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Condensed matter physics in the 21st century: The legacy of Jacques Friedel

Novel superconducting phenomena in quasi-one-dimensional Bechgaard salts



# Des nouveaux mécanismes de supraconductivité dans les sels de Bechgaard quasi-unidimensionnels

Denis Jerome<sup>a,\*</sup>, Shingo Yonezawa<sup>b</sup>

<sup>a</sup> Laboratoire de physique des solides, CNRS UMR 8502, Université Paris-Sud, 91405 Orsay cedex, France <sup>b</sup> Department of Physics, Graduate School of Science, Kyoto University, Kyoto 606-8502, Japan

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(TMTSF)<sub>2</sub>ClO<sub>4</sub>

# ABSTRACT

It is the saturation of the transition temperature  $T_c$  in the range of 24 K for known materials in the late sixties that triggered the search for additional materials offering new coupling mechanisms leading in turn to higher  $T_c$ 's. As a result of this stimulation, superconductivity in organic matter was discovered in tetramethyl-tetraselenafulvalene-hexafluorophosphate, (TMTSF)<sub>2</sub>PF<sub>6</sub>, in 1979, in the laboratory founded at Orsay by Professor Friedel and his colleagues in 1962. Although this conductor is a prototype example for low-dimensional physics, we mostly focus in this article on the superconducting phase of the ambient-pressure superconductor (TMTSF)<sub>2</sub>ClO<sub>4</sub>, which has been studied most intensively among the TMTSF salts. We shall present a series of experimental results supporting nodal *d*-wave symmetry for the superconducting gap in these prototypical quasi-one-dimensional conductors.

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# RÉSUMÉ

La saturation de la température de transition supraconductrice  $T_c$  vers 24 K à la fin des années soixante a stimulé la recherche de nouveaux matériaux avec l'espoir de trouver de nouveaux mécanismes de couplage, conduisant à des  $T_c$  plus élevées. Suite à cette stimulation, la supraconductivité dans la matière organique a été découverte dans le sel organique tétraméthyl-tétraséléfulvalène-hexafluorophosphate, (TMTSF)<sub>2</sub>PF<sub>6</sub>, en 1979 à Orsay dans le laboratoire fondé par le professeur Friedel et ses collègues en 1962. Bien que ce conducteur soit un prototype pour la physique à basse dimension, nous nous intéresserons dans cet article essentiellement à la phase supraconductrice du supraconducteur à pression ambiante (TMTSF)<sub>2</sub>ClO<sub>4</sub>, lequel parmi les sels de TMTSF est celui dont la phase supraconductrice a été étudiée de la manière la plus approfondie.

\* Corresponding author.

E-mail address: denis.jerome@u-psud.fr (D. Jerome).

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Nous présenterons pour ce prototype des conducteurs quasi-unidimensionnels une série de résultats expérimentaux en faveur d'une symétrie nodale de type *d* du gap supraconducteur. © 2015 Académie des sciences. Published by Elsevier Masson SAS. This is an open access article under the CC BY-NC-ND license (http://creativecommons.org/licenses/by-nc-nd/4.0/).

#### 1. Introduction - historical overview

Searching for new materials exhibiting the highest possible values for the superconducting (SC) critical temperature  $T_c$  was a strong motivation in materials science in the early 1970s, and the term "high-temperature superconductor" was already commonly used referring to the intermetallic compounds of the A15 structure, namely materials such as Nb<sub>3</sub>Sn or V<sub>3</sub>Si [1].

Extending the very successful explanation of the isotope effect in the Bardeen–Cooper–Schrieffer (BCS) theory, other models were proposed, in which excitations of the lattice responsible for the electron pairing had been replaced by higher-energy excitations, namely, electronic excitations, with the hope of finding new materials with  $T_c$  higher than those explained by the BCS theory. The small electronic mass  $m_e$  of the polarizable medium would lead to an enhancement of  $T_c$  of the order of  $(M/m_e)^{1/2}$  times the value that is observed in a conventional superconductor where M is an atomic mass. This is admittedly a huge factor. V.L. Ginzburg [2,3] considered in 1964 the possibility for the pairing of electrons in metal layers sandwiched between polarizable dielectrics through virtual excitations at high energy. But, the most provocative suggestion came from W.A. Little in 1964 [4,5], who predicted room-temperature superconductivity with a new pairing mechanism leading to a drastic enhancement of the superconducting  $T_c$ .

The idea of Little was rooted in the extension of the isotope effect proposed by BCS, replacing the mediating phonon by an electronic excitation in especially designed quasi-one-dimensional (Q1D) macromolecules. However, a prerequisite to the model of Little was the achievement of metallic conduction in organic molecular crystals. This was not a trivial problem in the sixties.

A short time later, the synthesis of the first stable organic compound displaying metallic conduction below room temperature, the charge transfer complex TTF–TCNQ came out. This compound is made up of two kinds of flat molecules, each forming segregated parallel conducting stacks. It fulfills the conditions for an organic conductor as the orbitals involved in the conduction ( $\pi$ -HOMO, highest occupied molecular orbital and  $\pi$ -LUMO, lowest unoccupied molecular orbitals for TTF and TCNQ, respectively) are associated with the molecule as a whole rather than with a particular atom. Free carriers within each stack are given by an interstack charge transfer *at variance* with other organic conductors known at that time, such as the conducting polymers, in which charges are provided by doping [6]. However, the conducting behavior in TTF–TCNQ is stopped at low temperature by a metal–insulator transition accompanying a Peierls distortion [7]. The Peierls ground state turned out to be very robust, despite numerous attempts to suppress it under high pressure, making the one-dimensional (1D) conductor more two dimensional (2D) [8,9]. After more than thirty years, the insulating state is found to be almost suppressed at pressures as high as 8 GPa [10].

The clue to overcome the natural tendency for a 1D conductor to undergo a Peierls transition towards an insulating ground state came after a fair amount of experimental works in physics together with chemistry using the newly discovered organic donor tetramethyl-tetraselena-fulvalene TMTSF [11].

The Copenhagen group led by Klaus Bechgaard, very experienced with the chemistry of selenium, succeeded in the synthesis of a new series of conducting salts all based on the TMTSF molecule with the stoichiometry 2:1, namely,  $(TMTSF)_2X$ , where X is an inorganic mono-anion with various possible symmetry, octahedral (PF<sub>6</sub>, AsF<sub>6</sub>, SbF<sub>6</sub>, TaF<sub>6</sub>), tetrahedral (BF<sub>4</sub>, ClO<sub>4</sub>, ReO<sub>4</sub>), or triangular (NO<sub>3</sub>) [11]. All these compounds but the one with  $X = ClO_4$  did exhibit an insulating ground state under ambient pressure.

What is so special with  $(TMTSF)_2PF_6$ , the prototype of the so-called Bechgaard salts, unlike previously investigated TTF– TCNQ, is the magnetic origin of the ambient-pressure insulating state [12] contrasting with the Peierls-like ground states discovered previously in charge-transfer compounds. The ground state of  $(TMTSF)_2PF_6$  turned out to be a spin-density wave (SDW) state as shown in Fig. 1, similar to the predictions made by Lomer [13] in 1962 and by Overhauser [14] for metals. However, the SDW has been suppressed under a hydrostatic pressure of about 9 kbar, enabling the stabilization of metal-like conduction down to liquid helium temperature, and finally the stabilization of superconductivity below 1 K found back in December 1979 [15], as presented in Fig. 2.

