0) and BaFe<sub>2</sub>P<sub>2</sub> (x = 1) were used. Copyright 2010, the America Physical Society.

near the AFM phase since Curie–Weiss (CW) behavior is observed in  $1/T_1T$  (see Fig. 19). For x = 0.33,  $1/T_1T$  increases significantly down to  $T_c$  whereas the Knight shift is constant. These  $1/T_1T$  and K data demonstrate convincingly that AFM fluctuations with finite **q** continue to grow down to  $T_c$  at optimal doping.

The AFM fluctuations in BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> are enhanced significantly as the P concentration is reduced towards the maximum  $T_c$  ( $x \simeq 0.33$ ), as evidenced by the rapid increase in  $1/T_1T$  from conventional FL behavior at x = 0.64 (where  $1/T_1T$  and K are almost constant). The crossover from FL to CW behavior in  $1/T_1T$  correlates perfectly with the change in the resistivity results [54]. As the system evolves from a FL (x = 0.71) towards the maximum  $T_c$  (x = 0.33) near the AFM phase, the temperature dependence of the resistivity changes from  $T^2$  to T-linear, one hallmark of non-FL behavior. The exponent of the temperature dependence of the resistivity is shown as a contour plot in Fig. 21(a). Specifically, the CW behavior of  $1/T_1T$  and the T-linear resistivity at x = 0.33 can be explained by the existence of two-dimensional (2D) AFM spin fluctuations in the theory of nearly AFM metals [60]. Indeed, the evolution of the AFM spin excitations measured by  $1/T_1T$  upon P substitution can be fit consistently by the equation expected from the same theory [60],  $1/T_1T = a + b/(T + \theta)$  (see solid lines in Fig. 19). Such 2D AFM fluctuations were experimentally observed in the parent BaFe<sub>2</sub>As<sub>2</sub> via neutron scattering experiments [61]. According to band calculations [62], substantial 2D AFM fluctuations can be generated by the inter-band spin excitations between the multiple FSs predominantly derived from Fe *d* electrons.



**Fig. 21.** Temperature-P concentration phase diagram of BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> [11].  $T_c$ ,  $T_s$ , and  $T_N$  denote the SC, orthorhombic-tetragonal, and AFM transition temperatures, respectively. (a) Colors represent the exponent,  $\alpha = d(\ln \Delta \rho_{ab})/d(\ln T)$ , at zero magnetic field for the resistivity curves in Ref. [54], where  $\Delta \rho_{ab} = \rho_{ab} - \rho_{ab}(T \rightarrow 0 \text{ K})$ . (b) The triangles represent  $\theta$  obtained by fitting  $(T_1T)^{-1}$  data to the equation,  $(T_1T)^{-1} = a + b(T + \theta)^{-1}$  (error bars are within the symbol size). *T*-linear resistivity, suggesting quantum-critical behavior, is observed in proximity to a magnetic instability signaled by  $\theta \simeq 0$  at x = 0.33. These quantum-critical fluctuations are found to correlate with the enhancement of the effective mass as denoted by the pentagons (taken from Ref. [55]). Copyright 2010, the America Physical Society.

Our central finding in BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> is that the 2D AFM fluctuations of a quantum-critical nature have a clear correlation with the enhancement of quasiparticle effective mass and  $T_c$  as summarized in Fig. 21. We found that the Weiss temperature  $\theta$  obtained from the fitting increases with P substitution and becomes almost zero near x = 0.33 where the maximum  $T_c$  is achieved.  $\theta = 0$  K implies that the dynamical susceptibility probed by  $1/T_1T$  measurement diverges at absolute zero, or that the magnetic correlation length continues to increase down to T = 0 K. Our result thus strongly suggests the presence of an AFM quantum critical point near the maximum  $T_c$  in proximity to the AFM phase boundary. As the P concentration is varied towards optimal doping ( $x \sim 0.33$ ) from x = 0.64 where the FL state is observed, the magnetic fluctuations become dramatically enhanced as  $\theta$  decreases. Importantly, the quasiparticle mass and  $T_c$  increase as  $\theta$  approaches 0 K. This strongly suggests that the AFM quantum-critical fluctuations lead to strong mass renormalization and unconventional superconductivity. Our systematic NMR measurements, which are compared with transport measurements, thus provide the first evidence that the quasiparticle mass enhancement is strongly coupled to the AFM quantum-critical fluctuations in iron-pnictide superconductors as previously observed in heavy fermion systems [63]. Furthermore, since  $N(E_F)$ generally correlates with  $T_c$  in conventional BCS superconductors, the enhancement of  $T_c$  with approaching the quantum critical point from the overdoped side cannot be accounted for by a nearly unperturbed  $N(E_F)$ , demonstrating clearly that superconductivity in  $BaFe_2(As_{1-x}P_x)_2$  is tuned predominantly by the AFM fluctuations. Therefore, we conclude that the 2D AFM quantum-critical fluctuations are likely to play a central role in the occurrence of unconventional superconductivity in  $BaFe_2(As_{1-x}P_x)_2$ .