Soon after the discovery of superconductivity, it was revealed that the electronic band of  $(\text{TMTSF})_2 X$  can be well modeled with the tight-binding model between TMTSF molecular sites [16–21]. These tight-binding bands agree surprisingly well with recent first-principles band calculations [22–26]. Moreover, it is now established that the Q1D electron gas model with weak-coupling limit explains fairly well key properties of the SDW phases in  $(\text{TMTSF})_2 X$  materials: both the suppression of the SDW phase under pressure [27,28] and the stabilization of magnetic-field-induced SDW phases [29,30]. The non-interacting part of the Q1D electron gas model is defined in terms of a strongly anisotropic electron spectrum yielding an orthorhombic variant of the real open Fermi surface in the *ab* plane of the Bechgaard salts. The spectrum  $E(\mathbf{k}) = v_F(|\mathbf{k}| - \mathbf{k}_F) - 2t_b \cos k_b - 2t'_b \cos 2k_b$  as a function of the momentum  $\mathbf{k} = (k, k_b)$  is characterized by an intrachain or longitudinal Fermi energy  $E_F = v_F k_F$ , which takes a value around 3000 K in  $(\text{TMTSF})_2 X$  [31,21]; here  $v_F$  and  $k_F$  are the longitudinal Fermi velocity and the wave vector. This energy is much larger than the interchain hopping integral  $t_b (\approx 200 \text{ K})$ ,



**Fig. 1.** (a) Side view of the TMTSF molecule (yellow and red dots are selenium and carbon atoms respectively, hydrogens not shown) and (TMTSF)<sub>2</sub>PF<sub>6</sub> Q1D structure seen along the *b* axis, *courtesy* of J.-C. Ricquier, IMN, Nantes. The yellow and green clouds around the atoms schematically present the real-space distribution of molecular orbitals responsible for electronic conduction. (b) Generic phase diagram for the  $(TM)_2X$  family [43] based on experiments on the sulfur compound (TMTTF)<sub>2</sub>SbF<sub>6</sub>. The ambient pressure for this compound is taken as the origin of the pressure scale. The horizontal tics correspond to a ~ 5 kbar interval. All colored phases are long-range ordered. The curve between the 1D metal and charge localization marks the onset of 1D charge localization, which ends at around 15 kbar, slightly above (TMTTF)<sub>2</sub>Br. The 1D to 2D deconfinement occurs on the continuous curve in the higher-pressure regime. The curve between 2D and 3D regimes defines the upper limit for the low-temperature 3D coherent domain. There exists a small pressure window around 45 kbar in this generic diagram, where SC coexists with SDW according to Refs. [44–46]. (TMTSF)<sub>2</sub>ClO<sub>4</sub> is the only compound to exhibit superconductivity under ambient pressure.

in turn much bigger than the second-nearest neighbor transverse hopping amplitude  $t'_b$ . The latter stands as the antinesting parameter of the spectrum, which simulates the main influence of pressure in the model.

The unnesting parameters of the band structure  $t'_b$  and similarly  $t'_c$  for the  $c^*$  direction both play an important role in the T - P and T - P - H phase diagrams of (TMTSF)<sub>2</sub>X. When  $t'_b$  exceeds a critical unnesting band integral of the order of the SDW transition temperature for the complete nesting ( $\approx$  15–30 K) [27,28], the SDW ground state is suppressed in favour of a metallic phase with the possibility of restoration of SDW phases under magnetic field along the  $c^*$  axis [32].

The close proximity between antiferromagnetism and SC ground states of  $(TM)_2 X$  (TM = TMTSF or TMTTF) superconductors and the deviation of the metallic phase from the traditional Fermi-liquid behavior have been recognized as early as in the beginning of the 1980s. The possibility for a pairing mechanism involving carriers on neighboring chains in these Q1D conductors avoiding the Coulomb repulsion has been proposed by V. Emery in the context of the exchange phonon mechanism [33]. Soon after, Emery and coworkers introduced the possibility that antiferromagnetic fluctuations play a role in the pairing mechanism [34,35], but concluded that superconductivity could not emerge from pairing on the same organic chain. The exchange of spin fluctuations between carriers on neighboring chains was thus proposed [34] to provide the necessary glue for pairing in analogy with the exchange of charge density waves proposed by Kohn and Luttinger [36] in the context of a new pairing mechanism in low-dimensional conductors.

In the context of superconductivity in heavy fermions metals discovered the same year as organic superconductivity [37], J. Hirsch performed a Monte Carlo simulation of the Hubbard model. He showed an enhancement of anisotropic spin-singlet pairing correlations due to the on-site Coulomb repulsion, leading eventually to an anisotropic spin-singlet SC state [38].

One year later, L. Caron and C. Bourbonnais [39,40] extended their theory for the generic  $(TM)_2X$  phase diagram to the metallic domain and proposed a gap equation with singlet superconductivity based on an interchain magnetic coupling with an attraction deriving from an interchain exchange interaction overcoming the on-stack Coulomb repulsion. More recently, it has been recognized that, since the Cooper channel (responsible for superconductivity) and Peierls channel (responsible for spin/charge density wave orders) are both diverging at low temperature in 1D conductors, their behaviors in temperature should be treated on equal footing. With the renormalization-group theory, one can take into account the interference between such diverging channels. Such studies have been indeed performed subsequently for Q1D conductors [41]. An overview of the theory of 1D conductors can also be found in the textbook by T. Giamarchi [42].

For several experimental reasons, we are now entitled to attribute the pairing in organic superconductivity to a mechanism that differs from the regular electron–phonon-driven pairing in traditional superconductors. First, the superconductivity of Q1D Bechgaard salts shares a common border with magnetism, as displayed on the generic diagram in Fig. 1(b). Second, strong antiferromagnetic fluctuations exist in the normal state above  $T_c$  in the vicinity of the SDW phase, providing the dominant contribution to the nuclear hyperfine relaxation and also controlling the linear temperature dependence of electronic transport. Third, some experimental results point to the existence of a non-conventional pairing mechanism. These are summarized below.

#### 2. Basic properties of superconductivity

Although superconductivity in organic conductors has first been stabilized under pressure [15] (see Fig. 2), more detailed investigations of this phenomenon have been conducted in  $(TMTSF)_2ClO_4$  for experimental reasons since it is the only com-



Fig. 2. First observation of superconductivity in (TMTSF)<sub>2</sub>PF<sub>6</sub> under a pressure of 9 kbar [15]. The resistance of the two samples is normalized to its value at 4.5 K.

pound among the Q1D Bechgaard salt series that exhibits superconductivity (at 1.2 K) under ambient pressure. Additional evidences for superconductivity in  $(TMTSF)_2X$  conductors came out from  $(TMTSF)_2ClO_4$  transport studies [47], specific-heat measurements [48,49] and Meissner flux expulsion (Fig. 3) [50]. More recent specific-heat data are presented in Section 3.1.

Regarding evidences for the Meissner expulsion, the lower critical field  $H_{c1}$  is obtained from the magnetization curves at low temperature. The obtained values are 0.2, 1, and 10 Oe along the *a*, *b'*, and *c*\* axes, respectively. Following the values for the upper critical fields  $H_{c2}$  derived either from the Meissner experiments and the knowledge of the thermodynamical field [50] or from a direct measurements of transport, superconductivity is in the extreme type-II limit. The Ginzburg– Landau parameter  $\kappa$  can even overcome 1000 when the field is along the *a* axis due to the weak interchain coupling, making field penetration very easy for this external-field configuration. An interpretation of the critical fields assuming the clean limit has been suggested in 1985 [51]. According to this theory, the slopes of  $H_{c2}(T)$  near H = 0 should be given by:

$$H_{c2\parallel a}(T) = \frac{98.7 \times 10^3}{t_{b'} t_{c^*}} T_{c0}(T_{c0} - T)$$
(1)

$$H_{c2 \parallel b'}(T) = \frac{199 \times 10^3}{t_{c^*} t_a} T_{c0}(T_{c0} - T)$$
<sup>(2)</sup>

$$H_{c2 \parallel c^*}(T) = \frac{365 \times 10^3}{t_a t_{b'}} T_{c0}(T_{c0} - T)$$
(3)

where  $H_{c2}$  is given in unit of kOe and the hopping integrals in K. Derivation of the numerical factors are explained in Refs. [51,52]. This proposal was based on the microscopic expressions for the effective mass tensor in the Ginzburg–Landau equation near  $T_c$  [53].

Given  $H_{c2}$  slopes near  $T_c$  of (TMTSF)<sub>2</sub>ClO<sub>4</sub> from transport studies [54,52],  $dH_{c2\parallel a}/dT = -67$  kOe/K,  $dH_{c2\parallel b'}/dT = -36$  kOe/K, and  $dH_{c2\parallel c^*}/dT = -1.5$  kOe/K, Eqs. (1)–(3) lead to band parameters  $t_a: t_{b'}: t_{c^*} = 1200, 310$ , and 7 K, respectively. If one uses slopes from a thermodynamic study [55],  $dH_{c2\parallel a}/dT = -81$  kOe/K,  $dH_{c2\parallel b'}/dT = -23$  kOe/K, and  $dH_{c2\parallel c^*}/dT = -1.1$  kOe/K, we obtain  $t_a: t_{b'}: t_{c^*} = 1800, 250$ , and 6 K. These values are in reasonable agreement with the realistic band parameters [32]

From the slopes of  $H_{c2}(T)$ , one can also deduce the SC coherence lengths  $\xi_i$  ( $i = a, b', c^*$ ), by using formulae  $H_{c2}^{orb} = -0.73T_{c0} dH_{c2}(T)/dT|_{T=T_{c0}}$  [56] and  $H_{c2\parallel i}^{orb} = \Phi_0/(2\pi\xi_j\xi_k)$ , where  $\Phi_0$  is the flux quantum. We obtain ( $\xi_a, \xi_{b'}, \xi_{c^*}$ ) = (620 Å, 330 Å, 14 Å) from the transport phase diagram [52],<sup>1</sup> and ( $\xi_a, \xi_{b'}, \xi_{c^*}$ ) = (1100 Å, 300 Å, 14 Å) from the thermodynamic phase diagram. The obtained coherence lengths are quite anisotropic, reflecting the Q1D nature of (TMTSF)<sub>2</sub>ClO<sub>4</sub>. Note that the coherence lengths  $\xi_a$  and  $\xi_{c^*}$  from the transport may be underestimated because of the enhancement of  $H_{c2} \parallel b'$  due to the field-induced dimensional crossover [57,58]. Also notice that the coherence lengths are much shorter than the mean free path along the *a* axis,  $l_a \sim 1.6 \mu m$  [52]. Thus, this system is well within the clean limit  $\xi \ll l$ .

## 3. Non-s-wave superconducting nature in $(TMTSF)_2 X$

In general, SC states can be classified by symmetries associated with the SC wave function. The SC wave function should be odd under commutation of electrons, because electrons are fermions. The most simple state, assumed in the original

<sup>&</sup>lt;sup>1</sup> The coherence length values in Ref. [52] should be multiplied by  $\sim$  1.4 because of a trivial calculation error.



Fig. 3. Diamagnetic shielding of (TMTSF)<sub>2</sub>ClO<sub>4</sub> at T = 0.05 K for magnetic fields oriented along the three crystallographic axes, from Ref. [50].



**Fig. 4.** Critical fields of  $(TMTSF)_2CIO_4$  determined from the onset temperature of the  $c^*$ -axis resistance  $T_c^{onset}$  for fields along the three principal axes with an indication of the Pauli limit at low temperature. The figure is taken from Ref. [54].

BCS theory and indeed realized in most of superconductors, is the spin-singlet state (i.e. spin state being represented as  $\alpha \mid \uparrow \downarrow - \downarrow \uparrow \rangle / \sqrt{2}$ , with the total spin S = 0) with a *k*-independent isotropic gap. Such a state is called the *s*-wave SC state, in analogy to the atomic *s* orbitals, which is isotropic in the real space. However, gaps anisotropic in the *k* space are possible, e.g., when magnetic interactions are responsible for the Cooper pairing. Such gaps can be classified as *p*, *d*, *f*, ... waves, depending on the rotational symmetry breaking associated with the wave function, again analogously to the atomic wave function. For odd-parity states such as *p*, *f*, ... wave states, odd-commutation conditions require the spin state to be of spin-triplet nature (total spin S = 1, combinations of spin states  $|\uparrow\uparrow\rangle$ ,  $|\uparrow\downarrow + \downarrow\uparrow\rangle/\sqrt{2}$ ,  $|\downarrow\downarrow\rangle$ ). Notice that the spin part for a triplet state is even under commutation. Investigation of non-*s*-wave pairing has been one of the central topics of condensed-matter physics for more than 30 years.

Since the SC phase of  $(TMTSF)_2ClO_4$  is located next to the spin-density wave (SDW) phase as shown in Fig. 1(b), possibility of non-*s*-wave pairing mediated by spin fluctuation has been proposed. Experimentally, early evidences for non-*s*-wave pairing in  $(TMTSF)_2ClO_4$  have been obtained with the spin-lattice relaxation rate  $1/T_1$  measurement with the nuclear magnetic resonance (NMR) technique, which revealed the absence of the coherence peak just below  $T_c$  as well as the power-law behavior at lower temperatures [59]. This behavior is theoretically interpreted as a consequence of non-*s*-wave pairing [60]. Strong suppression of superconductivity by non-magnetic impurities was revealed by using alloyed samples  $(TMTSF)_2(ClO_4)_{1-x}(ReO_4)_x$  [61,62], as described in detail in Section 3.2. Observation of a  $\sqrt{H}$  dependence of the lowtemperature specific heat [55], as well as the temperature dependence of the specific heat in zero field described below, also provides strong evidence of nodal SC state. Furthermore, the in-plane field-angle dependence of the specific heat provides information on the location of nodes, as explained in Section 3.4. We note that several experiments claim fully gapped



**Fig. 5.** (a) Temperature dependence of the specific heat of  $(\text{TMTSF})_2\text{CIO}_4$ . We present data for two different single crystals, sample #1 (0.257 mg; blue circles) and sample #2 (0.364 mg; red squares). The broken curves are fitting results with the Sommerfeld–Debye formula  $C_p/T = \gamma_e + \beta_p T^2$  to the normal state data (T > 1.3 K). Resulting fitting parameters are  $\gamma_e = 10.8 \pm 0.2$  mJ/K<sup>2</sup>mol and  $\beta_p = 12.6 \pm 0.1$  mJ/K<sup>4</sup>mol for sample #1, and  $\gamma_e = 10.6 \pm 0.4$  mJ/K<sup>2</sup>mol and  $\beta_p = 9.8 \pm 0.2$  mJ/K<sup>4</sup>mol for sample #2. (b) Electronic specific heat  $C_{el}/T$  of the two samples.

states: the thermal conductivity [63] reveals electronic thermal conductivity vanishes exponentially below  $T_c$  after subtraction of phonon contribution; in-field muon spin rotation ( $\mu$ SR) [64] revealed the temperature dependence of the penetration depth, suggesting a fully gapped state, but only in magnetic fields. Nevertheless, we believe that so far the nodal SC scenario has been accumulating more direct evidence. We also note that zero-field  $\mu$ SR measurement [64] could not detect spontaneous time-reversal symmetry breaking (i.e. spontaneous magnetization) in the SC state, excluding the possibility of "chiral" SC state. Experiments on superconductivity in (TMTSF)<sub>2</sub>X are also reviewed excellently in Refs. [65–68].

Theoretically, as already explained, the spin-fluctuation pairing mechanism in  $(TMTSF)_2X$  has been proposed as early as 1986 [34]. A tremendous amount of theories have been proposed, because of the simplicity of the Q1D electronic structure in  $(TMTSF)_2X$ , as well as the stimulation by interesting experiments. Microscopic theories considering spin and/or charge fluctuations have proposed unconventional SC state, not only spin-singlet *d*-wave-like states, but also spin-triplet *p*-wave-like or *f*-wave-like states, based on methods such as random phase approximation (RPA) or fluctuation exchange (FLEX) theories [69–75], quantum Monte Carlo method [76–78], perturbation theory [79], and RG theory [80–84]. Considering only the single pair of Fermi surface sheets, which is the electronic band structure for  $(TMTSF)_2PF_6$ , *s* or *p*-wave-like states can be fully gapped, whereas *d* or *f*-wave-like states should have nodes on the Fermi surface. In the case of  $(TMTSF)_2CIO_4$ , the Fermi surface consists of two pairs of sheets at low temperatures because of the band folding due to the anion ordering below  $T_{AO} = 24$  K [21]. For such "folded" Fermi surfaces, it has been pointed out that a fully-gapped *d*-wave-like state is also possible [85]. For more details of theories, see review articles such as Refs. [86,58,66].

#### 3.1. Specific heat data

Recent new results of the temperature dependence of the specific heat  $C_p$  are presented in Fig. 5. This data is obtained by the ac technique [87] and using only one single crystal. To improve the accuracy of the obtained data, we measured the dependence of the temperature oscillation amplitude  $T_{ac}$  on the heater-current frequency f and we fitted the  $T_{ac}(f)$  data with the theoretical function  $T_{ac}(f) = P/(8\pi f C_p)[1 + (4\pi f \tau_1)^2 + (4\pi f \tau_2)^{-2}]^{-1/2}$  to obtain  $C_p$ , where  $\tau_1$  and  $\tau_2$  are the external and internal relaxation rates, respectively. More details will be published elsewhere. In Fig. 5, we compare results for different samples. Both samples exhibit sharp anomalies at around  $T_c \sim 1.2$  K, indicating bulk superconductivity. The electronic specific-heat coefficient is found to be  $\gamma_e = 10.6-10.8$  mJ/K<sup>2</sup>mol, in good agreement with the previous works ( $\gamma_e = 10.5$  mJ/K<sup>2</sup>mol) [48,49], although the phononic specific heat coefficient exhibits ~ 20% variation depending on the samples, but still comparable to  $\beta_p = 11.4$  mJ/K<sup>4</sup>mol reported in Ref. [49]. In addition, it can be checked from the data in Fig. 5(b) that the entropy of the SC state at  $T_c$  equals that of the normal state at the same temperature within ~ 13% for both samples.