Previous NMR measurements also indicated that there is a strong connection between low-energy spin fluctuations and superconductivity in "122" [10], "111" [64–66] and "11" iron-based superconductors [67–70]. These suggest that the relevance of spin fluctuations to the high- $T_c$  superconductivity is universal despite the nonuniversal gap structure. The strong connection would be naturally understood if one considers the superconductivity observed near magnetic phase and the well-nested hole and electron FSs. By contrast, we reported that the connection is relatively weaker in LaFeAs( $O_{1-x}F_x$ ) [7]. Such a weak link may originate from much lower  $T_c$  of 26 K in LaFeAs( $O_{1-x}F_x$ ) than that of RFeAs( $O_{1-x}F_x$ ) (R = Ce, Pr, Sm, etc.). However, it remains unresolved whether spin fluctuations are also important for high- $T_c$  superconductivity in the 1111 system with  $T_c$  exceeding 50 K, since magnetic rare-earth atoms R hinder quasiparticle excitations responsible for superconductivity [71]. Therefore, examinations of the connection between magnetic fluctuations and superconductivity of high- $T_c$  1111 iron-pnictides would be crucial for establishing general view of iron pnictide superconductivity.

# 2.3.3. <sup>31</sup>P-NMR in the superconducting state of $BaFe_2(As_{1-x}P_x)_2$ [10]

The SC properties of BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub>, which is the optimal-doping sample, was investigated with <sup>31</sup>P-NMR measurements [10]. We observed a marked <sup>31</sup>(1/ $T_1$ ) behavior distinctly different from other iron arsenides. Fig. 22(c) shows that <sup>31</sup>(1/ $T_1$ ) decreases sharply just below  $T_c$  and there is no evidence for a coherence peak. We find  $1/T_1 \propto T$  below  $\sim 4$  K



**Fig. 22.** (a) and (b) show <sup>31</sup>P nuclear-spin relaxation curves for 175 and 1.5 K in 4.12 T, exhibiting clear single exponential behavior [10]. (c) <sup>31</sup>P  $1/T_1$  under 2.1, 4.12, and 6.0 T. Inset in panel (c) shows <sup>31</sup>P  $1/T_1$  vs magnetic field at 2 K; a linear fit is used to extrapolate  $1/T_1$  for  $H \rightarrow 0$  T. Copyright 2010, the America Physical Society.



**Fig. 23.** Normalized <sup>31</sup>P  $1/T_1$  for BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> and (Ba<sub>0.6</sub>K<sub>0.4</sub>)Fe<sub>2</sub>As<sub>2</sub> [79]. The solid curve shows a calculation for a line-node gap function  $\Delta(\phi) = \Delta_0 \sin(2\phi)$  with  $2\Delta_0 = 6k_BT_c$ ,  $N_{\rm res}/N_0 = 0.34$  [10]. Copyright 2010, the America Physical Society.

down to 100 mK, showing the existence of a residual DOS at zero energy. Below about 10 K ( $\sim 0.3T_c$ ),  $1/T_1$  depends on the magnetic field [see Fig. 22(c)]. By extrapolating to zero field, we still find  $T_1T = \text{const.}$  behavior below  $\sim 4$  K, excluding the possibility that the  $T_1T = \text{const.}$  behavior is attributable to applied fields. The existence of a residual DOS in  $H \rightarrow 0$  inferred from NMR is consistent with thermal-conductivity results on BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> that reveal a finite thermal conductivity divided by temperature  $\kappa_0/T$  at  $T \rightarrow 0$  under zero field [62]. Our findings may also be related to the recent specific-heat results on Ba(Fe<sub>1-x</sub>Co<sub>x</sub>)<sub>2</sub>As<sub>2</sub> [72]. There are two possible contributions to the field dependence of  $1/T_1$  arising from quasiparticle excitations in the mixed state: localized quasiparticles inside vortex cores and delocalized quasiparticles originating from nodes in the SC gap. Since the applied fields are much smaller than  $H_{c2} \approx 52$  T, localized quasiparticles inside vortex cores are unlikely to contribute to the relaxation at these fields ( $H/H_{c2} \leqslant 0.22$ ). In fact, the thermal-conductivity measurements also show a sizable field dependence of  $\kappa_0(H)/T$  at low fields, attaining nearly 70% of the normal-state value even at  $0.2H_{c2}$ , indicative of the predominance of delocalized quasiparticles originating from nodes in the gap, compatible with the existence of a residual DOS in the SC state. The existence of a residual DOS in the SC state of BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> adiffers strikingly from other iron arsenides, including "1111" [7,8,20,32,73-76] and "122" superconductors [77-80], instead resembling the cuprates and heavy fermion superconductors, which have nodes in their SC gap.