Fig. 5(b) displays several features supporting a non-s-wave pairing state. Firstly, the height of the specific-heat jump at  $T_c$ ,  $\Delta C$ , nearly equals to  $\gamma_e T_c$ . This is notably smaller than the expectation of the BCS theory, in which  $\Delta C/\gamma_e T_c$  is expected to be 1.43. Instead, it is known that  $\Delta C/\gamma_e T_c$  can be smaller than 1.43 if the SC gap has substantial anisotropy. In particular, if the gap has line nodes, the ratio can be even smaller than 1.0 [88,33]. Secondly,  $C_{el}/T$  exhibits linear temperature dependence in a wide temperature range below ~ 0.7 K. Such linear behavior also evidences a nodal SC gap. The finite intercept for the linear extrapolation of  $C_{el}/T$  to zero temperature is expected in the case of a finite elastic scattering time [89]. Using the data for sample # 1, the residual density of states amounts to about 18.5% of the value of the normal state according to Fig. 5(b). This will be further commented on in the next section.



**Fig. 6.** Phase diagram of  $(\text{TMTSF})_2(\text{CIO}_4)_{(1-x)}(\text{ReO}_4)_x$ , governed by non magnetic disorder. The data are obtained by newly analysing the temperature dependence of resistivity reported in Ref. [62] (see text). Points with labels "R" refer to very slowly cooled samples in the R-state (the so-called relaxed state) with different ReO<sub>4</sub><sup>-</sup> contents, whereas points with labels "Q" refer to quickly cooled samples in the quenched state. A sample with  $\rho_0 = 0.27 \ \Omega$ -cm, i.e. beyond the critical defect concentration, is metallic down to the lowest temperature of the experiment. The continuous curve is a fit of Eq. (4) to the data with  $T_c^0 = 1.23$  K.

#### 3.2. Non-magnetic defects

A basic property of the *s*-wave superconductivity proposed in the BCS theory is the isotropic (*k*-independent) gapping on the Fermi surface. Hence, no pair breaking is expected from the scattering of electrons against spinless impurities [90], since such scattering essentially just mixes and averages gaps at different *k* positions. Experimentally, this property has been verified in non-magnetic dilute alloys of *s*-wave superconductors and provided a strong support to the BCS model of conventional *s*-wave superconductors. However, the condition for isotropic gap is no longer met for the case of non-*s*-wave pairing, in which the average of the gap  $\Delta(\mathbf{k})$  over the Fermi surface vanishes due to sign changes in  $\Delta(\mathbf{k})$ , i.e.  $\sum_{FS} \Delta(\mathbf{k}) \sim 0$ . Consequently,  $T_c$  for these superconductors should be strongly affected by any non-magnetic scattering, cancelling out the positive and negative parts of the gap. Theories on effects of non-magnetic impurities on  $T_c$  in such superconductors have been deduced by generalizing the conventional pair-breaking theory for magnetic impurities in *s*-wave superconductors. Then the famous relation,

$$\ln\left(\frac{T_{\rm c}^0}{T_{\rm c}}\right) = \psi\left(\frac{1}{2} + \frac{\alpha T_{\rm c}^0}{2\pi T_{\rm c}}\right) - \psi\left(\frac{1}{2}\right) \tag{4}$$

is obtained [91,92], with  $\psi(x)$  being the Digamma function and  $\alpha = \hbar/2\tau k_B T_c^0$  the depairing parameter related to the elastic scattering time  $\tau$ . Experimentally, it has been found that this relation holds for non-s-wave superconductors such as Sr<sub>2</sub>RuO<sub>4</sub> ( $T_c = 1.5$  K; most likely a *p*-wave spin-triplet superconductor) [93,94].

It is also the remarkable sensitivity of organic superconductivity to irradiation detected in the early years [95,96] that led Abrikosov to suggest the possibility of triplet pairing in these materials [97]. A more recent investigation of the influence of non-magnetic defects on organic superconductivity has been conducted following a procedure that rules out the addition of possible magnetic impurities, which is the case for X-ray-irradiated samples [98]. Attempts to synthesize non-stoichiometric compounds have not been successful for these organic salts. However, what turned out to be feasible is an iso-electronic anion solid solution keeping the charge transfer constant. One attempt has been made to create non-magnetic disorder through the synthesis of solid solutions with centrosymetrical anions such as  $AsF_6$  and  $SbF_6$ . This attempt turned out to be unsuccessful, as the effect of disorder happened to be very limited, with only a minute effect on  $T_c$  [99].

Another scheme with which non-magnetic defects can be introduced in a controlled way for non-centro-symetrical anions in the  $(TMTSF)_2X$  series is either by fast cooling, preventing the complete ordering of the tetrahedral ClO<sub>4</sub> anions or by introducing ReO<sub>4</sub> anions to the ClO<sub>4</sub> site by making the solid solution  $(TMTSF)_2(ClO_4)_{(1-x)}(ReO_4)_x$ . As displayed in Fig. 6, superconductivity in the solid solution is suppressed and the reduction in  $T_c$  is clearly related to the residual resistivity, the enhancement of the elastic scattering in the normal state. The data in Fig. 6 show that the relation  $T_c$  versus  $\rho_0$  follows Eq. (4) with good accuracy, with  $T_c^{0} = 1.23$  K.

At this stage, it is worth pointing out that the determination of the residual resistivity is not a trivial matter. Various procedures have been used in the literature. First, the resistivity displays an usual quadratic temperature dependence both above the anion ordering temperature  $T_{AO} = 24$  K and below down to approximately 10 K. Consequently, a first attempt to determine  $\rho_0$  was to extrapolate  $\rho(T)$  down to zero temperature the quadratic behavior observed between  $T_{AO}$  and 10 K. It turned out that  $\rho_0$  is rather ill defined with this procedure (see Ref. [62]). Second, another procedure was to use a linear extrapolation of the temperature dependence below 10 K down to  $T_c$ , leading to lower values of  $\rho_0$  [61]. However, several



**Fig. 7.** <sup>77</sup>Se Knight shift (a) and  $1/T_1$  vs *T* (b) for (TMTSF)<sub>2</sub>ClO<sub>4</sub>, for H//b' and *a*, according to reference [103]. The sign of the variation of the Knight shift at  $T_c$  depends on the sign of the hyperfine field. A linear temperature dependence of the relaxation rate is recovered at very low temperature, signaling the existence of unpaired carriers at the Fermi level.

recent re-analysis of the temperature dependence of the resistivity in the neighborhood of  $T_c$  in pure (TMTSF)<sub>2</sub>ClO<sub>4</sub> [100] and in the alloy series [101] have emphasized the existence of two different regimes: a regime between 10 and 2 K where the single particle scattering is dominated by antiferromagnetic fluctuations leading in turn to a linear dependence, and another regime between 2 K and  $T_c$ , where the downturn of the resistivity can be ascribed to the sliding of SDW waves without any transverse coherence in the vicinity of an antiferromagnetic order. The latter is not accessible in (TMTSF)<sub>2</sub>ClO<sub>4</sub>, since it would require a negative pressure as shown by elongation experiments along the b' axis [102]. The procedure used to derive  $\rho_0$  in Fig. 6 is a linear extrapolation to zero temperature of the linear regime between 2 and 10 K dominated by scattering against AF fluctuations. This procedure should be rather accurate, in particular in (TMTSF)<sub>2</sub>ClO<sub>4</sub>.

It has been checked that the additional scattering cannot be ascribed to magnetic scattering with the electron paramagnetic resonance (EPR) technique, which shows no additional traces of localized spins in the solid solution. Thus, the data in Fig. 6 cannot be reconciled with the picture of a SC gap keeping a constant sign over the whole  $(\pm k_F)$  Fermi surface. They require a picture of pair breaking in a superconductor with an anisotropic gap symmetry.

It is interesting to compare the residual density of states predicted by theories with experimental data. Fig. 6 shows that the depairing parameter of the pristine sample amounts to about 6.25% of the critical value for the suppression of superconductivity. Given the ratio  $\Gamma/\Gamma_0 = 0.0625$  for the pristine sample where  $\Gamma$  is the scattering rate, the calculation of Sun and Maki [89] leads in turn to a residual density of states  $N(0) = 0.26N_0$ , which is fairly close to the residual density of states derived from our specific heat experiments, see the previous subsection. In the NMR data in Ref. [103], the spin lattice relaxation rate  $1/T_1$  below 0.2 K amounts to ~25% of that in the normal state. Since,  $1/T_1$  is proportional to the square of the density of states, the observed residual value of  $1/T_1$  corresponds to ~50% of the density of states remaining in the SC state. Such a residual density of states from NMR compares very favorably with the value 18.5% provided by the measurement of the electronic specific heat. The larger value found by NMR can be attributed to the field dependence of the density of states, as reported in Ref. [55], since NMR data have been taken under magnetic field  $\mu_0 H = 0.96$  T along the b' axis or 1.3 T along the a axis.

The influence of non-magnetic impurities on the SC phase implies the existence of positive as well as negative values for the SC order parameter on the Fermi surface. It precludes the usual case of *s*-symmetry but is still unable to discriminate between two possible options namely, singlet-d(g) or triplet-p(f) [81] (see Fig. 8).

#### 3.3. Spin susceptibility in the superconducting phase

The detailed study of the behavior of static and dynamic properties electron spins has been undertaken via the <sup>77</sup>Se Knight shift and  $1/T_1$  measurements across  $T_c$  in the compound (TMTSF)<sub>2</sub>ClO<sub>4</sub> [103].

The Knight shift is revealed to decrease below  $T_c$ , as presented in Fig. 7(a), providing solid evidence in favour of spinsinglet pairing. Furthermore, the temperature dependence of the relaxation rate shown in Fig. 7(b) does not display the exponential behavior expected in a regular fully gapped *s*-wave superconductor, but instead a power-law dependence below  $T_c$  with a linear regime taking place below 0.2 K, showing that there is a non-zero density of states at the Fermi level. Because  $1/T_1T$  is proportional to the square of the density of states, the observed residual  $1/T_1T$  value amounting to 25–30% of the density in the normal state indicates that the density of states is recovered by 50% at  $\mu_0 H = 0.96$  T for  $H \parallel b'$  and  $\mu_0 H = 1.3-1.4$  T for  $H \parallel a$ .

Moreover, a steep increase in the spin-lattice relaxation rate versus the magnetic field for both field orientations parallel to a and b' has provided the evidence of a sharp cross-over or even a phase transition occurring at low temperature under

Symmetry	S	р	d	f	g
Sensitivity to impurities		1	1	1	1
NMR Knight shift and $1/T_1$			~		1
Specific heat (Doppler shift)			1	(√)	1

Fig. 8. Possible gap symmetries agreeing with the different experimental results. The spin-singlet *d*-wave (or *g*-wave) symmetry is the only symmetry agreeing with all experiments (yellow columns on line).



**Fig. 9.** Schematic description of the Volovik effect in a superconductor with gap nodes or zeros. (a) Supercurrent flowing around magnetic vortices. Supercurrent velocity  $\mathbf{v}_s$  is perpendicular to the vortex direction, namely the direction of the magnetic field. (b) Quasiparticle excitation around gap nodes excited by the Volovik effect. (c) Quasiparticle excitation when the field is parallel to the Fermi velocity at a node. In such a situation, the excitation at this node is zero, since  $\mathbf{v}_s \cdot \mathbf{v}_F = 0$  at this node.

a magnetic field between 1 and 2 Tesla from the low-field *d*-wave singlet phase and a high-field regime exceeding the paramagnetic limit  $H_P$  being either a triplet-paired state [104,105] or an inhomogeneous Fulde–Ferrell–Larkin–Ovchinnikov state [106,107]. The nature of this high-field phase is further discussed in Section 4.

According to the NMR data, a spin-singlet pairing is clearly established for the SC state of  $(TMTSF)_2ClO_4$ . Quite a different situation had been claimed in an earlier <sup>77</sup>Se NMR study of the SC phase of  $(TMTSF)_2PF_6$  [108]. The <sup>77</sup>Se Knight shift revealing no change through  $T_c$  had been taken as a strong suggestion in favor of spin-triplet superconductivity in  $(TMTSF)_2PF_6$ . However, it can be noticed that the experiment in  $(TMTSF)_2PF_6$  had been conducted under a relatively high magnetic field of  $\mu_0 H = 1.43$  T aligned along the most conducting *a* axis. Following the results in  $(TMTSF)_2ClO_4$  and, in particular, the relaxation-rate data of the latter compound displayed in Fig. 15, a field of 1.43 T may have been high enough to place the sample in the high-field SC phase discussed in Section 4, for which the density of states does not reveal any noticeable change through the SC transition. This is corroborated by the data of the Korringa relaxation rate in  $(TMTSF)_2PF_6$ , showing hardly any change after crossing  $T_c$  (see Fig. 5 in Ref. [108]). In conclusion, although different symmetries for the order parameter in  $(TMTSF)_2CIO_4$  and  $(TMTSF)_2PF_6$  cannot be totally ruled out, we consider such a scenario as quite unlikely.

#### 3.4. Magneto-calorimetric studies

In addition to the spin state, the orbital gap structure of the SC state is also fundamentally important information. As we explained in the preceding sections, evidence for a non-s-wave pairing state in  $(TMTSF)_2X$  had been accumulated. To reveal more precise gap structures, one of the common techniques is to measure the field-angle-dependent quasiparticle excitations. As first proposed by Volovik [109], superconductors with nodes (or zeros) exhibit field-dependent quasiparticle excitation with momentum close to the nodal position, induced by the energy shift  $\delta\omega$  caused by the supercurrent surrounding vortices penetrating the sample. Such field-induced excitations are now called the Volovik effect. This quasiparticle excitation is also field-direction dependent [110], because  $\delta\omega$  is proportional to the inner product of the Fermi velocity  $\mathbf{v}_F$  at the node and the superfluid velocity  $\mathbf{v}_s$ , the latter being in turn perpendicular to the applied field. Thus, if one rotates the magnetic field within a certain plane, it is expected that the quasiparticle density of states oscillates as a function of the field angle. Such oscillation can be detected by measuring, for example, the specific heat or thermal conductivity while rotating the magnetic field within the conducting plane. Indeed, such studies have been widely performed in three-dimensional (3D) or quasi-two-dimensional (Q2D) tetragonal systems such as CeCoIn<sub>5</sub> [111,112], YNi<sub>2</sub>B<sub>2</sub>C [113], Sr<sub>2</sub>RuO<sub>4</sub> [114,115], and many other materials [116].

In contrast to Q2D systems, the story for Q1D systems is not so simple, because substantial in-plane anisotropy of  $H_{c2}$  leads to pronounced specific-heat oscillation as a function of the in-plane field angle, even concealing the oscillation originating from the gap anisotropy. In addition, one should be careful that the Fermi velocity  $\mathbf{v}_{\rm F}$  and the Fermi wavenumber  $\mathbf{k}_{\rm F}$  are *not* necessarily parallel to each other (see Fig. 9(b)). More specifically,  $\mathbf{v}_{\rm F}$ , which is parallel to the gradient of the quasiparticle energy  $\varepsilon(\mathbf{k})$  in the reciprocal space and thus is perpendicular to the Fermi surface, is not always parallel to  $\mathbf{k}_{\rm F}$ ,



**Fig. 10.** (a)–(f) Observed in-plane field-angle dependence of the heat capacity of  $(TMTSF)_2CIO_4$  [55]. Blue curves in panels (a)–(c) are C/T obtained at 0.14 K and red curves in (d)–(f) are at 0.50 K. The black curves indicate C/T plotted against  $-\phi$ . The difference between the colored and the black curves represents the asymmetry of the  $C(\phi)/T$  curve. The curves in (g) are simulated results by calculating the density of states based on a simple Doppler-shift model with nodes at  $\phi = \pm 10 \text{ deg}$  [55]. The definition of the in-plane field angle  $\phi$  is indicated at the bottom-right corner.

which is the vector pointing at a k position on the Fermi surface from the origin of the reciprocal space (the  $\Gamma$  point). In Q1D systems, this is almost always the case. Therefore, even if the specific-heat oscillation originating from the gap is observed, the field direction where the specific heat exhibits an anomaly does not have any direct relation to the gap node position in the k space: one can only obtain the direction of the Fermi velocity at nodes from the field-angle-dependent quasiparticle excitation. To reveal the gap structure in k-space, one should know the band structure of the material. For these reasons, the gap-structure investigation of Q1D superconductors by the field-angle-induced quasiparticle excitation had not been explored.