As shown in Fig. 23,  $1/T_1$  of <sup>57</sup>Fe in Ba<sub>0.6</sub>K<sub>0.4</sub>Fe<sub>2</sub>As<sub>2</sub> near optimal doping exhibits a  $T^5$ -like dependence well below  $T_c$  [79]. The fairly large exponent of 5 in  $1/T_1$  can be understood by a fully gapped state in Ba<sub>0.6</sub>K<sub>0.4</sub>Fe<sub>2</sub>As<sub>2</sub>, and was analyzed in terms of  $s_{\pm}$ -wave superconductivity with two gaps [79]. In the  $s_{\pm}$  models with unitary scatterings, in-gap states at zero energy can be induced without severely reducing  $T_c$  and can in principle account for the  $1/T_1 \propto T$  behavior. However, the penetration depth  $\Delta\lambda(T) \propto T$  at low temperatures observed in BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> is incompatible with these models, but is consistent with line nodes in the gap. In a symmetry-imposed nodal superconductor such as described by a linenode model  $\Delta = \Delta_0 \sin(2\phi)$ ,  $1/T_1 \propto T^3$  in the clean limit, but impurity scattering induced near gap nodes gives rise to an enhanced  $1/T_1$  that is proportional to temperature at low temperatures. P dopants in BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> can provide a source for nonmagnetic scatterers, consistent with the existence of Fermi-level DOS. In fact, the  $1/T_1$  data of BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> are well fit by the line-node model with  $2\Delta_0/k_BT_c = 6$  and  $N_{res}/N_0 = 0.34$ , where  $N_{res}/N_0$  is the ratio of a residual DOS in the SC state to that in the normal state (see Fig. 23). Therefore, NMR, penetration-depth, and thermal conductivity results on

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BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> are consistent with the existence of line nodes in the SC gap. In the case of nodes imposed by symmetry, a residual DOS at zero energy is a natural consequence of the impurity scattering that broadens the nodes. However, this is not clear for the case of "accidental" nodes not imposed by symmetry, as in the extended *s*-wave case because impurity scattering will lift the nodes and produce a more isotropic gap [81]. Our experimental findings impose significant constraints on candidate theoretical descriptions of iron pnictide superconductivity. The strikingly different behavior of  $1/T_1$  in the SC state between BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> and Ba<sub>0.6</sub>K<sub>0.4</sub>Fe<sub>2</sub>As<sub>2</sub> is surprising because they have comparable  $T_c$  values and similar Fermi surfaces. This implies that high- $T_c$  superconductivities with and without nodes are nearly degenerate and that subtle differences can significantly modify the nature of superconductivity [17,82,81,83,84]. Changes in the pnictogen height may lead to nodal superconductivity, but its  $T_c$  should be much lower than that of fully gapped  $s_{\pm}$  states [82]. However, this is not the case in BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub>. One notable difference inferred from band calculations [54,62] is that BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> may be more three-dimensional than Ba<sub>0.6</sub>K<sub>0.4</sub>Fe<sub>2</sub>As<sub>2</sub>, suggesting that a three-dimensional model is required. Reconciling their comparable  $T_c$  values and fundamentally different SC gap functions needs further theoretical and experimental works. To clarify this problem, identifying the location of the node on Fermi surfaces will be crucial. In order to know how the SC gap evolves with the P-doping, we have systematically measured  $1/T_1$  in the SC state on ther samples with various P concentration.

### 3. Summary

We have shown NMR results obtained in LaFeAs( $O_{1-x}F_x$ ) and BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>. The following results have been obtained:

- 1. Undoped LaFeAsO shows AFM ordering at  $T_N \sim 142$  K,  $\sim 15$  K below the structural transition  $T_S$ . Since AFM fluctuations are enhanced below  $T_S$ , the magnetic transition is intimately coupled with the structural transition. On the other hand, two transitions occur simultaneously with a first-order character in BaFe<sub>2</sub>As<sub>2</sub>. The antiferromagnetic *q* vectors, which are  $(\pi, 0)$  and  $(0, \pi)$  in the "unfolded" Brillouin zone and thus correspond to a stripe-type magnetic structure, are suggested also from the analyses of the <sup>75</sup>As-NMR spectrum.
- 2. From the F-concentration and temperature dependence of  $1/T_1T$ , the low-energy magnetic fluctuations are strongly suppressed by electron doping, and the pseudogap behavior is observed in  $1/T_1T$  for LaFeAs( $O_{1-x}F_x$ ) and LaFeAs $O_{1-\delta}$  with the maximum  $T_c$ . The pseudogap behavior becomes pronounced with F (electron)-doping. The doping dependence of the pseudogap behavior is opposite to that observed in the cuprate superconductors, in which the pseudogap behavior is significant in the underdoped region. The pseudogap behavior is not ascribed to the AFM correlations discussed in the cuprate, but to the character of the band structure near  $E_F$  in the iron-pnictide superconductors.
- 3.  $1/T_1T$  in LaFeAs( $O_{1-x}F_x$ ) depends significantly on the F-concentration, whereas  $T_c$  is insensitive to x within a range from x = 0.04 to 0.14. Almost constant value of  $T_c$  against the F-concentration, irrelevant to the drastic change of  $1/T_1T$  in the normal state, suggests that the spin fluctuations observed through the  $1/T_1$  measurements do not play a vital role for the superconductivity.
- 4. In contrast with LaFeAs( $O_{1-x}F_x$ ), the <sup>31</sup>P-NMR measurements on BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> with various P-doping reveal that two-dimensional AFM fluctuations are notably enhanced with little change in static susceptibility on approaching the AFM phase from the SC dome, and that magnetically ordered temperature  $\theta$  deduced from  $1/T_1T$  vanishes at optimal doping. These results strongly indicate the presence of the quantum critical points, and suggest that the AFM fluctuations with the quantum critical character play a central role in the high- $T_c$  superconductivity. Therefore, we suggest that BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> shares the commonality with heavy-fermion superconductors which are also in the proximity of magnetic ground states.
- 5. The relationship between superconductivity and magnetic fluctuations probed with NMR measurement is quite different between LaFeAs( $O_{1-x}F_x$ ) and BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>. The difference of the relationship is also suggested from phase diagrams of two systems [see in Figs. 9 and 21]. (The AFM phase disappears abruptly, and the SC phase with nearly constant  $T_c$  appears in LaFeAs( $O_{1-x}F_x$ ), but  $T_N$  is gradually suppressed by P-doping, and the SC phase appears as if it covers the magnetic quantum critical point in BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>). However, since the  $1/T_1$  measurements can detect the low-energy magnetic fluctuations (typically ~ mK order), and might fail to detect important magnetic fluctuations if their characteristic energy exceeds the limitation of the NMR experiments, the inelastic neutron experiments over wide *q*-space and energy range are needed for uncovering magnetic fluctuations thoroughly, particularly on "1111" compounds.
- 6.  $1/T_1$  in the SC state on LaFeAs( $O_{1-x}F_x$ ) shows the absence of a coherence peak just below  $T_c$  and the  $T^3$  temperature dependence down to  $\sim 0.2T_c$ . The  $T^3$  dependence in the compounds suggests highly anisotropic superconducting gaps with gap-zero regions along lines, whereas the absences of the field-induced extra relaxation rate and of the residual DOS at low temperatures are incompatible with *d*-wave superconductivity. The absence of the coherence peak in  $1/T_1$  just below  $T_c$  is interpreted in terms of the  $s_{\pm}$ -wave model.
- 7.  $1/T_1$  result in the SC state on BaFe<sub>2</sub>(As<sub>0.67</sub>P<sub>0.33</sub>)<sub>2</sub> shows the existence of a residual DOS at zero energy, which is consistent with the presence of nodes in the SC gap inferred from a field dependence of  $1/T_1$  and from thermal conductivity and penetration-depth results. This suggests that strikingly different SC gaps appear in BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> despite comparable high- $T_c$  values, analogous phase diagrams, and similar FSs with (Ba<sub>1-x</sub>K<sub>x</sub>)Fe<sub>2</sub>As<sub>2</sub>.

### Acknowledgements

Above studies have been done in collaboration with Y. Kamihara, M. Hirano and H. Hosono (Tokyo Institute of Technology) and S. Kasahara, H. Ikeda, T. Shibauchi, Y. Matsuda and T. Terashima (Kyoto University). The authors thank K. Kitagawa, Y. Ihara, D.C. Peets and Y. Maeno for experimental support and discussion, and also grateful to K. Kuroki, H. Kontani, Q. Si and S. Fujimoto for theoretical discussions. The authors were supported by a Grant-in-Aid for Scientific Research on Innovative Areas "Heavy Electrons" (No. 20102006) from The Ministry of Education, Culture, Sports, Science, and Technology (MEXT) of Japan, a Grant-in-Aid for the Global COE Program "The Next Generation of Physics, Spun from Universality and Emergence" from MEXT of Japan, and the Grants-in-Aid for Scientific Research from Japan Society for Promotion of Science (JSPS).

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