Recently, such experiments were reported by Yonezawa et al. [55,117], who developed a highly sensitive calorimeter based on the "bath modulating method" [118] and measured the field-strength and field-angle dependence of the heat capacity of one single crystal of (TMTSF)<sub>2</sub>ClO<sub>4</sub>. The in-plane field-angle  $\phi$  dependence presented in Fig. 10 is of particular interest. In addition to the large oscillation in the heat capacity originating from the in-plane anisotropy of  $H_{c2}$ , additional kink structures in  $C(\phi)$  curves are observed. The kinks are located at  $\phi = \pm 10 \text{ deg}$ ; i.e. for fields  $\pm 10 \text{ deg}$  away from the crystalline *a* axis within the *ab* plane.

By comparing the experimental data with a simple simulation shown in Figs. 10(g), 11(c), and 11(d), it is suggested that  $\pm$ 10 deg is the direction of  $\mathbf{v}_{\rm F}$  at the gap nodes. Nagai et al. [23] calculated the field-angle dependence of the specific heat based on the quasiclassical framework together with the first-principles band calculations, and they deduced similar conclusions. Thus, it is now clarified that the Fermi-surface positions at which  $\mathbf{v}_{\rm F}$  is pointing  $\pm$ 10 deg away from the *a* axis are candidate nodal positions in the *k* space.

Based on the Fermi surface obtained by the tight-binding band calculation [21], Yonezawa et al. proposed that the *d*-wave-like state with nodes at  $k_y = \pm 0.25/b^*$  best matches with experiment [55]. Here,  $k_y$  is the wavevector perpendicular to the *a* axis and  $b^* = \pi/b$  is the size of the first Brillouin zone along the  $k_y$  direction. Considering the nesting vectors of the Fermi surface of (TMTSF)<sub>2</sub>ClO<sub>4</sub>, this state is likely to be realized if intra-band nesting plays the dominant role for Cooper pairing [117].

One comment should be made here; there is still a debate concerning the detailed Fermi-surface shape of (TMTSF)<sub>2</sub>ClO<sub>4</sub>. The conclusion of the nodal position in the *k* space strongly depends on the assumption of the Fermi-surface shape, which is affected by the anion gap  $\Delta_a$ . A value of  $\Delta_a \sim 100$  meV has been used in the tight-binding-model calculation [21], and for the analysis of the specific-heat data [55]. On the other hand, Nagai et al. [23] recently performed first-principles band calculation for the anion-ordered low-temperature crystal structure of (TMTSF)<sub>2</sub>ClO<sub>4</sub>, and evaluated  $\Delta_a$  as nearly zero. As a result, the calculated Fermi surfaces nearly touch each other. Another first-principles calculation by Alemany et al. [25] revealed small but sizable anion-order effect with  $\Delta_a \sim 14$  meV, accompanied by a weak anti-crossing between



**Fig. 11.** (a) In-plane field-angle dependence of the heat capacity of  $(\text{TMTSF})_2\text{ClO}_4$  near  $\phi = 0 \text{ deg [55]}$ . The arrows indicate positions of the observed kinks. (b) First and second derivatives of  $C(\phi)/T$ . Anomalies at  $\phi = \pm 10 \text{ deg corresponding to the kinks in } C(\phi)/T$  are easily seen. Calculated density of states *N* and their derivatives based on a simple Doppler shift model with nodes at  $\phi_{n1} = -10 \text{ deg are plotted in (c) and (d)}$ .

the split bands. Thus the resultant Fermi surfaces are well separated in the *k* space. More recent calculation by Aizawa et al. obtained a similar gap value  $\Delta_a \sim 8.7$  meV [26]. Experimentally,  $\Delta_a$  should be finite but seems to be no more than 25 meV [119,120]. A value around 14 meV is confirmed by a recent analysis of magnetoresistance oscillations in (TMTSF)<sub>2</sub>ClO<sub>4</sub> by G. Montambaux and D. Jérome [121].

Returning back to the nodal SC gap structure, the *d*-wave-like state with nodes at  $k_y = \pm 0.25b^*$  remains a candidate structure even with  $\Delta_a = 0$  meV, according to the detailed analysis [117], at least within the tight-binding model. Experimental determination of  $\Delta_a$  and analyses based on the relevant band structure are still necessary to resolve the nodal structure. In addition, microscopic theories on the gap structure based on realistic band structures are also important to finally settle this issue of the exact nodal positions.

#### 4. High-field superconducting state

As already mentioned in previous sections,  $(TMTSF)_2X$  salts have been known to exhibit a divergent behavior of the transport  $H_{c2}$  with decreasing temperatures. The origin of this behavior has been attributed to spin-triplet pairing or to the Fulde–Ferrell–Larkin–Ovchinnikov (FFLO) states [122,123,57,124–129,104,130,131,73,132,133]. In case of  $(TMTSF)_2ClO_4$ , the former is excluded, since a clear decrease in the spin susceptibility is observed [103] as described in Section 3.3. In addition, sudden increase of the nuclear-lattice relaxation rate  $1/T_1$  observed above around 2 T [103] was considered as a consequence of the formation of unusual high-field SC phases.

The FFLO state [106,107] can be realized when spin-singlet Cooper pairs are formed among Zeeman-split Fermi surfaces in high magnetic fields [134]. Due to the Zeeman split, the Fermi wavenumber for the up-spin electron  $\mathbf{k}_{F\uparrow}$  and that for the down-spin electron  $\mathbf{k}_{F\downarrow}$  are not equal. Thus, when a Cooper pair is formed between  $\mathbf{k}_{F\uparrow}$  and  $-\mathbf{k}_{F\downarrow}$  electrons as presented in Fig. 12, the pair acquires the non-zero center-of-mass momentum  $\mathbf{q}_{FFLO} = \mathbf{k}_{F\uparrow} - \mathbf{k}_{F\downarrow}$ . This momentum results in the spatial oscillation of the SC order parameter. This means that the FFLO state is accompanied by the translational symmetry breaking. In particular, for Q1D systems,  $\mathbf{q}_{FFLO} = \mathbf{k}_{F\uparrow} - \mathbf{k}_{F\downarrow}$  should be nearly fixed to the *a* axis, since the number of pairs can be maximized if  $\mathbf{q}_{FFLO}$  matches with the nesting vector between the spin-up and spin-down Fermi surfaces, which is nearly parallel to the *a* axis, as schematically shown in Fig. 12(b). Indeed, it is theoretically shown that the FFLO state with  $\mathbf{q}_{FFLO} \parallel a$  generally acquires high  $T_c$  in a Q1D system [135]. Observation of unusual phenomena resulting from the symmetry breaking with such a fixed  $\mathbf{q}_{FFLO}$  can be a hallmark of the Q1D FFLO state.

There are only a few candidate materials for the FFLO state. The heavy Fermion compound CeCoIn<sub>5</sub> clearly exhibits an unusual high-field phase [136,137]. However, this phase may not be a textbook-like FFLO state, since the phase is revealed to be accompanied by antiferromagnetic ordering [138]. Other leading candidates are the two-dimensional organic super-conductors  $\kappa$ -(BEDT-TTF)<sub>2</sub>Cu(NCS)<sub>2</sub> and  $\lambda$ -(BETS)<sub>2</sub>FeCl<sub>4</sub>. In the former, the existence of additional high-field SC phase has been confirmed by magnetic and thermodynamic measurements [139,140], as well as by an NMR study [141]. More recently, substantial increase of  $1/T_1$  attributable to the Andreev reflections originating from the order-parameter modulation



Fig. 12. Schematic comparison between FFLO pair formations for (a) 3D or 2D Fermi surfaces and (b) Q1D Fermi surfaces.

is observed [142]. In the latter compound, an oscillatory behavior in the electric resistivity due to the vortex flow is observed [143]. This behavior is believed to be a consequence of the "locking" effect between vortices and order-parameter modulation. Its sister compound  $\lambda$ -(BETS)<sub>2</sub>GaCl<sub>4</sub> also exhibits a signature of the FFLO state [144].

For (TMTSF)<sub>2</sub>ClO<sub>4</sub>, only the unusual divergent-like behavior of  $H_{c2}(T)$  for  $H \parallel b'$  had been known for the high-field state [145,146]. In 2008, Yonezawa et al. investigated the in-plane field-angle dependence of the onset temperature of superconductivity,  $T_c^{\text{onset}}$ , based on the  $c^*$ -axis resistance measurements of (TMTSF)<sub>2</sub>ClO<sub>4</sub> single crystals [54,52]. They made use of the anisotropy of  $H_{c2}$  to accurately deduce  $T_c^{\text{onset}}$ : they compared the resistance in fields exactly parallel to the *ab* plane to those in fields tilted away from the *ab* plane only by a few degrees. The  $c^*$  axis component of the field induced by the tilting destroys the superconductivity, allowing one to extract the contribution of superconductivity by comparing resistances for the two field directions.

It is revealed that, not only for  $H \parallel b'$ , but also for  $H \parallel a$ ,  $T_c^{\text{onset}}$  remains finite up to 5 T, the maximal field achieved in this study, as shown in Fig. 4. In particular, the onset curve for  $H \parallel a$  exhibits a peculiar "S" shape, a limited behavior at around 0.8 K and a further increase below 0.3 K. The behavior for  $H \parallel a$  resembles that observed in the pressure-induced superconductivity in  $(\text{TMTSF})_2\text{PF}_6$  [147], and is recently theoretically treated within the FFLO scenario [133,135]. What is more, unusual modulation in in-plane field-angle  $\phi$  dependence of  $T_c^{\text{onset}}$  is observed above 3.0 T. In particular, the maxima of the  $T_c^{\text{onset}}(\phi)$  curve, which is located at  $\phi = 0 \text{ deg} (H \parallel a)$  and  $\phi = 90 \text{ deg} (H \parallel b')$  at low fields: the latter is found to shift away from the crystalline b' axis at high fields. This is in some sense a (quasi) field-induced breaking of symmetry.<sup>2</sup> To the best of our knowledge, such a modulation in  $T_c$  has never been reported in any other FFLO candidates. In addition, the high-field state is sensitively suppressed by a tiny amount of impurities [52] (Fig. 13(b)).

This unusual phenomena is interpreted as a consequence of the formation of FFLO states. In FFLO states, the modulation vector  $\mathbf{q}_{\text{FFLO}}$  of the SC order parameter breaks the translational symmetry of the SC state, and may lead to unusual field-angle dependence of  $T_c^{\text{onset}}$ . Such an interpretation has been indeed supported by recent theories. Croitoru and Buzdin [148, 149] found that  $T_c(\phi)$  exhibits unusual  $\phi$  dependence once the system is in the FFLO state, by solving linearized Eilenberger equations for *s*-wave superconductivity in a highly anisotropic quasi-two-dimensional (Q2D) model. More recently, they revealed similar results by quasiclassical formalisms for an *s*-wave model with a more-realistic Q1D band [150] and for a *d*-wave model but with a Q2D band [151].

It is then natural that much effort has been devoted to search for thermodynamic evidence of the realization of the high-field FFLO phase. Interestingly, a specific-heat study with accurately aligned magnetic fields revealed that an anomaly in the specific heat at  $T_c^{\text{onset}}$  cannot be detected [55]: For field directions along the three principal axes, the only detected anomaly is located close to the curve below which resistivity is zero, as shown in Fig. 14. (This may be just a coincident, since in some experiments the zero-resistance state is observed up to around 3 T for  $H \parallel a$  and  $H \parallel b'$  [146,103]. Also see Fig. 15.) The field at which the specific heat anomaly is detected and the specific heat recovers its normal state value should be assigned as the thermodynamic  $H_{c2}$ , and above this field superconductivity has a density of states nearly equal to that in the normal state. Nevertheless, the resistivity anomaly observed above the thermodynamic  $H_{c2}$  is quite robust and has been reproduced by several groups [145,146,54].

One possible explanation is that the density of states in the high-field FFLO state is nearly equal to that in the normal state, because of the zero-gap region in real space originating from the order-parameter modulation [106]. This is reasonable, but experimental efforts to reveal the thermodynamic phase boundary between the FFLO state and normal state is highly required to support the scenario. Another explanation is that the high-field FFLO region intrinsically acquires fluctuating nature, probably assisted by the low-dimensional electronic state in this material. We emphasize here that, even with fluctuating superconductivity, the observed anomalous behavior in  $T_c^{\text{onset}}(\phi)$  is rather difficult to be explained without (quasi-)symmetry breaking in the underlying pairing channel.

<sup>&</sup>lt;sup>2</sup> Since the crystal structure of (TMTSF)<sub>2</sub>ClO<sub>4</sub> belongs to the triclinic space group, any spatial symmetry except for the inversion symmetry is already broken by the lattice. Therefore, strictly speaking, it is not accurate to say "symmetry breaking by the magnetic field" in the present case. Nevertheless,  $T_c^{\text{onset}}(\phi)$  exhibits nearly a mirror symmetry with respect to the *a* and *b'* axes in low field.



**Fig. 13.** (a) Polar plot of the  $\phi$  dependence of  $T_c^{\text{onset}}$  at several magnetic fields. The red line indicates the new principal axis emerging above 3 T [54]. (b) Comparison of  $T_c^{\text{onset}}(\phi)$  for different samples [52]. The blue and red points indicate  $T_c^{\text{onset}}$  of Sample #1 (very clean) and Sample #2 (moderately clean), respectively. Substantial difference is seen for  $|\phi| > 19 \text{ deg}$ , whereas the sample dependence is rather small for smaller field angles. This difference is attributed to the fact that the FFLO state, as well the field-induced 2D confinement for  $H \parallel b'$ , is very sensitive to impurity scatterings.



**Fig. 14.** SC phase diagram of  $(TMTSF)_2CIO_4$  obtained by the specific heat (filled points) and resistivity measurements (crosses) for (a)  $H \parallel a$ , (b)  $H \parallel b'$ , and (c)  $H \parallel c^*$ . Figures are made based on data in Refs. [54,55]. Notice that the vertical scale of the panel (c) is 20 time smaller than those of the other panels.

#### 5. Metallic state above $T_c$ : antiferromagnetic fluctuation and its relation to superconductivity

Interestingly, the metallic phase of  $(TMTSF)_2PF_6$  in the 3D coherent regime when pressure is in the neighborhood of the critical pressure  $P_c$  behaves in a way far from what is expected for a Fermi liquid. This behavior indicates the dominance of quantum critical fluctuations near  $P_c$ . Moreover, close relation between the non-Fermi-liquid behavior and superconductivity has been recently revealed both experimentally and theoretically, as described in detail below.

Experimentally, NMR measurements of  $1/T_1$  have probed antiferromagnetic fluctuations. The canonical Korringa law,  $1/T_1T \propto \chi^2(q=0,T)$ , is well obeyed at high temperatures, say, above 25 K, but the low-temperature behavior deviates strongly from the standard relaxation in paramagnetic metals. As shown in Fig. 16, an additional contribution to the relaxation rate emerges on top of the usual Korringa relaxation. This additional contribution rising at low temperatures has been attributed to the onset of antiferromagnetic fluctuations in the vicinity of  $P_c$  [153–155]. On the other hand, in the lower-temperature regime, the relaxation rate follows a law such that  $T_1T = C(T + \Theta)$ , as shown in Fig. 16. This is the Curie-Weiss behavior for the relaxation which is to be observed in a 2D fluctuating antiferromagnet [156–159]. Similar behavior is also found in a <sup>13</sup>C NMR study [160].

The positive Curie–Weiss temperature  $\Theta$ , which provides the energy scale of the fluctuations, becomes zero when pressure is equal to  $P_c$  (the quantum critical conditions). When  $\Theta$  becomes large comparable to T, the standard relaxation mechanism is expected to recover down to low temperatures, in agreement with the observation at very high pressures [161].



**Fig. 15.** Field dependence of  $1/(T_1T)$  for  $H \parallel a$  and  $H \parallel b'$  obtained by the NMR study on (TMTSF)<sub>2</sub>ClO<sub>4</sub> [103].



**Fig. 16.** Temperature dependence of the nuclear relaxation time multiplied by temperature versus temperature according to the data of Ref. [152]. A Korringa regime,  $T_1T$  = const is observed down to 25 K. The 2D AF regime is observed below  $\approx$  15 K and the small Curie–Weiss temperature of the 9 kbar run is the signature of the contribution of quantum critical fluctuations to the nuclear relaxation. The Curie–Weiss temperature becomes zero at the QCP. These data show that the QCP should be slightly below 9 kbar with the present pressure scale. The inset shows that the organic superconductor (TMTSF)<sub>2</sub>ClO<sub>4</sub> at ambient pressure is very close to fulfill quantum critical conditions.

The existence of fluctuations is also observed as anomalous behavior in transport. At  $P = P_c$ , the inelastic scattering in transport reveals at once a strong linear term at low temperatures, as presented in a log-log plot of the resistivity versus *T*, Fig. 17. This strongly linear behavior evolves to quadratic behavior in the high-temperature regime. As pressure is increased away from  $P_c$ , the resistivity exhibits a general tendency to become quadratic at all temperatures [153] (see Figs. 17 and 1). The existence of a linear temperature dependence of the resistivity is *at variance* with the  $T^2$  dependence expected from the ordinary electron-electron scattering in a conventional Fermi liquid, indicating that the dominant scattering involves spin fluctuations.

Furthermore, the investigation of both transport and superconductivity under pressure in  $(TMTSF)_2PF_6$  has established a correlation between the amplitude of the linear temperature dependence of the resistivity and the value of  $T_c$ , as displayed in Fig. 18. This correlation suggests a common origin for the inelastic scattering of the metallic phase and pairing in the SC phase  $(TMTSF)_2PF_6$  [153], as discussed in the rest of this section.

Within the framework of a weak-coupling limit, the problem of the interplay between antiferromagnetism and superconductivity in the Bechgaard salts has been theoretically worked out using the renormalization group (RG) approach [159,81] as summarized below. The theories take into account only the 2D problem. The RG integration of high-energy electronic degrees of freedom was carried out down to the Fermi level, and leads to a renormalization of the couplings at the temperature T [41,82,159]. The RG flow superimposes the  $2k_F$  electron-hole (density wave) and Cooper pairing many-body processes, which combine and interfere at every order of perturbation. As a function of the 'pressure' parameter  $t'_b$ , i.e. the



Fig. 17. A log-log plot of the inelastic longitudinal resistivity of (TMTSF)<sub>2</sub>PF<sub>6</sub> below 20 K, according to Ref. [153].



**Fig. 18.** Coefficient *A* of linear resistivity as a function of  $T_c$  plotted versus  $T_c/T_{c0}$  for (TMTSF)<sub>2</sub>PF<sub>6</sub>.  $T_c$  is defined as the midpoint of the transition and the error bars come from the 10% and 90% points, and  $T_{c0}$  is defined as  $T_{c0} = 1.23$  K, the maximal  $T_c$  under the pressure of 8 kbar in the SDW/SC coexistence regime. The dashed line is a linear fit to all data points excluding that at  $T_c = 0.87$  K, according to Ref. [153].

unnesting interchain coupling, a singularity in the scattering amplitudes signals an instability of the metallic state toward the formation of an ordered state at some characteristic temperature scale. At low  $t'_b$ , nesting is sufficiently strong to induce a SDW instability in the temperature range of experimentally observed  $T_{SDW} \sim 10-20$  K. When the antinesting parameter approaches the threshold coupling  $t'_b^*$  from below ( $t'_b \approx 25.4$  K using the above param-

When the antinesting parameter approaches the threshold coupling  $t_b^*$  from below ( $t_b^{**} \approx 25.4$  K using the above parameters),  $T_{SDW}$  sharply decreases as a result of an interference between the Cooper and the Peierls channel (SDW correlations). This situation leads in turn to an attractive pairing in the SC *d*-wave (SCd) channel. This gives rise to an instability of the normal state against SCd order at the temperature  $T_c$  with pairing coming from antiferromagnetic spin fluctuations between carriers of neighboring chains. Such a pairing model actually supports the conjecture of interchain pairing in order for the electrons to avoid the Coulomb repulsion made by V. Emery in 1983 and 1986 [33,34].

The calculated phase diagram shown in Fig. 19 with reasonable parameters  $g_1 = g_2/2 \approx 0.32$  for the backward and forward scattering amplitudes respectively and  $g_3 \approx 0.02$  for the longitudinal Umklapp scattering term [159,155] captures the essential features of the experimentally-determined phase diagram of (TMTSF)<sub>2</sub>PF<sub>6</sub> presented in Fig. 1.

Sedeki et al. [162] have proceeded to an evaluation of the imaginary part of the one-particle self-energy. In addition to the regular Fermi-liquid component, whose scattering rate goes as  $T^2$ , low-frequency spin fluctuations yield  $\tau^{-1} = aT\xi$ , where *a* is a constant and the antiferromagnetic correlation length  $\xi(T)$  increases according to  $\xi = c(T + \Theta)^{-1/2}$  as  $T \to T_c$ , where  $\Theta$  is the temperature scale for spin fluctuations [162]. It is then natural to expect the Umklapp resistivity to contain (in the limit  $T \ll \Theta$ ) a linear term *AT*, whose magnitude would presumably be correlated with  $T_c$ , as both scattering and pairing are caused by the same antiferromagnetic correlations. The observation of a *T*-linear law for the resistivity up to 8 K in (TMTSF)<sub>2</sub>PF<sub>6</sub> under a pressure of 11.8 kbar as displayed in Fig. 17 is therefore consistent with the value of  $\Theta = 8$  K determined from NMR relaxation at 11 kbar displayed in Fig. 16. More recently, Bakrim and Bourbonnais [163] studied



**Fig. 19.** Calculated phase diagram of the quasi-one-dimensional electron gas model from the renormalization group method at the one-loop level [159].  $\Theta$  and the dash-dotted line defines the temperature region of the Curie–Weiss behavior for the inverse normalized SDW response function.

the effects of electron-phonon interactions on the SC and SDW channels. Interestingly, it is revealed that electron-phonon coupling enhances spin fluctuation, leading to unusual phenomena such as the positive isotope effect.

We add one comment that, in  $(TMTSF)_2X$ , the existence of the quantum critical point is actually not trivial because the boundary between the SDW and SC phases is a first-order phase transition within the pressure-temperature phase diagram, in contrast to ordinary theories on quantum criticality assuming a second-order transition. However, it has been recently revealed that other typical "quantum critical" materials such as iron pnictides [164] indeed exhibit a first-order-like-behavior in the vicinity of the quantum critical point, evidenced by phase separation between magnetically ordered and paramagnetic phases detected by  $\mu$ SR studies [165]. Thus, it is now getting clearer that the quantum criticality near a first-order transition observed in (TMTSF)<sub>2</sub>X probably shares general and important physics with a broad class of materials.

#### 6. Conclusion

Both experimental and theoretical results point to the contribution of electron correlations to the SC pairing problem. The extensive experimental evidence in favor of the emergence of superconductivity in the  $(TM)_2 X$  family next to the stability pressure threshold for antiferromagnetism has shown the need for a unified description of all electronic excitations that lies at the core of both density-wave and SC correlations. In this matter, the recent progresses of the renormalization group method for the 1D–2D electron gas model have resulted in predictions about the possible symmetries of the SC order parameter when a purely electronic mechanism is involved, predictions that often differ from phenomenologically based approaches to superconductivity but are in fair agreement with recent experimental findings.

To summarize, firstly, the SC order parameter is displaying lines of nodes that are governing the stability against impurity and thermodynamics of the SC phase. Important constraints on the nodal position have been obtained by the field angular dependence of the specific heat. Secondly, electron scattering in the metallic phase above  $T_c$  suggests the existence of strong antiferromagnetic fluctuations leading to the possibility of a spin-mediated pairing in the SC phase. The pairing mechanism behind organic superconductivity is likely different from the proposal made by Little, but it is nevertheless a phonon-less mechanism, at least in  $(TM)_2 X$  superconductors.

What is also emerging from the work on these prototype 1D organic superconductors is their very simple electronic nature with only a single band at the Fermi level, no prominent spin orbit coupling and extremely high chemical purity and stability. They should be considered in several respects as model systems to inspire the physics of the more complex high  $T_c$  superconductors, especially for pnictides and electron-doped cuprates. Most concepts discovered in these simple low-dimensional conductors may also become of interest for the study of other 1D or Q1D systems such as carbon nanotubes, artificial 1D structures, the purple bronze superconductor  $Li_{0.9}Mo_6O_{17}$  with Mo-O chains [166,167], the newly-discovered telluride superconductor  $Ta_4Pd_3Te_{16}$  with Ta-Pd chains [168], and the recently discovered  $A_2Cr_3As_3$  (A = K, Rb, Cs) materials comprising [( $Cr_3As_3$ )<sup>2</sup>-]<sub> $\infty$ </sub> chains [169,170]. It should be noted that the electronic anisotropy of the latter two classes of compounds seems to be weaker than originally expected [171,172] and much weaker than those of the Bechgaard superconductors. Nevertheless, unconventional behaviors, such as possible nodal superconductivity in  $Ta_4Pd_3Te_{16}$  [173] and unusually large  $H_{c2}$  in  $Li_{0.9}Mo_6O_{17}$  [174] and  $A_2Cr_3As_3$  [169,170,172], resemble those observed in (TMTSF)<sub>2</sub>X and thus it is interesting to explore the common nature of Q1D superconductivity amongst a wide class of materials. Of course, serious work using clean single crystals should be accomplished before truly establishing any 1D/Q1D physics governing SC properties. This is actually what has been done on the Bechgaard salts for more than 30 years.

This article shows that there is still plenty of food for thought in the field of organic superconductors.

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